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Full Length Article

# The thermal and mechanical properties of hafnium orthosilicate: Experiments and first-principles calculations



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## ABSTRACT

Hafnium orthosilicate (HfSiO<sub>4</sub>: hafnon) has been proposed as an environmental barrier coating (EBC) material to protect silicon and silicon-based ceramic materials at high temperatures and as a candidate dielectric material in microelectronic devices. It can naturally form at the interface between silicon dioxide (SiO<sub>2</sub>) and hafnia (HfO<sub>2</sub>). When used as an EBC its coefficient of thermal expansion (CTE) should match that of the protecting layer (e.g. silicon and SiC composites) to reduce the stored elastic strain energy, and thus the risk of failure of these systems. In this work, the physical, mechanical, thermodynamic and thermal transport properties of hafnon have been investigated using a combination of density functional theory (DFT) calculations and experimental assessments. The average linear coefficient of thermal expansion (CTE) calculated using the quasi-harmonic approximation increase from  $3.06 \times 10^{-6} \ K^{-1}$  to  $6.36 \times 10^{-6} \ K^{-1}$ , as the temperature increases from 300 to 1500 K, in agreement with both X-ray diffraction lattice parameter and dilatometry measurements. The predicted thermal conductivity from Boltzmann transport theory is approximately 16.1 W/m.K at 300 K. The thermal conductivity of our samples using both hot disk and laser flash measurements gave a value of 13.3 W/m.K. This slightly lower value is expected and is indicative of residual disorder in the experimental samples, which is absent in the theoretical analysis. First-principles calculations and nanoindentation techniques are used to assess the ambient temperature elastic constants and bulk modulus respectively. The elastic properties obtained by both approaches agreed to within 5%, validating the computational approach and its future use for the study of the thermomechanical properties of other oxides or silicates.

#### 1. Introduction

Compounds of Group-IV elements have many applications in a wide variety of fields. For instance, orthosilicates such as ZrSiO<sub>4</sub>, HfSiO<sub>4</sub>, ThSiO<sub>4</sub>, and USiO<sub>4</sub>, are effective radiation-resistant materials that are hosts for plutonium during the dismantling of nuclear weapons [1,2]. Zirconium- and hafnium-based borides, carbides, and nitrides possess extremely high melting points, high hardness, but modest oxidation resistance, and may replace silicon-based ceramics for temperatures above 1700 °C [3,4]. Other applications of the group IV oxides arise in thermal barrier and the environment barrier coatings (TBCs and EBCs). For example, yttriua-stabilized zirconia is used as a thermal barrier coating material that is applied to gas turbine components because it is stable, has low thermal conductivity and is conveniently prepared using air-plasma-spraying [5-8], vapor deposition technology [9] or soft hydrothermal synthesis. [10] The group IV silicates have also shown potential as TBC or EBC materials. Ueno et al. examined corrosion behaviors of ZrSiO<sub>4</sub> (zircon) and HfSiO<sub>4</sub> (hafnon) EBC materials in a water vapor environment at 1500 °C on silicon nitride specimens [11]. Although hafnon exhibited higher silica volatility, the underlying substrate experienced noticeably less oxidation and crack propagation. This was thought to be a consequence of hafnon's coefficient of thermal expansion (CTE) match with the silicon nitride substrate. Hisamatsu et al. [12] created an EBC configuration that placed a hafnon layer between a yttria-stabilized hafnia topcoat and a ceramic substrate, and thus protected the substrate interface from cracks arising from stress.

Many of the late Group IV oxides have shown better gate dielectric performances than silicon dioxide in field-effect transistors due to their large dielectric constants, stability in direct contact with silicon, and low leakage current in the ultrathin film regime [13,14]. Hafnium silicates have also been investigated as possible high dielectric candidates to replace  $\mathrm{SiO}_2$  gate dielectrics due to their phase stability, large bandgap, and compatibility with microelectronic fabrication processing environments [15–17]. Wilk et al. obtained a dielectric constant of 11 from their hafnium silicate samples, which corresponds to an equivalent silicon oxide thickness of 17.8 Å . The high thermal stability of hafnium silicate is also of interest since it provides resistance to the thermal aging problems encountered with many dielectric gates [15].

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The physical properties of hafnon have been investigated by both experiments and theoretical calculations. Its Raman-active fundamental frequencies [10,18–20] and its linear coefficient of thermal expansion (CTE) [21,22] were measured. First-principles [23] and molecular dynamics (MD) simulations [24] have provided consistent phonon properties of hafnon with the experiments. However, the Gruneisen parameters of hafnon calculated by a variety of simulation approaches [24–27] have not converged, and no experimental data are currently available for comparison. The thermal transport properties and mechanical properties of hafnon have also not been fully investigated by either theory or experiment.

Reliable data for the thermal and mechanical properties of hafnium silicate are also needed to assess the growing list of applications. Here we conduct a comprehensive assessment of the physical and mechanical properties of hafnon using both first-principles calculations and a variety of experiments. Starting with its lattice structure determined by Speer et al. [28], the phonon dispersion, Gruneisen parameters, CTE, thermal conductivity, and elastic constants and moduli are calculated. Measurements of the CTE of hafnon *via* X-ray diffraction (XRD) and dilatometry, thermal conductivity through hot disk and the laser flash techniques, and the elastic modulus and hardness by the nanoindentation measurements are reported, and compared with our predictions and the results of other studies.

#### 2. Methods

### 2.1. Physical and mechanical property calculations

The Quantum Espresso (QE) package [29,30] was used for structural relaxation and force constant calculations with the finite displacement approach. We applied a revised Perdew-Burke-Ernzerhof (PBEsol) [31] exchange-correlation functional with the GBRV-ultrasoft pseudopotential [32] that treats Hf (5 s, 5p, 5d, 5f, 6 s, and 6p), Si (3 s and 3p) and O (2 s and 2p) as valence states. For structural optimization and selfconsistent calculations, the cutoff energy of plane wave expansion is set to 100 Ry, and the reciprocal space is sampled by a 4 × 4 × 4 Monkhorst-Pack k-mesh [33]. A force convergence criterion is set to be 10<sup>-3</sup> eV/Å for tests on the exchange-correlation functional, the pseudopotential, the cutoff energy, and the k-mesh. Harmonic force constants (FCs) are fitted by the PHONOPY package [34] and the ALAMODE package [35]. For phonon dispersion and second-order force constants (FCs) calculations,  $2 \times 2 \times 2$  supercells with atomic displacements of 0.02 Å and a  $2 \times 2 \times 2$  Monkhorst-Pack k-mesh are generated by PHONOPY to ensure the convergence. We also apply force calculations on 88 configurations of  $2 \times 2 \times 2$  supercells with random displacements to fit cubic FCs using ALAMODE. As hafnon is a polar material, to include the non-analytical correction term [36] that leads to the splitting between longitudinal optical (LO) and transverse optical (TO) modes, the Born charge correction was applied to the phonons, Gruneisen parameters and thermal conductivity calculations.

Gruneisen parameters were calculated according to the definition.

$$\gamma_{qj} = -\frac{\partial \log \omega_{qj}}{\partial \log V} = -\frac{(e_{qj}^*)^{\mathrm{T}} \delta D(q) e_{qj}}{6\omega_{qj}^2} \tag{1}$$

Here V is the unit cell volume,  $\gamma_{qj}$  is the Gruneisen parameter for each q point for the jth phonon band,  $\omega_{qj}$  and  $e_{qj}$  are the corresponding phonon frequency and eigenvector,  $\delta D(q)$  is the change in the dynamical matrix due to a 1% lattice parameter (i.e. 3% volume) increase. It can be either obtained from the difference in dynamical matrices calculated with the lattice parameters a and 1.01~a; or from a Taylor expansion of the harmonic force constants in first power of atomic displacements:  $\Phi_{ij}(u) = \Phi_{ij}(0) + \Sigma_k \Psi_{ijk} u_k + O(u^2)$  where the atomic displacement u corresponds to a uniform 1% lattice constant expansion. In this work, we used the latter approach and later validated it by comparing to the results from the former one. Cubic FCs  $\Psi_{ijk}$  are used to approximate  $\delta D(q)$ . To obtain reliable cubic FCs, it is important to determine the cutoff ra-

dius for each pair of atoms, because considering all the pairs would significantly increase computational cost. Besides, long-distance pairs may introduce noise to the fitting and affect the fitting quality. Therefore, when using ALAMODE, for each triplet of atoms in the fitting of cubic FCs, only Hf-O-Hf, Hf-O-Si, O-Hf-O, and O-Si-O bonds were kept, and all non-bond triplets were excluded. To calculate the Gruneisen parameters, a q-mesh of  $30\times30\times30$  was used to assure convergence of the sums over the first Brillouin zone. Finally, with the fitted cubic FCs and the harmonic phonon frequencies and normal modes obtained from PHONOPY, the Gruneisen parameters of hafnon were calculated using the thirdorder.py script and the ShengBTE code [37].

The volumetric thermal expansion of hafnon was calculated using the quasi harmonic approximation (QHA) approach that is implemented in PHONOPY [38]. Eight conventional cells were created with varied volumes around the equilibrium structure and used to calculate the lattice dynamical properties of each structure. For each temperature, a map of Helmholtz free energies at different volumes was obtained. By fitting the free-energy versus volume curves at each temperature between 300 and 1500 K, the corresponding equilibrium volume could be found, and thus the volume expansion and volumetric CTE were deduced. For a better comparison to experimental measurements from XRD, we also calculated the linear CTE of hafnon,  $\alpha$ , according to the relation between the Gruneisen parameter and linear CTE for anisotropic materials:

$$\alpha_i = (\partial \epsilon_i / \partial T)_{\sigma} = \sum_{i=1}^6 C_{\epsilon} S_{ij}^T \gamma_j \tag{2}$$

In this formula,  $\sigma$  and  $\epsilon$  are respectively the stress and strain tensors, T the temperature,  $C_{\epsilon}$  the constant-strain volumetric heat capacity,  $S_{ij}^T$  the isothermal elastic compliance tensor, and  $\gamma_j$  the average Gruneisen parameter, and (i,j), which vary from 1 to 6, are cartesian components in Voigt format. For hafnon that is a tetragonal system, once we define two average Gruneisen parameters:  $\gamma_1 = \gamma_2 \neq \gamma_3$ , we obtain the linear CTE  $\alpha_1$  and  $\alpha_3$  along the a- and c- axes, respectively as:

$$\alpha_1 = C_{\varepsilon} \left[ \left( S_{11}^T + S_{12}^T \right) \gamma_1 + S_{12}^T \gamma_3 \right] \tag{3}$$

$$\alpha_3 = C_{\varepsilon} \left[ 2S_{12}^T \gamma_1 + S_{22}^T \gamma_3 \right] \tag{4}$$

The thermal conductivity of hafnon was calculated by solving the Boltzmann transport equation within the relaxation-time approximation (RTA) using ALAMODE. The phonon lifetimes were obtained through the phonon linewidth corresponding only to three-phonon scattering processes. This leads to a decrease in the thermal conductivity proportional to 1/T at high temperatures.

## 2.2. Mechanical property predictions

For elastic moduli calculations, Lagrangian strains were applied to the tetragonal unit-cell which contains 24 atoms (see Fig. 2 and captions) to generate deformed structures using the ElaStic code [39]. The total energy of several strained structures is fitted with a second-order polynomial in powers of strain in order to extract the elastic constants. A cross-validation method was then adopted to evaluate the fitting quality. A fourth- or sixth-order polynomial was chosen for fitting and the variation of the elastic constants was kept below 0.1 GPa. The Voigt bulk  $(B_V)$  and shear  $(G_V)$  moduli were calculated from the elastic stiffness constants  $c_{ij}$  and compliances  $S_{ij}$  assuming that the strain was uniformly applied everywhere [40]:

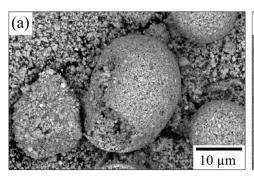
$$B_V = \frac{1}{9} \left[ \left( c_{11} + c_{22} + c_{33} \right) + 2 \left( c_{12} + c_{13} + c_{23} \right) \right] \tag{5}$$

$$G_V = \frac{1}{15} \left[ \left( c_{11} + c_{22} + c_{33} \right) - \left( c_{12} + c_{13} + c_{23} \right) + 3 \left( c_{44} + c_{55} + c_{66} \right) \right] \tag{6}$$

The Reuss bulk,  $B_R$  and shear moduli,  $G_R$  were obtained using, [40].

$$B_{R} = \left[ \left( S_{11} + S_{22} + S_{33} \right) + 2 \left( S_{12} + S_{13} + S_{23} \right) \right]^{-1} \tag{7}$$

$$G_R = 15 \left[ 4 \left( S_{11} + S_{22} + S_{33} \right) - \left( S_{12} + S_{13} + S_{23} \right) + 3 \left( S_{44} + S_{55} + S_{66} \right) \right]^{-1} \tag{8}$$



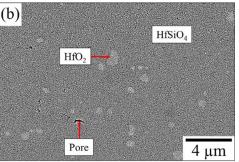
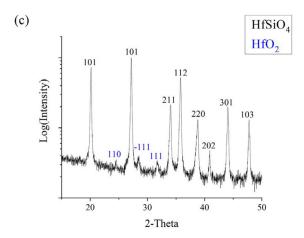


Fig. 1. (a) Example of pre-reacted  $HSiO_4$  powder granules in the as-received condition. (b) The hafnon sample microstructure after spark plasma sintering showing the presence of a small volume fraction of unreacted hafnia inclusions (the lighter contrast regions estimated to be 6–8% volume fraction), and pores (the darker contrast regions estimated to be 2% volume fraction). (c) Room temperature XRD where remnent  $HfO_2$  peaks (in blue) were also identified.



The Hill bulk,  $B_H$  and shear,  $G_H$  moduli were determined as the average of Voigt and Reuss moduli [40].

$$B_H = \frac{1}{2} \left( B_V + B_R \right) \tag{9}$$

$$G_H = \frac{1}{2} \left( G_V + G_R \right) \tag{10}$$

Once the bulk modulus and the shear modulus were calculated, Young's modulus E and Poisson's ratio  $\nu$  were obtained from the linear elastic solid approximation [41]:

$$E = \frac{9BG}{3B+G} \tag{11}$$

$$v = \frac{3B - 2G}{2(3B + G)} \tag{12}$$

## 2.3. Experimental lattice parameter and CTE measurements

Hafnon samples were made from 20 to 60 µm diameter Praxair #02-P6644SG granules, consisting of fine SiO2 and HfO2 paprticles that had been pre-reacted to form sub-micron hafnon particles with a minor amount of yttria-stabilized zirconia (YSZ) ball-mill media used in order to break up larger granules. The milled powder was loaded into a graphite die of 20 mm diameter lined with graphite foil in order to ensure easy removal of the final product from the die, and consolidated via spark plasma sintering using a Thermal Technologies SPS Model 25-10 (Santa Rosa, CA, USA). The SPS process was conducted using a maximum pressure of 65 MPa and a maximum temperature of 1650 °C reached using a heating rate of 150 °C/minute. Samples were held at the maximum temperature and pressure for 40 min prior to cool down. Final bulk material underwent a 1300 °C heat treatment for 24 h to restore oxygen stoichiometry, remove any residual carbon and remove possible stresses due to processing. The resulting microstructure is shown in Fig. 1b. Phase analysis of samples was conducted by X-ray diffraction (XRD) using a PANalytical Empyrean (Malvern Panalytical, Westborough, MA) and by scanning electron microscopy (SEM) using a Helios NanoLab DualBeam microscope (Thermo Scientific, Hillsboro, OR). Density measurements were made using Archimedes' Principle. An average relative density of 97.6% was achieved, assuming a theoretical density for hafnon of 6970 kg/m³. Samples were polished to 1  $\mu m$  with diamond suspension, followed by a final polish using 0.05  $\mu m$  colloidal silica prior to SEM and XRD measurements. The SEM observations, Fig. 1(b), revealed that most of the hafnia and silica had reacted to form hafnon, leaving approximately 6–8% unreacted hafnia. The pore volume fraction was 2.4%. Room temperature XRD results plotted in Fig. 1c as the log of intensity confirmed the presence of a small amount of remnant hafnia within the processed material. Residual hafnia peaks are shown in blue, while all others correspond to HfSiO4. The hafnia content is estimated to be less than 5 vol percent based on XRD, and was consistent with analysis of plan view SEM micrographs where the lighter phase in Fig. 1b represents HfO2 inclusions.

To determine the coefficient of thermal expansion via dilatometry, each sample was first cut into a 15 × 3 × 3 mm rectangular bar, followed by dilatometry using a Netzsch Dil 402c dilatometer (NETZSCH, Burlington, MA, USA). It was then heated in flowing argon at a rate of 3 °C per minute with 60 recordings of length change per minute. The sample was held for 15 min at temperature before the cooling phase was started. The CTE was also determined from changes in the lattice parameter during heating of the samples in an Anton Paar HTK 1200 N non-ambient X-ray diffractometer (Anton Paar, Ashland, VA, USA). In this approach, the sample was radiatively heated from room temperature to 1200 °C at 60 °C/min. The temperature was held constant every 100 °C to capture an X-ray scan of 15 – 60° 2-theta range. Rietveld refinement and lattice determinations were computed for each XRD plot using the HighScore Plus Software (Malvern Panalytical, Malvern, UK). From these data, direction-dependent thermal expansion coefficients were determined for the given temperature range.

## 2.4. Thermal conductivity and elastic property measurement techniques

A hot disk approach using a Hot Disk TPS 3500 (Thermtest Inc., Fredericton, NB, Canada) was used to measure the thermal conductivity of

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**Table 1**Lattice parameters from simulations and experiments. The relative difference between prediction and the experimental values are shown in parentheses. The second experimental values followed by a (\*) sign are from our own XRD measurements.

	PBEsol(present work)	Experiment [28]	LDA [23] (ABINIT)	LDA [26] (CASTEP)	GGA [27] (WIEN2k)	GGA [25] (CASTEP)	Empirical potential [24]
a (Å)	6.5822 (0.15%)	6.5725 6.571(*)	6.61 (0.57%)	6.68 (1.64%)	6.64 (1.03%)	6.76 (2.85%)	6.48 (1.41%)
c (Å)	5.9665 (0.06%)	5.9632 5.972(*)	5.97 (0.11%)	5.97 (0.11%)	6.08 (1.96%)	6.04 (1.29%)	6.06 (1.62%)
и	0.0651 (0.61%)	0.0655	0.0672 (2.60%)	0.06939 (5.94%)	0.07 (6.87%)	0.0691 (5.50%)	0.0070 (6.87%)
ν	0.1931 (0.87%)	0.1948	0.1964 (0.82%)	0.1977 (1.49%)	0.19 (2.46%)	0.1961 (0.67%)	0.207 (6.26%)

a pair of hafnon samples with a thickness of 6 mm and diameter 20 mm from 30 to 300 °C in a box furnace CARBOLITE GERO LHTG 30 – 3000 °C. The hot disk uses the transient plane source (TPS) method [42,43] to determine thermal conductivity. Two different sensors were used; one with a kapton layer and one with a mica layer over the nickel sensor. Prior to measurements, both sensors were used to measure a stainless steel standard (13.8  $\pm$  0.5 W/m-K) compared to literature values of approximately 14  $\pm$  0.7 W/m-K [44].

A laser flash technique was also used to determine the thermal diffusivity from which the thermal conductivity could be deduced. For the thermal diffusivity measurement conducted using a laser flash apparatus (467 HyperFlash, NETZSCH, Burlington, MA, USA), a 10 mm  $\times$  10 mm  $\times$  3.5 mm size sample was cut. The thermal conductivity  $\kappa$  was then obtained from  $\kappa=\rho c_p \alpha$  where  $\rho=6.97~g/cm^3$  is the theoretical density and  $c_p$  is the specific heat, which is also temperature dependent.

The elastic modulus and hardness of the hafnon were measured with a nanoindenter (MTS XP, MTS Systems, Eden Prairie, MN, USA) using standard continuous stiffness measurement (CSM) procedures from the literature [45]. Prior to measurements on hafnon, the modulus and hardness of a silica standard were measured and compared with literature values (values in brackets). These tests gave a modulus of  $72 \pm 2$  GPa  $(73.8 \pm 0.3 \text{ GPa } [46])$  and hardness of  $9.7 \pm 0.4$  GPa  $(8.85 \pm 0.05 \text{ GPa } [47])$ .

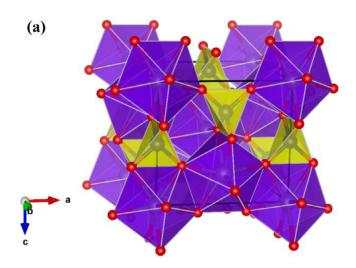
## 3. Results and discussion

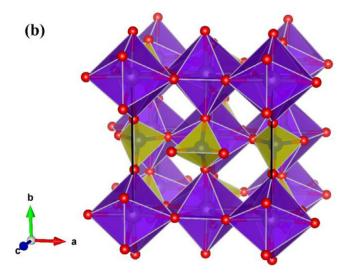
## 3.1. The lattice structure

Our XRD measurements revealed that the hafnon samples have a body-centered tetragonal (zircon-like) structure with a space group of I4<sub>1</sub>/amd (No. 141). The conventional (tetragonal) unit cell consists of four formula units as shown in Fig. 2. Highly symmetric hafnium, silicon and oxygen atomic coordinates in units of lattice parameters a and c are (0, 3/4, 1/8), (0, 1/4, 3/8) and (0, u, v), respectively, where u and v are oxygen reduced coordinates given in Table 1. As shown in Fig. 2, hafnium atoms are at the center of decahedra (purple), silicon atoms are at the center of tetrahedra (yellow), and oxygen atoms at the corners are in red. Each tetrahedron shares two edges with adjacent decahedra. The lattice constants are the same along the a- and b- axes, which are slightly larger than that along the c-axis. Our optimized lattice constants are summarized in Table 1 and compared with experiments [28] and other calculations [23-27]. The difference in the lattice parameters predicted by the PBEsol method was within <1% of measurements, while the other simulation methods gave larger relative errors.

## 3.2. Mechanical properties

The tetragonal symmetry of hafnon dictates that there are six independent second-order elastic stiffness constants. Their predicted values, determined by the present study, together with other moduli derived





**Fig. 2.** Lattice structure of  $HfSiO_4$  unit cell. The figures (a) and (b) show views of (a,c) plane and (a,b) plane perspectives respectively. Oxygen atoms are shown in red; hafnium atoms are at the center of purple decahedra; silicon atoms are at the center of yellow tetrahedra. The decahedra and tetrahedra are edge-sharing. Each hafnium atom is connected to eight oxygen atoms, while every silicon atom has four oxygen neighbors. The primitive cell of  $HfSiO_4$  has 12 atoms, while the conventional tetragonal cell has 24.

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Table 2
Voigt-Reuss-Hill bulk modulus, shear modulus, and Young's modulus in GPa, and Poisson's ratio. Relative errors of Hill Young's modulus are in parentheses compared to the experimental value from nanoindentation.

	PBEsol (present work)	LDA [26] (CASTEP)	GGA [25] (CASTEP)	Empirical potential [24]	GGA [27] (WIEN2k)
$c_{11} = c_{22}$	430	484	604.8	441	_
c <sub>12</sub>	70	66	125.3	77	=
$c_{13} = c_{23}$	151	160	217.7	192	=
c <sub>33</sub>	487	520	575.8	537	_
$c_{44} = c_{55}$	110	106	103.2	107	_
c <sub>66</sub>	50	43	32	41	-
Voigt bulk modulus	233	-	323	260	236.72
Voigt shear modulus	119	-	129.3	_	_
Voigt Young modulus	306	_	342.2	_	=
Voigt Poisson ratio	0.28	_	0.323	_	=
Reuss bulk modulus	228	-	322.1	_	_
Reuss shear modulus	98.6	-	82.3	_	_
Reuss Young modulus	258	-	227.5	_	_
Reuss Poisson ratio	0.31	-	0.382	_	_
Hill bulk Modulus	230	249	322.5	_	_
Hill shear modulus	109	109	105.8	_	_
Hill Young's modulus	282 (5.0%)	285 (4.0%)	286.1 (3.7%)	_	=
Hill Poisson's ratio	0.30	0.31	0.352	_	

from them, are compared with those obtained by various other methods in Table 2. The substantial differences in the elastic constants obtained by the different first-principles calculations are a result of the use of different exchange-correlation functionals. With the exception of c<sub>13</sub> and c<sub>33</sub>, the PBEsol method used here gives elastic constants that are quite close to those predicted using LDA, while the GGA method predicts larger values. Under the Voigt-Reuss-Hill approximation, the Voigt bulk modulus and the Voigt shear modulus predicted by GGA have a larger magnitude than those calculated from PBEsol, which is similar to the elastic constant coefficients. However, the Hill shear modulus predicted by the PBEsol, LDA and GGA methods are very similar. The Hill Young's modulus and Poisson's ratio obtained by PBEsol, LDA, and GGA are all within 5% of the experimental values. The reason for this good agreement for Young's modulus obtained by the three methods is that for hafnon, the calculated Hill shear modulus is much smaller than the Hill bulk modulus, and this mainly determines the magnitude of the Hill Young's modulus. The nanoindentation measurements yielded an averaged Young's elastic modulus of 297 ± 3% GPa. Its measured hardness (not calculated here) was  $19.2 \pm 0.8$  GPa.

# 3.3. Phonon dispersion and Gruneisen parameters

The phonon dispersion curves of hafnon within the Brillouin zone (BZ) of the primitive cell are displayed in Fig. 3(a). Phonon frequencies determined by PBEsol (red curves) agree well with experimental data obtained by Raman spectroscopic techniques [18–20] and with results obtained from other first-principles calculations [23]. The MD results obtained using an empirical potential [24] differ slightly from our calculation along the  $\Gamma$ – Z direction. The Born charge correction yields the LO-TO mode splitting and results in the frequency of 32.8 THz at the  $\Gamma$  point that is also predicted by the first-principles and the empirical MD calculations.

The phonon dispersion describes the harmonic properties of the hafnon crystal. In order to evaluate its anharmonicity, Gruneisen parameters that define the change in phonon frequency with change in unit cell volume were calculated. Fig. 3(b) shows our calculated mode-Gruneisen parameters for hafnon using the ALAMODE and ShengBTE packages. The three groups of Gruneisen parameters match well, especially in the high frequency region. The difference near 5 THz may come from supercell size and cubic FCs fitting. For simplicity, we used  $1\times1\times1$  conventional cells for ShengBTE, and  $2\times2\times2$  supercells for ALAMODE calculations.

Table 3 The compliances in  $10^{-4}$ /GPa under 0 K, 600 K and 1200 K, calculated within the QHA.

	S <sub>11</sub>	S <sub>12</sub>	S <sub>13</sub>	S <sub>33</sub>
0K	26.05	-1.6	-7.57	25.2
600K	27.65	-1.51	-8.18	26.43
1200K	29.19	-1.39	-8.78	27.6

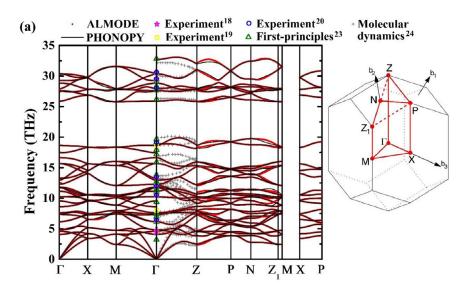
### 3.4. Coefficients of thermal expansion

The measured and calculated temperature dependence of linear CTE are summarized in Fig. 4. The XRD and the dilatometry measurements provide the linear CTE (along the a- and c-axes), and the volumetric CTE, respectively, which we compare with our first-principles results. We also include results predicted by the FP-LAPW method[28]. The simulation and the experimental results share the same temperature dependence and have similar orders of magnitude. Our first-principles calculations presented in this work yield closer values to the experiments. The linear CTE of hafnon is calculated using the average Gruneisen parameters, the compliance matrices and the volumetric CTE. The linear CTE along the c-axis is larger, which is consistent with the experiments, despite the difference in the high temperature region. In order to reduce this difference, we consider temperature effects on the compliance matrices. We keep the equilibrium volumes under high temperatures predicted by the QHA and adopt the ElaStic Code again to calculate the corrected compliances needed in the formula (3) that are listed in Table 3. The black squares and the round dots in Fig. 4 are the corrected linear CTE in which the temperature dependence of the compliance tensor has been taken into account within the QHA. The temperature correction to the CTE is minor, the results are however closer to the experiments.

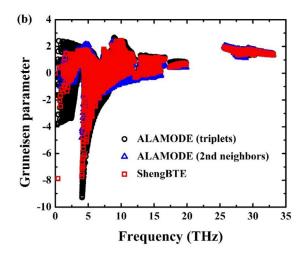
Table 4 shows our calculated, XRD and dilatometer measured CTE's and compares them with results from other groups. We believe that the dilatometer-measured negative CTE of  $-1.8 \times 10^{-6}$  °C  $^{-1}$  from 300 K to 1073 K) in Ref. [49] could be due to the porosity of their samples. Other experiments [21,22] and simulations [26] have found the linear CTE of hafnon to lie in the range of 3.6 - 4.4 ×  $10^{-6}$  K  $^{-1}$  for temperatures between 300 K and 1473K These temperature-averaged values are consistent with our calculated and measured linear CTEs. For hafnon to be used as an EBC material, CTE should match that of Si bond coats and the SiC composites they protect. Since the linear CTE of Si is 3.5 –  $4.5 \times 10^{-6}$  K  $^{-1}$  [50] and that of SiC/SiC melt infiltrated CMCs is

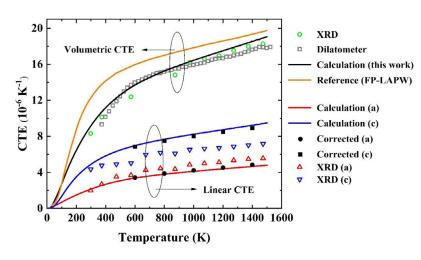
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**Fig. 3.** (a) Phonon dispersion versus wavevector of hafnon along high-symmetry directions in the first Brillouin zone of the primitive cell [48] shown on the right.  $b_1$ ,  $b_2$  and  $b_3$  are reciprocal lattice vectors of the primitive cell. (b) Mode Gruneisen parameters calculated by the cubic FCs approximation using ALAMODE and ShengBTE. Nearest neighbors considered: the second nearest neighbors (2nd neighbors and ShengBTE) and all the triplets connected by bonds (triplets). Harmonic FCs are the same in the three groups.

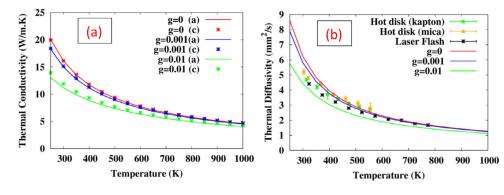




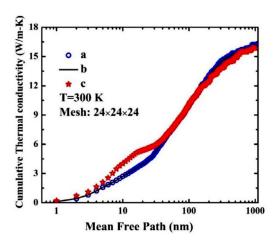
**Fig. 4.** The temperature dependence of the linear and volumetric CTEs of hafnon reported in this work. The corrected data (black circles and squares) include the temperature dependence of the compliance tensor, while the "calculation" (solid lines) used a constant value for it.

Table 4 Averaged linear CTE from calculations and experiments (Unit:  $10^{-6} K^{-1}$ ). The chemical bond theory (CBT) result is displayed in the last column.

Temperature (°C)       27 - 1227       25 - 1200       100 - 1250       25 - 1300       25 - 800       30 - 800       -         CTE       3.06 - 6.36       2.77 - 6.09       3.11 - 5.97       3.6       4.17       -1.8       4.41		Present calculation	Present XRD	Present Dilatometry	XRD [21,22]	XRD [49]	Dilatometry [49]	CBT [26]
	1 ,							- 4.41



**Fig. 5.** (a) Thermal conductivity (left) along a and c axes. The difference between a and c directions becomes more visible for g=0.01. (b) Isotropic thermal diffusivity (right) of hafnon from anharmonic calculations, laser flash and hot disk measurements. Kapton and Mica sensors distinguish the two hot disk measurements. Effect of impurity scattering (Tamura model) with parameters g=0.001 and 0.01 are also plotted.



**Fig. 6.** Cumulative thermal conductivity along a, b, and c axes versus mean free path of phonons, at 300 K. Saturation is reached at 1  $\mu$ m, meaning carrier MFPs essentially range from 1 nm to 1  $\mu$ m.

 $4.5-5.5\times10^{-6}$  K  $^{-1}$  [51], hafnon has a very good thermal expansion match with silicon EBC bond coats and the CMC substrates to which they are applied.

## 3.6. Thermal transport properties

Fig. 5 shows the thermal diffusivity and the thermal conductivity of hafnon calculated *via* the relaxation time approximation and measured by hot disk and laser flash methods. To calculate the thermal diffusivity, we used the specific heat and density from the QHA, as well as the thermal conductivity from the solution of the Boltzmann Transport Equation (BTE). To obtain converged thermal conductivity results, three meshes  $16 \times 16 \times 16$ ,  $20 \times 20 \times 20$  and  $24 \times 24 \times 24$  were used for sampling the first Brillouin zone. At each temperature, the reported thermal conductivity,  $\kappa$  was obtained by extrapolating the results from the three mesh values to infinite mesh. Since hafnon is a tetragonal crystal, the thermal conductivity along the a- and b-axes is the same, consistent with the cumulative thermal conductivity also shown in Fig. 6.

As seen in Fig. 5(b), the hot disk technique yields slightly larger thermal diffusivity than the laser flash approach. The difference between the experiments is negligible within the error bars. The thermal diffusivity was converted to thermal conductivity, using the theoretical specific heat obtained from the QHA. In the high-temperature region,  $\kappa$  was proportional to the inverse temperature, consistent with three-phonon scattering. Using laser flash and the hot disk method, the thermal conductivity of hafnon was 13.3 W/m.K at 303 K (30 °C) and decreased to 6.25 W/m.K at 773 K (500 °C). Experimental results by laser flash above 600 K show a similar trend and agree well with the calculation. Previous measurements of Varghese et al. yielded lower values of 11 W/mK at room temperature, probably reflecting the lower purity of their sam-

ples. From room temperature to 500 K, the laser flash values and the hot disk results are in good agreement, both slightly deviating from the power law of KT<sup>-1</sup>. The slight porosity of the hafnon sample leads to a lower density compared to the theory. We therefore compare the thermal diffusivities between theory and experiment, since it is the latter that is directly measured.

In the lower temperature region, the effect of the defect-phonon scattering becomes more important. As we found experimental evidence for a 6-8% volume fraction of hafnia and a 2.4% volume fraction of air in the samples, we assume that such impurities contribute to a lowering of the thermal conductivity. To take this into account, we first compare the size of the pores and hafnia grains, which can be inferred from Fig. 1(b) to be on the order of a micron, to the contribution of different mean free path modes displayed in Fig. 6. It can be seen from the latter figure that a majority of heat conducting modes have mean free paths less than a micron, implying heat carrying phonon wavelengths are also of submicron size. As a result, given the larger size of the microparticles (hafnia and air pockets), it seems reasonable to adopt an effective medium view and model the thermal conductivity of the samples as a weighted average of those of air, hafnia and hafnon with respective weights of 2.4%,7% and 90.6%. This results in an average room-temperature thermal conductivity of  $\kappa_{avg} = 0.024 \times 0.025 + 0.07 \times 1.1 + 0.906 \times 16.12 = 14.68 \frac{W}{mK}$ . When comparing to experiments, we have used the iosotropic avergage  $\kappa_{isotropic} = (2\kappa_a + \kappa_c)/3$ . If, on the other hand, we adopt the impurity scattering approach of Tamura [52], which is essentially the crystal extension of the Rayleigh scattering of phonons off point impurities, to model the scattering of phonons of hafnon with residual hafnia "particles", we have to define a "scattering parameter" g through  $g = \sum_{i} f_{i} (1 - \frac{m_{i}}{\pi})^{2}$ where  $\bar{m}$  is the average mass, and  $m_i$  is the mass of species i of concentration  $f_i$ . We assume two species, hafnon of concentration  $f_1 = 92.8\%$ and hafnia of concentration  $f_2$  =7.2%, and take the deviation in the density instead of that of mass:  $(1 - \frac{\rho_i}{\bar{\rho}})^2$  as the perturbation parameter, leading to  $g \approx 0.01$ . This scattering process is then added, without any fitting parameter, to the three-phonon scattering rates in order to calculate the total thermal conductivity. The approximation in this model is that impurities are considered as point particles, smaller than all phonon wavelengths. Impurity dimensions do not appear in the model. This may be questionable as impurity grains are of micron size (see Fig. 1) and not negligible compared to many of the phonon wavelengths. The reduction of  $\kappa$  due to this additional scattering is displayed in Fig. 5. While the impurity scattering model leads to a room-temperature value of 11.4 W/m.K, which is 27% lower than the thermal conductivity of pure hafnon, the effective medium model leads to only a lowering of 9%. We believe the Rayleigh scattering approach adopted above may not be a very realistic approach, as the grain sizes are relatively large and cannot be neglected compared to phonon wavelengths. Thermal diffusivity data of the laser flash method are in good agreement with theory especially at high temperatures where hot disk measurements fail. At very low temperatures where long mean free path and long wavelength phonons carry most of the heat, the scattering approach of Tamura becomes more accurate than the effective medium model.

#### 4. Conclusions

Due to its possible applications as radioactive materials storage, EBCs in the aerospace industry, and high-K dielectric in microelectronic industries, we undertook a comprehensive study of the physical, mechanical, and thermal transport properties of hafnon using both firstprinciples calculations and experiments. The first-principles methods were able to reliably predict crystal structure/lattice parameters, elastic constants, linear CTE and the thermal conductivity of hafnon. Amongst the first-principles methods, PBEsol most accurately predicted the lattice parameters (to within 1%). The hafnon elastic constants were also well predicted by this method. The Hill Young modulus was within 5% of the experimental value obtained using a nanoindentation technique. The predicted linear CTE agreed well with both hot stage XRD lattice parameter and pushrod dilatometer measurements. The CTE of hafnon was found to be close to that of silicon. This makes it an attractive material for EBC applications. The predicted temperature-dependent thermal diffusivity and thermal conductivity from the effective medium theory were found to be in better agreement with experimental values obtained using hot disk and laser flash methods, when compared to the Rayleigh scattering model of Tamura. It was shown that a concentration of hafnia as small as 7% can contribute to a lowering of room-temperature thermal conductivity by 9%. The solution of Boltzmann equation revealed that heat carriers have a broad spectrum of mean free paths ranging from 1 nm to 1 µm. Grains or domains of typical size 10 nm can therefore be very effective in strongly reducing the thermal conductivity of this material. Such strategies can be used to lower the thermal conductivity of this material. The results of this study can be used to support further exploration of the above-mentioned applications.

#### **Declaration of Competing Interest**

The authors declare no competing interests.

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# Data availability

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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