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& APPLIED SCIENCE

Electron and phonon thermal conductivity in high entropy carbides with variable carbon content



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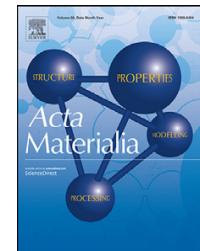
Acta Materialia 196 231–239 (2020)



Contents lists available at [ScienceDirect](#)

Acta Materialia

journal homepage: www.elsevier.com/locate/actamat



Full length article

Electron and phonon thermal conductivity in high entropy carbides with variable carbon content



Christina M. Rost^{a,b}, Trent Borman^c, Mohammad Delower Hossain^c, Mina Lim^d, Kathleen F. Quiambao-Tomko^e, John A. Tomko^e, Donald W. Brenner^d, Jon-Paul Maria^c, Patrick E. Hopkins^{a,e,f,*}

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^b Department of Physics and Astronomy, James Madison University, Harrisonburg, VA 22807, USA

^c Department of Materials Science and Engineering, The Pennsylvania State University, University Park, PA 16802, USA

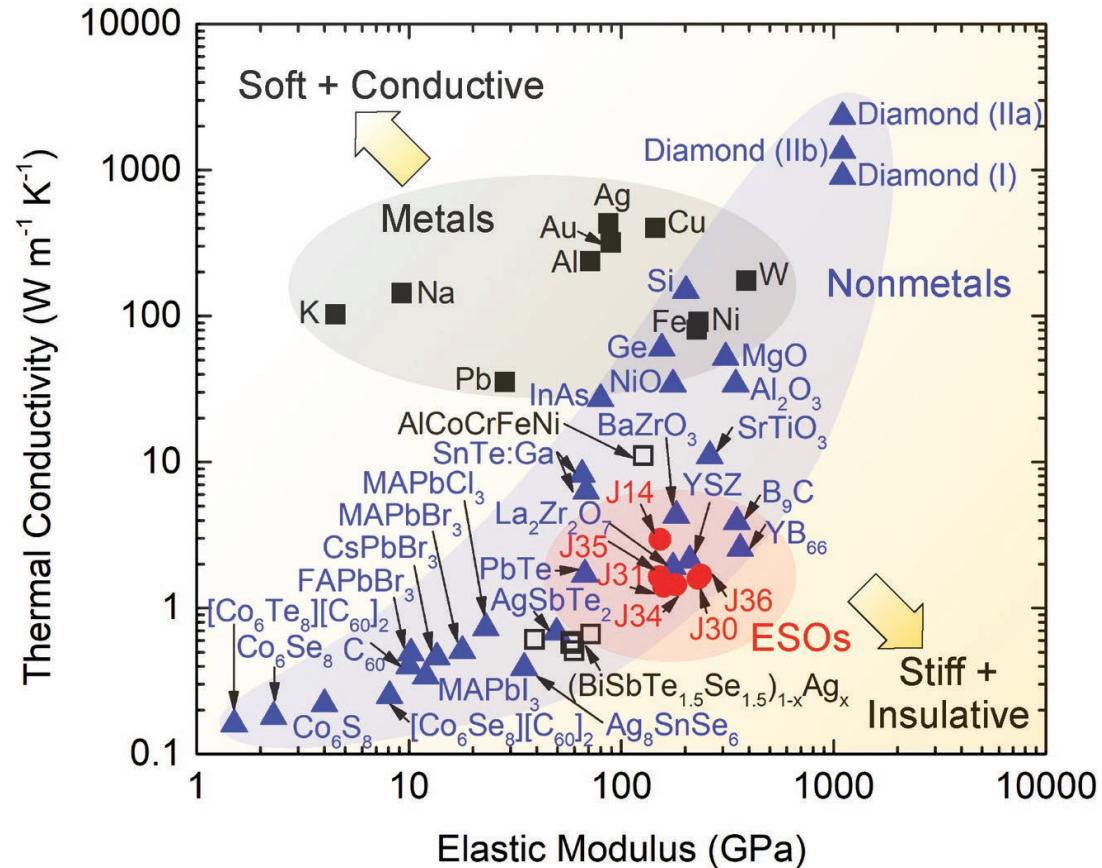
^d Department of Materials Science and Engineering, North Carolina State University, Raleigh, NC 27695, USA

^e Department of Materials Science and Engineering, University of Virginia, Charlottesville, VA 22904, USA

^f Department of Physics, University of Virginia, Charlottesville, VA 22904, USA

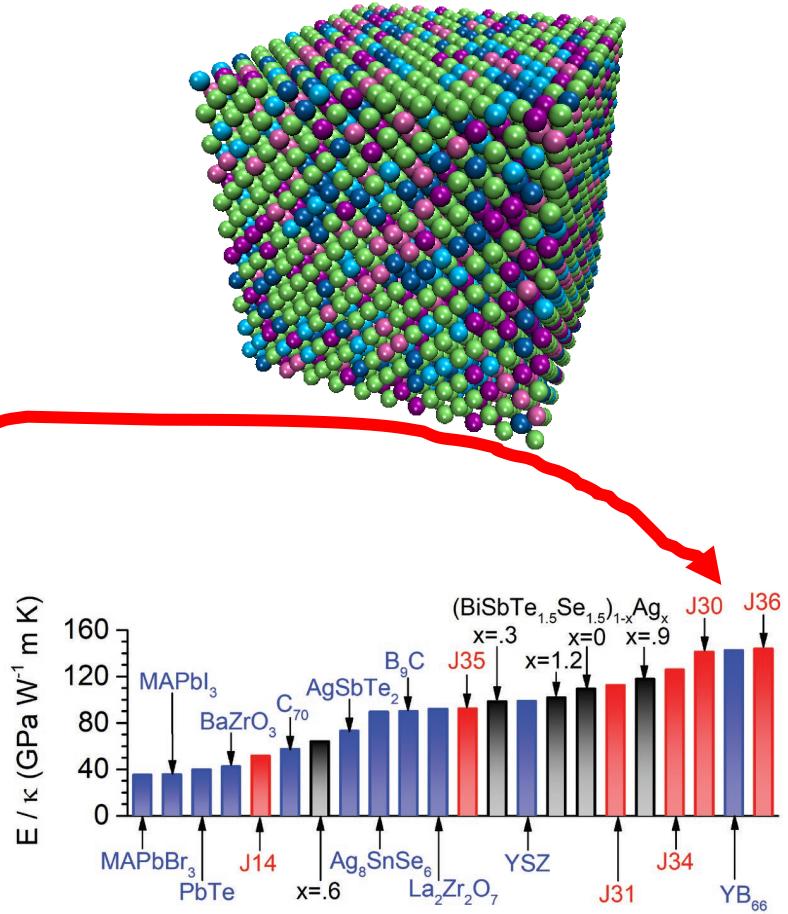
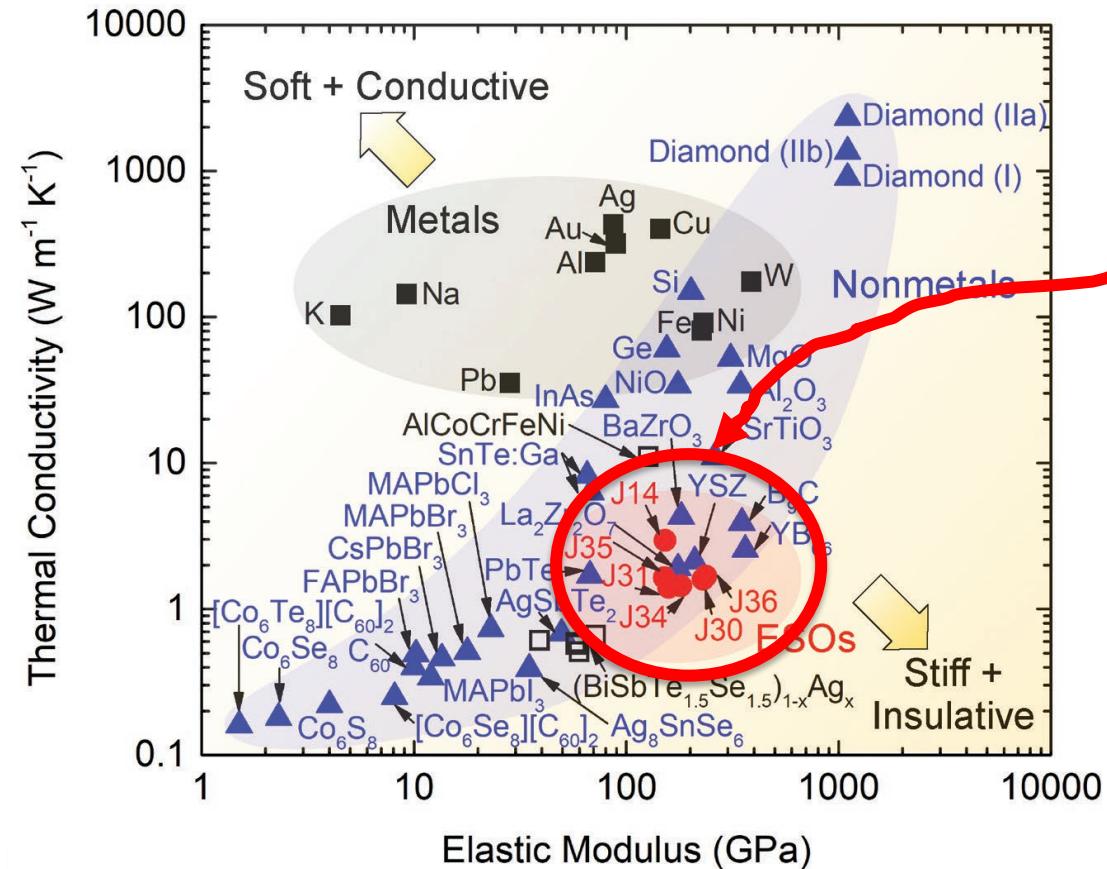


Thermal conductivity – the “mechanical” perspective

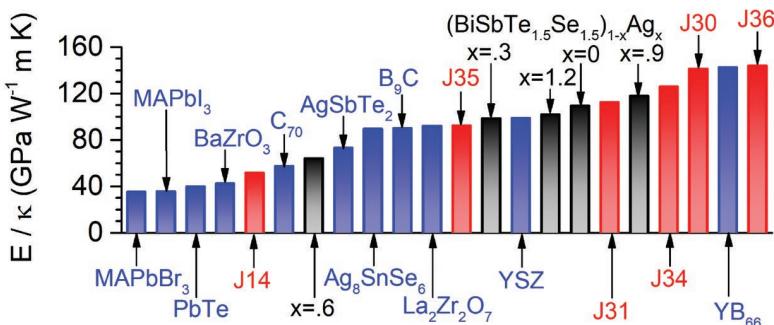
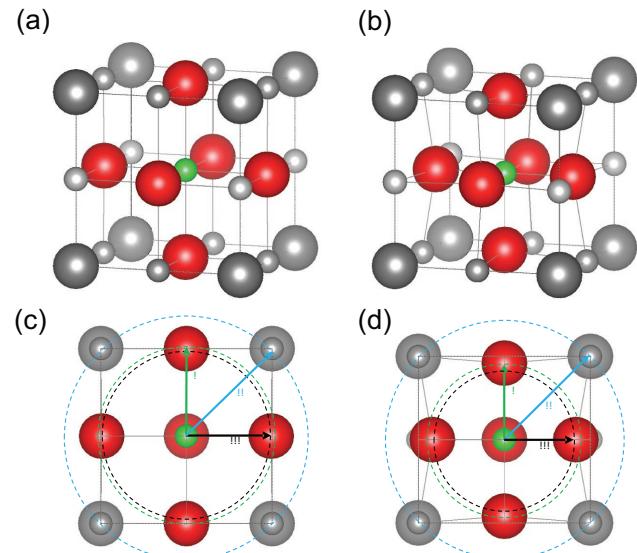
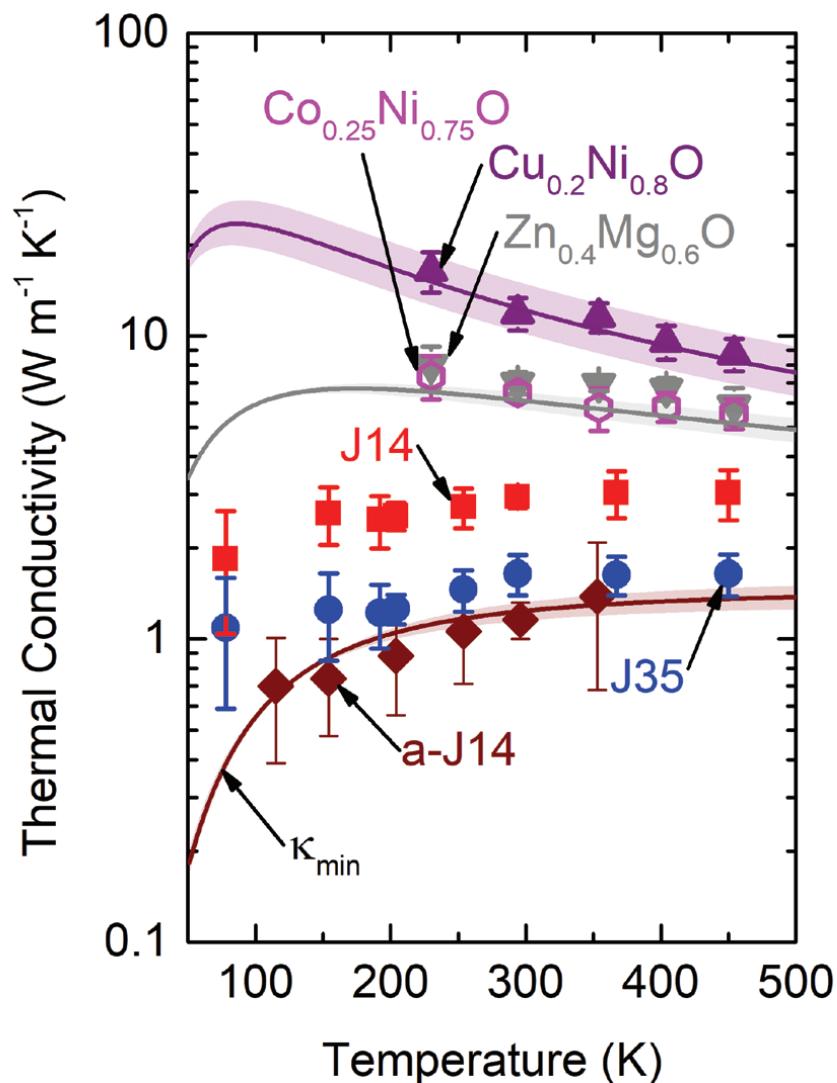


$$\kappa \propto \frac{E}{M_{\text{avg}}}$$

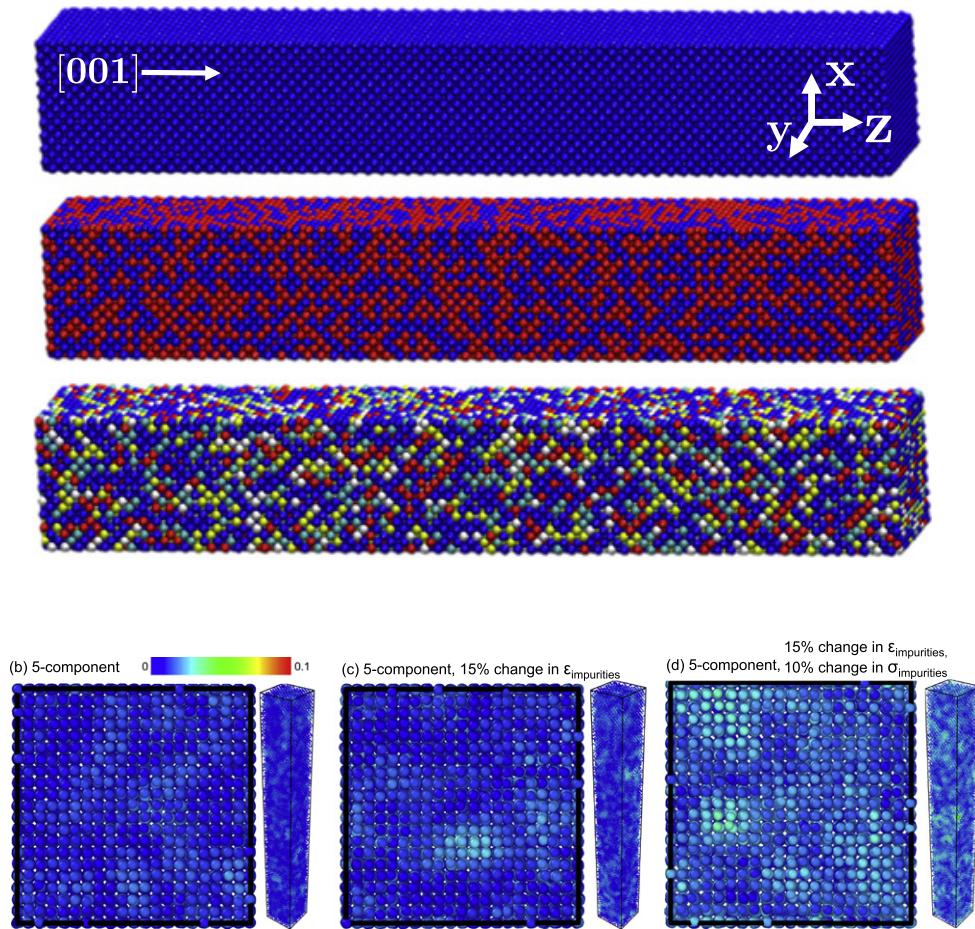
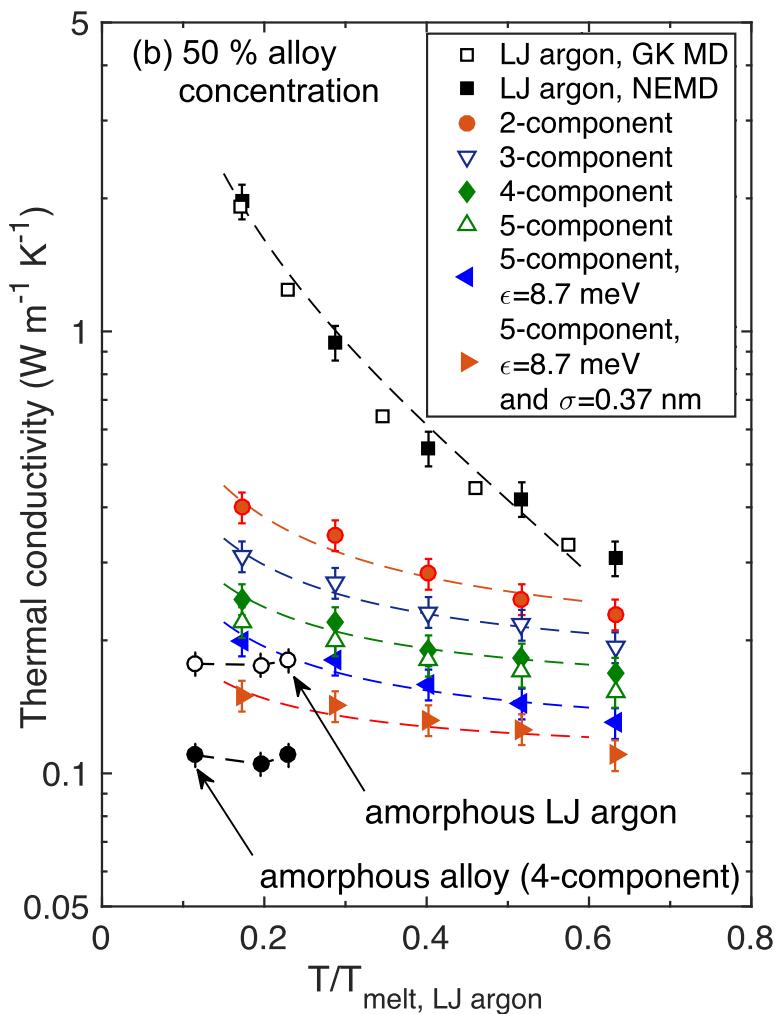
Thermal conductivity of high entropy oxides



Ultralow phonon conduction enabled by lattice distortion



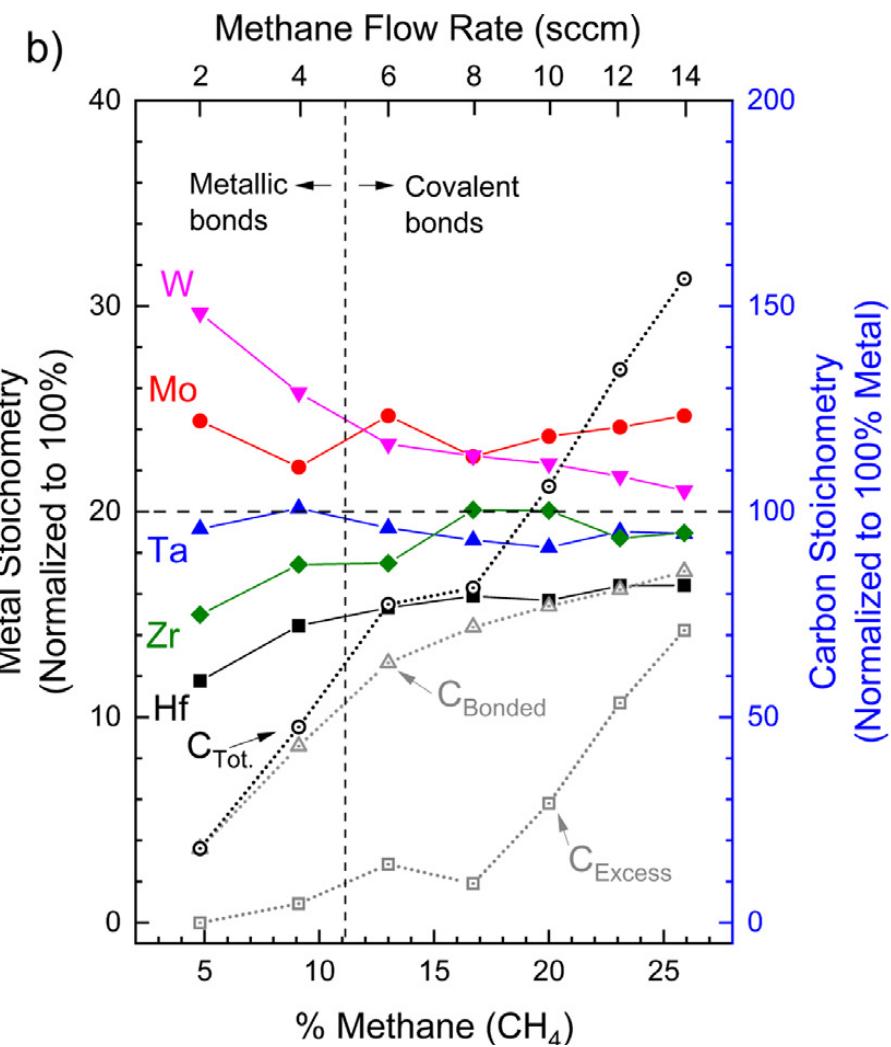
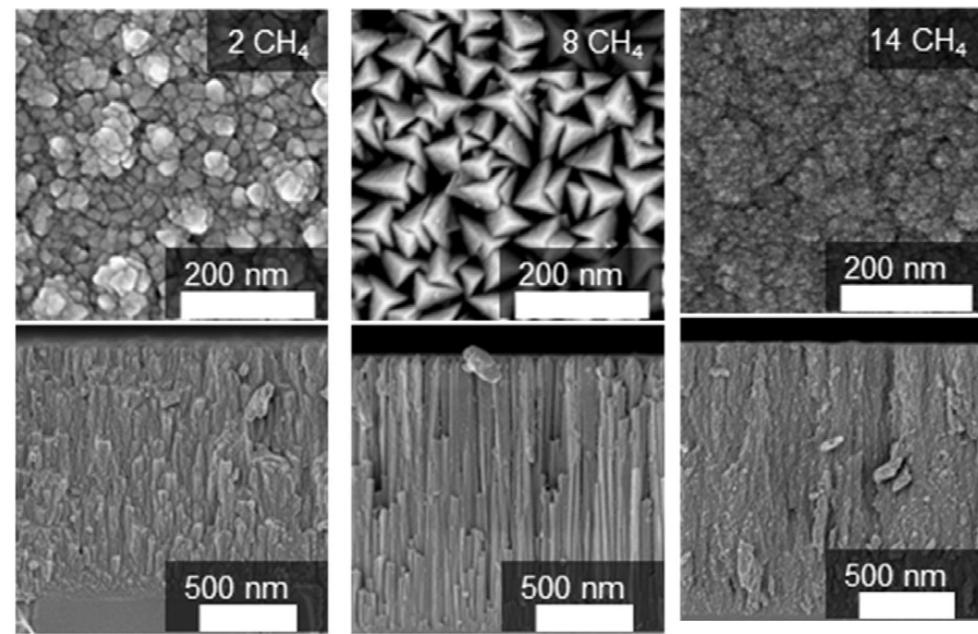
Ultralow phonon conduction enabled by lattice distortion



Electron vs. phonon heat conduction in HE ceramics

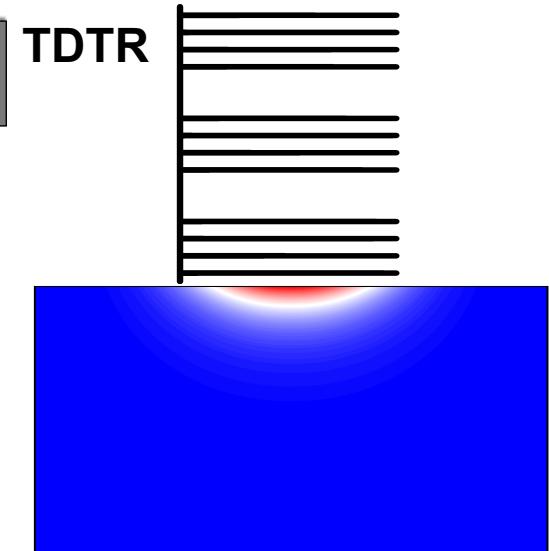
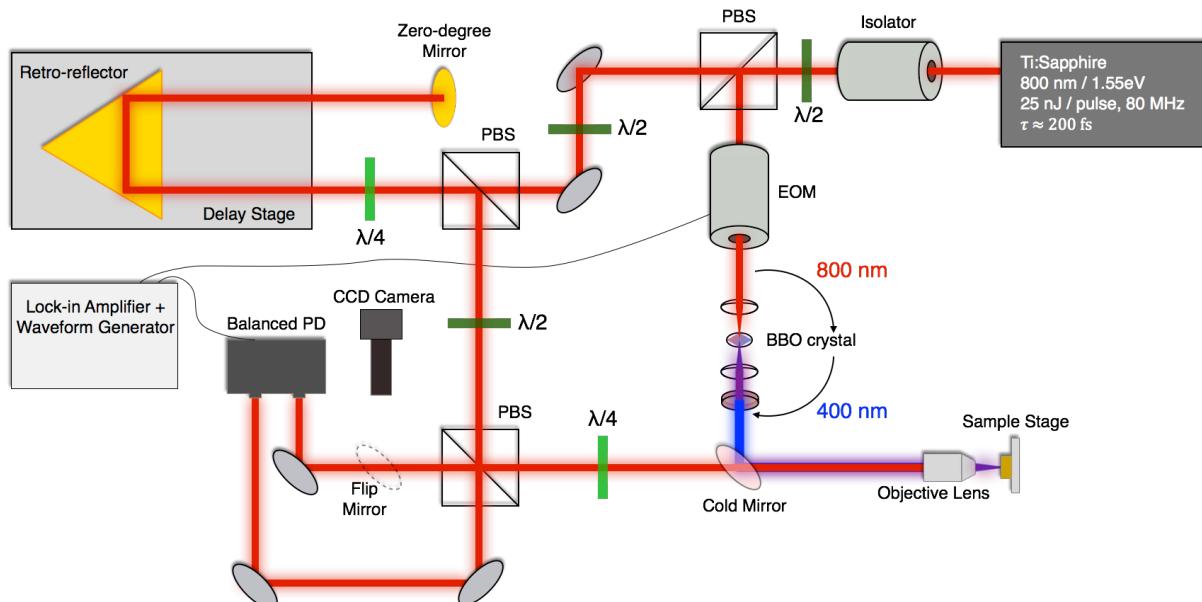
- Phonon conduction reduced in HE-ceramics due to increased phonon scattering from chemical disorder
- Prior work focused on oxides with no free carriers to contribute to thermal conduction
- What is interplay between electrons and phonons on heat conduction? Study in HE-carbides

HE carbide thin films (JP Maria - PSU)



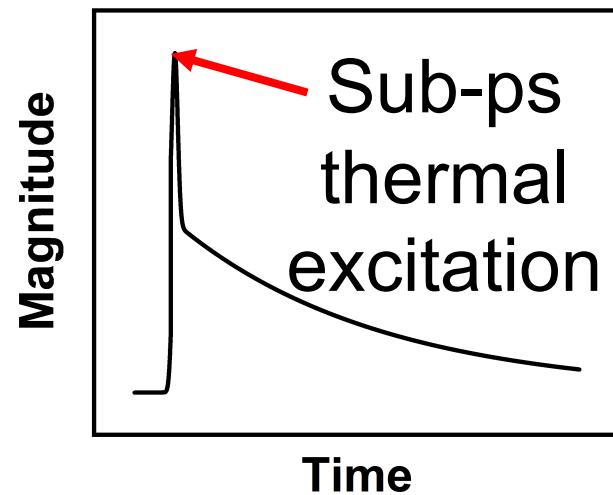
Thermal conductivity measurements – TDTR

Thin film or “near surface” measurements



TDTR Reviews and Analyses

- Rev. Sci. Instr.* **75**, 5119;
Rev. Sci. Instr. **79**, 114902
J. Heat Trans. **132**, 081302;
Ann. Rev. Heat Trans. **16**, 159



Our recent TDTR measurements of the thermal conductivity of HE ceramics: bulk and thin films

Journal of Materiomics 5 (2019) 337–343

Contents lists available at ScienceDirect

Journal of Materiomics

journal homepage: www.journals.elsevier.com/journal-of-materiomics/

A high-entropy silicide: $(\text{Mo}_{0.2}\text{Nb}_{0.2}\text{Ta}_{0.2}\text{Ti}_{0.2}\text{W}_{0.2})\text{Si}_2$

Joshua Gild ^a, Jeffrey Braun ^b, Kevin Kaufmann ^c, Eduardo Marin ^c, Tyler Harrington ^a,
Patrick Hopkins ^b, Kenneth Vecchio ^{a,c,*}, Jian Luo ^{a,c,*}



Journal of the European Ceramic Society 38 (2018) 3578–3584

Contents lists available at [ScienceDirect](#)

Journal of the European Ceramic Society

journal homepage: www.elsevier.com/locate/jeurceramsoc

Original Article

High-entropy fluorite oxides

Joshua Gild^a, Mojtaba Samiee^b, Jeffrey L. Braun^c, Tyler Harrington^a, Heidy Vega^b,

Patrick E. Hopkins^c, Kenneth Vecchio^{a,b}, Jian Luo^{a,b,c*}

Ceramics International 46 (2020) 6906–6913

Contents lists available at ScienceDirect

Ceramics International

journal homepage: www.elsevier.com/locate/ceramint

CERAMICS
INTERNATIONAL

Thermal conductivity and hardness of three single-phase high-entropy metal diborides fabricated by borocarbothermal reduction and spark plasma sintering

Joshua Gild^a, Andrew Wright^b, Kathleen Quiambao-Tomko^c, Mingde Qin^a, John A. Tomko^d, Md Shafkat bin Hoque^a, Jeffrey L. Braun^c, Blake Bloomfield^d, Daniel Martinez^{b,*}, Tyler Harrington^a, Kenneth Vecchio^{a,b,*}, Patrick E. Hopkins^{c,d,e}, Jian Luo^{a,b,*}

COMMUNICATION

Ceramics

Charge-Induced Disorder Controls the Thermal Conductivity of Entropy-Stabilized Oxides

Jeffrey L. Braun, Christina M. Rost, Mina Lim, Ashutosh Giri, David H. Olson, George N. Kotsonis, Gheorghe Stan, Donald W. Brenner, Jon-Paul Maria, and Patrick E. Hopkins*

ADVANCED MATERIALS

www.advmat.de

Acta Materialia 196 (2020) 231–239

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 ELSEVIER

Acta Materialia

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Full length article

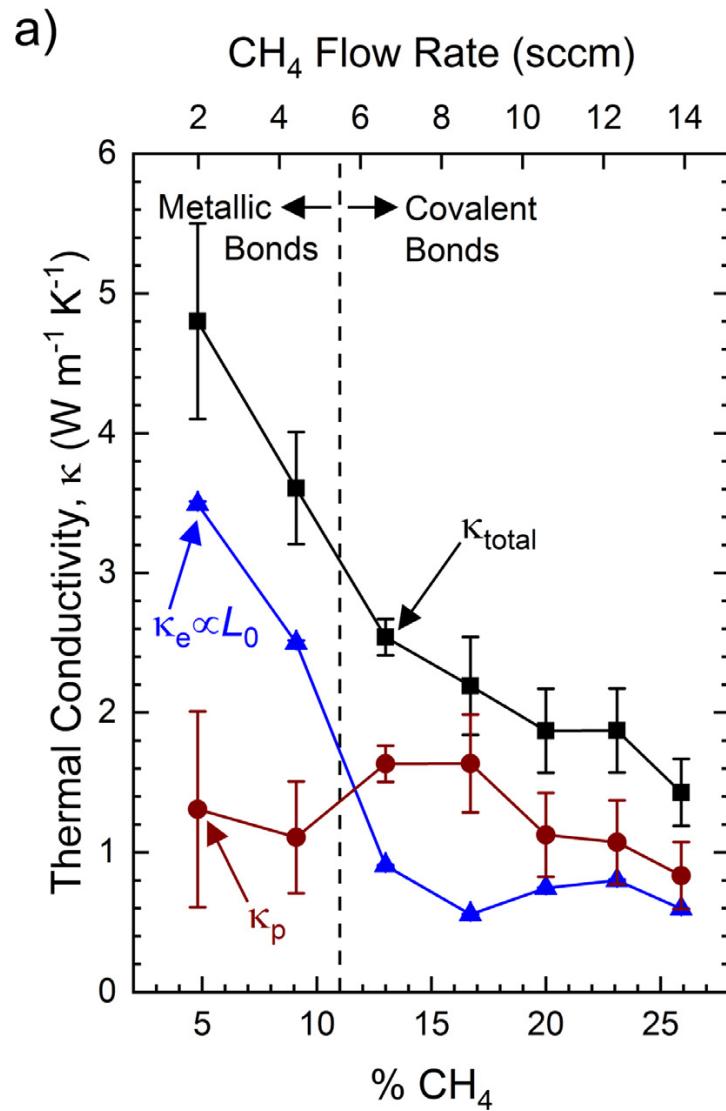
Electron and phonon thermal conductivity in high entropy carbides with variable carbon content

Christina M. Rost ^{a,b}, Trent Borman ^c, Mohammad Delower Hossain ^c, Mina Lim ^d, Kathleen F. Quiambao-Tomko ^e, John A. Tomko ^e, Donald W. Brenner ^d, Jon-Paul Maria ^c, Patrick E. Hopkins ^{a,c,f*}

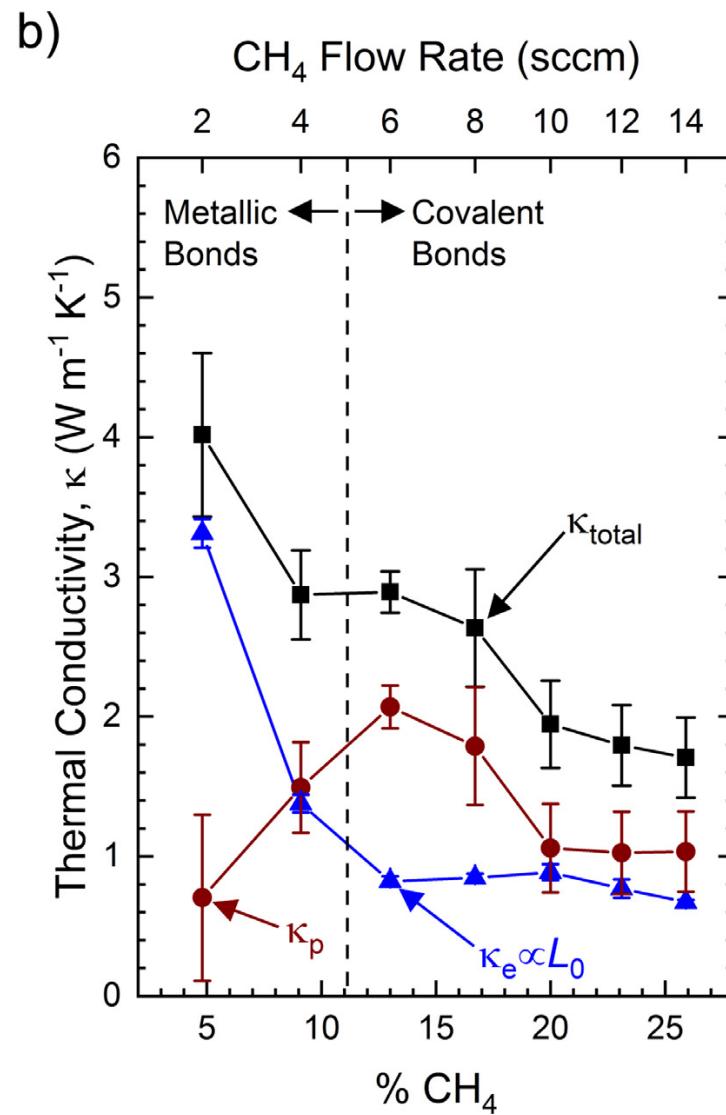


Thermal conductivity of HECs

1-2 μm thick film



100 nm film



What what do we assume about κ_e and L ?

The Widemann-Franz Law and $L=L_0$

$$\kappa_e = \sigma LT$$

1853. A N N A L E N No. 8.
 DER PHYSIK UND CHEMIE.
 BAND LXXXIX.

I. *Ueber die Wärme-Leitfähigkeit der Metalle;*
von G. Wiedemann und R. Franz.

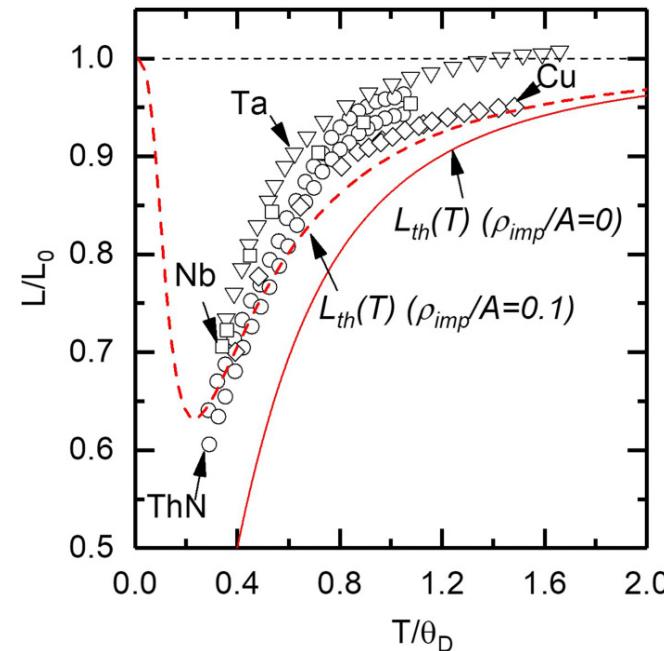
What what do we assume about κ_e and L ?

The Wiedemann-Franz Law and $L=L_0$

Only valid at low
or high T

Or

If sufficient elastic
electron scattering



PHYSICAL REVIEW MATERIALS 1, 065002 (2017)

Phonon and electron contributions to the thermal conductivity of VN_x epitaxial layers

Qiye Zheng,^{1,*} Antonio B. Mei,¹ Mohit Tuteja,¹ Davide G. Sangiovanni,^{2,3} Lars Hultman,³ Ivan Petrov,^{1,3} J. E. Greene,^{1,3} and David G. Cahill¹

¹Department of Materials Science and Engineering, Frederick Seitz Materials Research Laboratory, University of Illinois at Urbana-Champaign, 104 South Goodwin, Urbana, Illinois 61801, USA

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³Department of Physics (IFM), Linköping University, SE-581 83 Linköping, Sweden

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The Wiedemann-Franz Law and L more general form

$$L_{\text{th}} = \frac{\rho_{\text{imp}} + \left(\frac{\Theta_D}{T}\right)^5 J_5\left[\frac{\Theta_D}{T}\right]}{\rho_{\text{imp}} + \left(\frac{\Theta_D}{T}\right)^5 J_5\left[\frac{\Theta_D}{T}\right] \left(1 + \frac{3}{\pi^2} \left(\frac{k_F}{q_D}\right)^2 \left(\frac{\Theta_D}{T}\right)^2 - \frac{1}{2\pi^2} \frac{J_7\left[\frac{\Theta_D}{T}\right]}{J_5\left[\frac{\Theta_D}{T}\right]}\right)} L_0$$

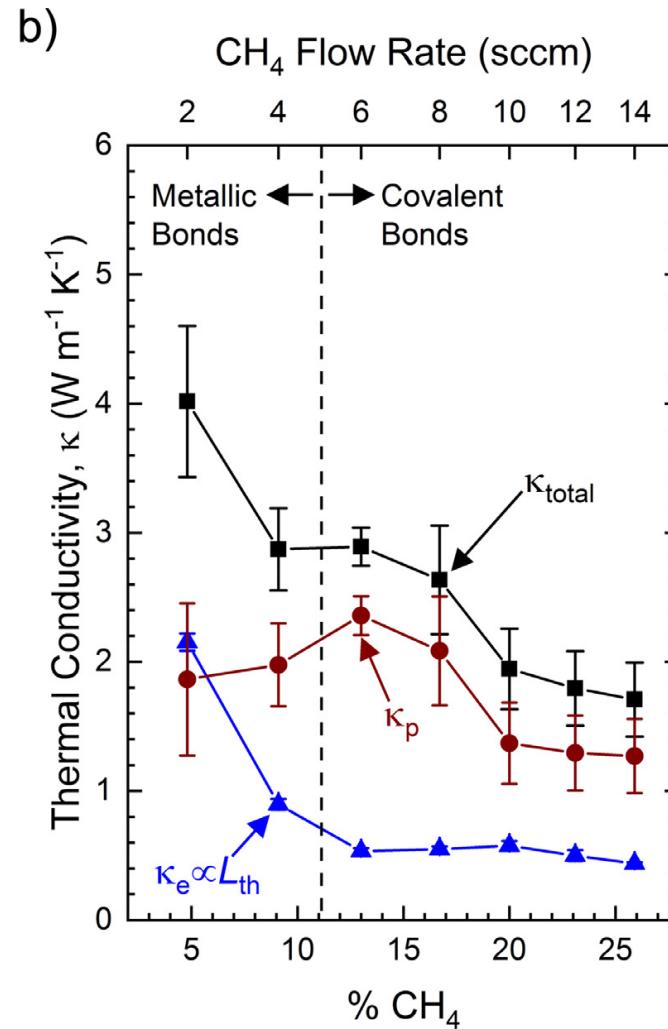
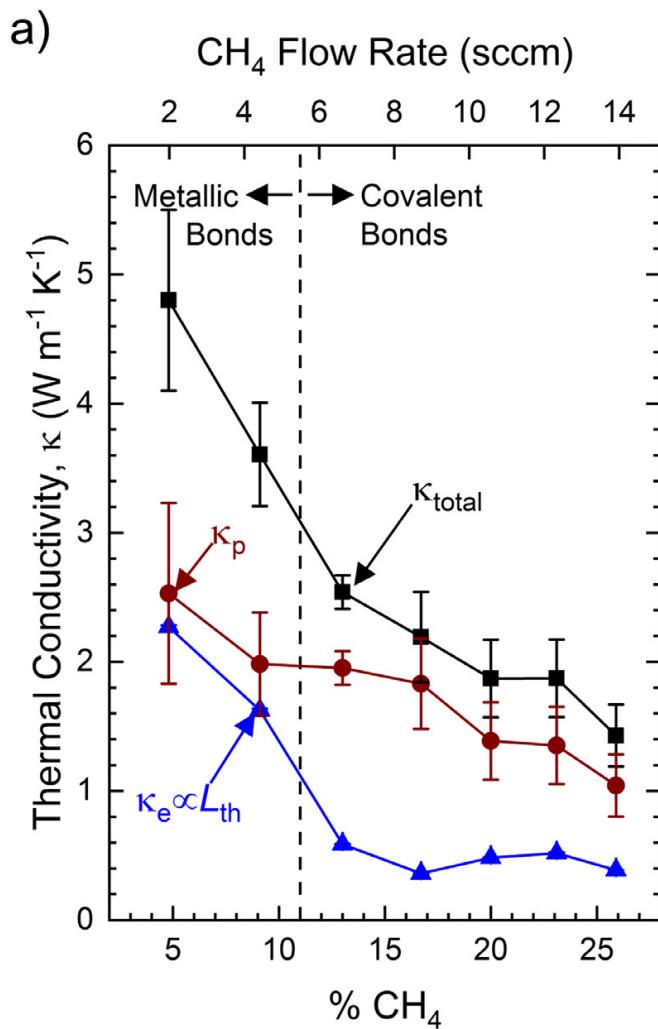
THE THERMAL CONDUCTIVITY OF METALS

By R. E. B. MAKINSON, St John's College

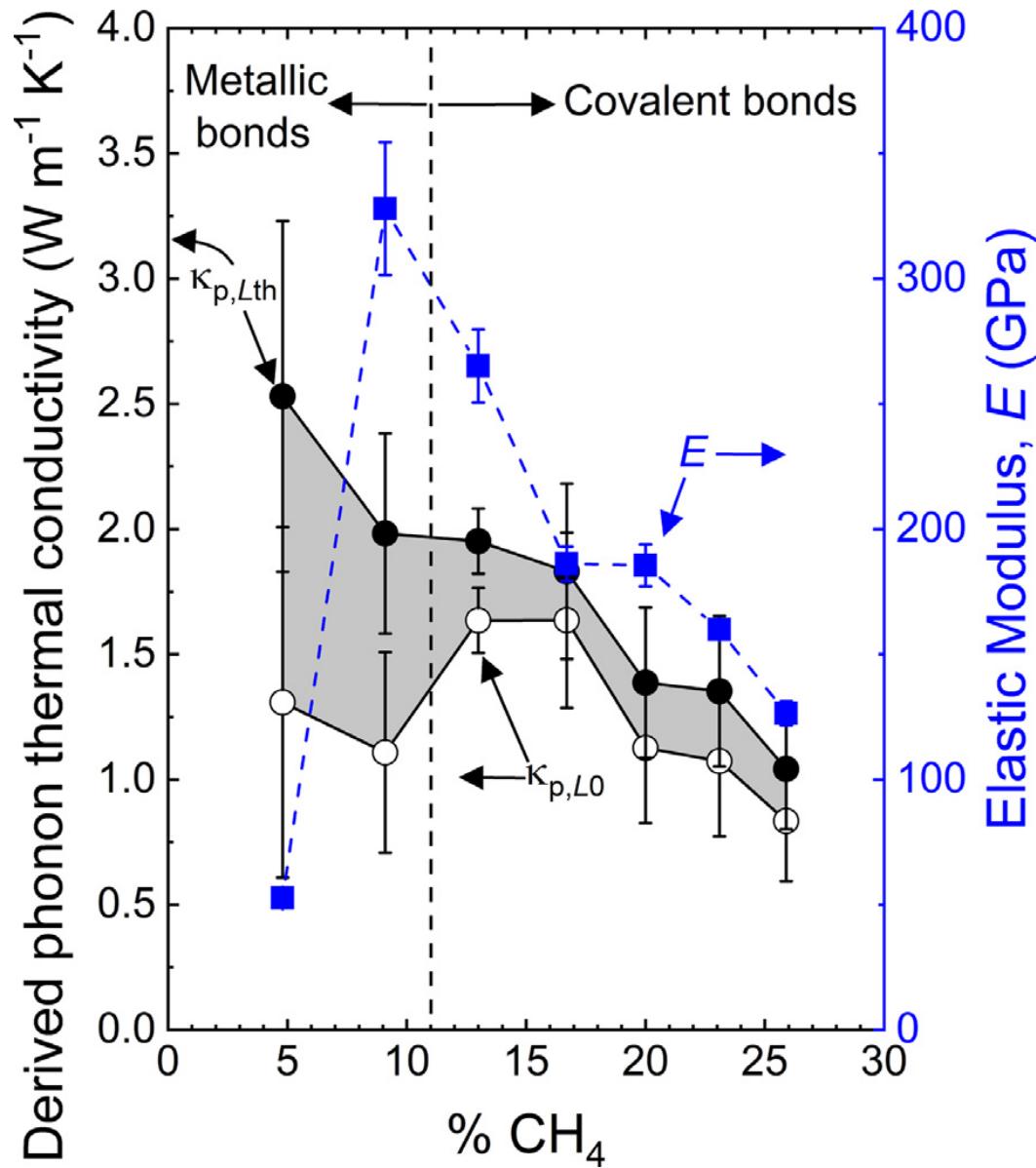
[Communicated by Mr A. H. WILSON]

[Received 9 May, read 16 May 1938]

Does assumption of L change our conclusion about HECs? No



Phonon conductivity of HECs scale with modulus



But only in non-metallic phase

$$\kappa \propto \frac{E}{M_{\text{avg}}}$$

Summary: Carbon content dictates electron and phonon thermal conductivity in high entropy ceramics through both electron thermal conductivity changes and modulus changes

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