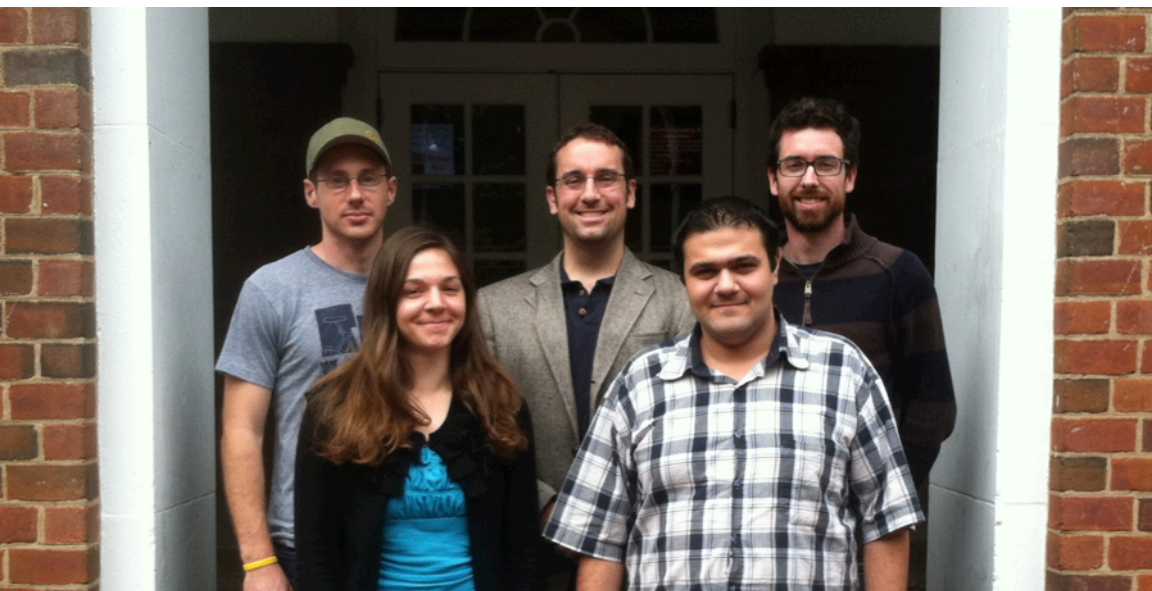




SCHOOL of ENGINEERING & APPLIED SCIENCE  
UNIVERSITY of VIRGINIA



# Energy transfer processes in nanosystems: phonon transport in metals, interfaces, and polymers



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Energy efficiency = heat transfer problem

57% of energy consumed in the United States is wasted as **HEAT**

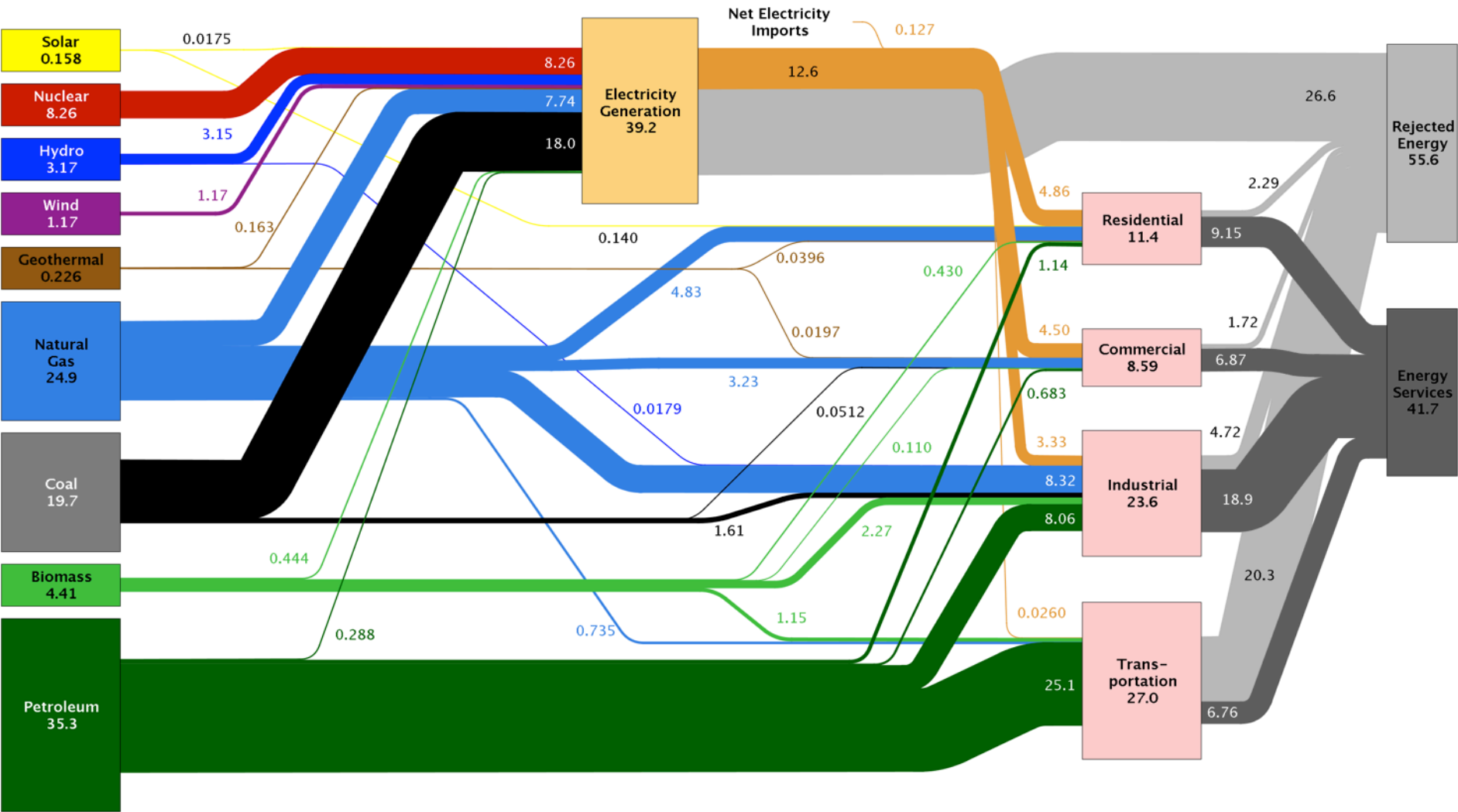


Let's look at a simple graph...

# Energy usage in the United States



Estimated U.S. Energy Use in 2011: ~97.3 Quads



Source: LLNL 2012. Data is based on DOE/EIA-0384(2011), October, 2012. If this information or a reproduction of it is used, credit must be given to the Lawrence Livermore National Laboratory and the Department of Energy, under whose auspices the work was performed. Distributed electricity represents only retail electricity sales and does not include self-generation. EIA reports flows for non-thermal resources (i.e., hydro, wind and solar) in BTU-equivalent values by assuming a typical fossil fuel plant "heat rate." The efficiency of electricity production is calculated as the total retail electricity delivered divided by the primary energy input into electricity generation. End use efficiency is estimated as 80% for the residential, commercial and industrial sectors, and as 25% for the transportation sector. Totals may not equal sum of components due to independent rounding. LLNL-MI-410527

# Making energy usage more efficient?



Lighting has already  
experienced a paradigm  
shift

**The Light Emitting  
Diode (LED)!**





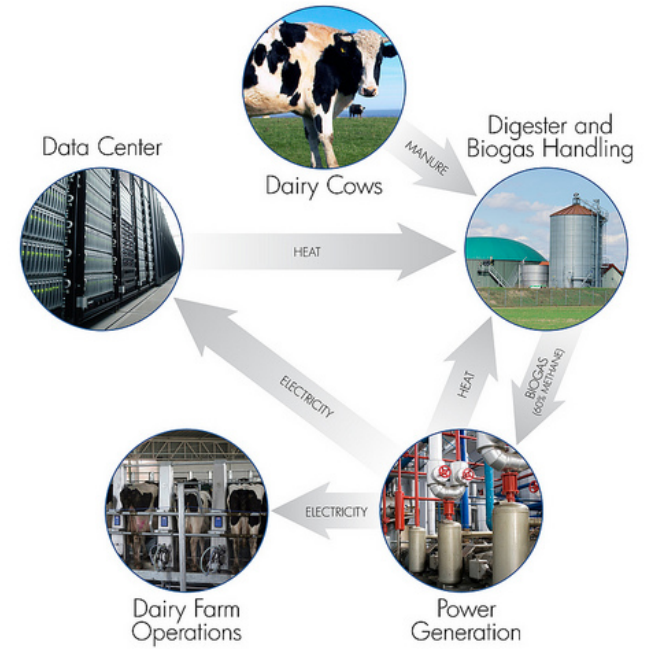
# Making energy usage more efficient?

Server farms...



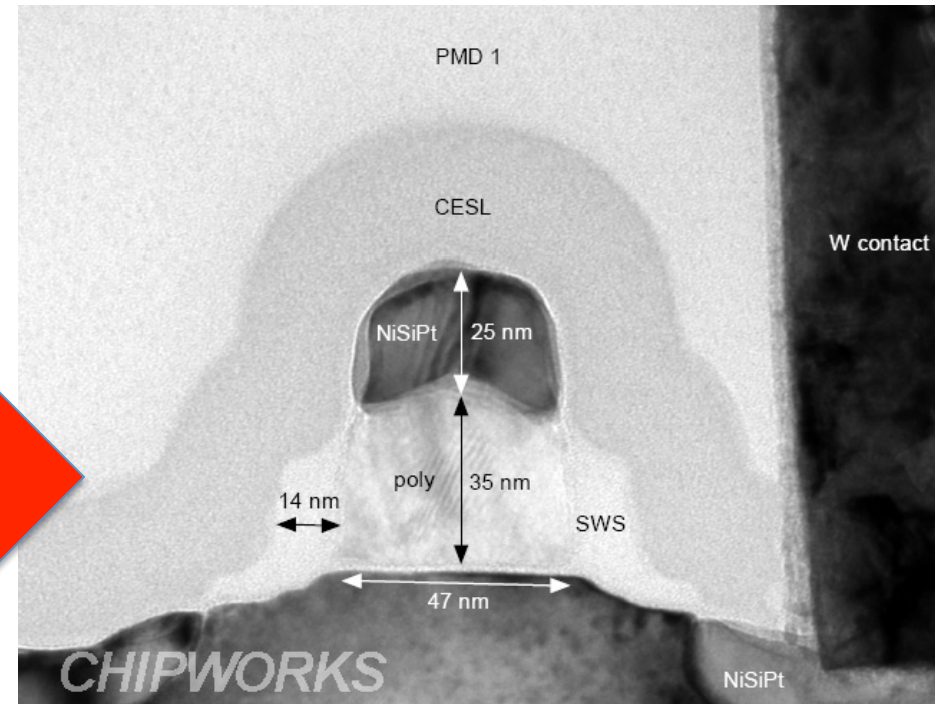
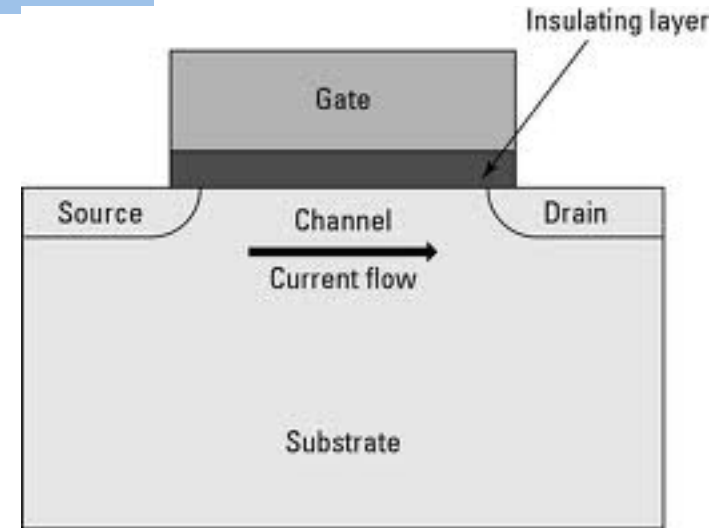
Recycle the wasted heat  
(NET energy decrease)

HP Labs Design for a Farm Waste  
Data Center Ecosystem



Can we make  
computers chips more  
energy efficient?

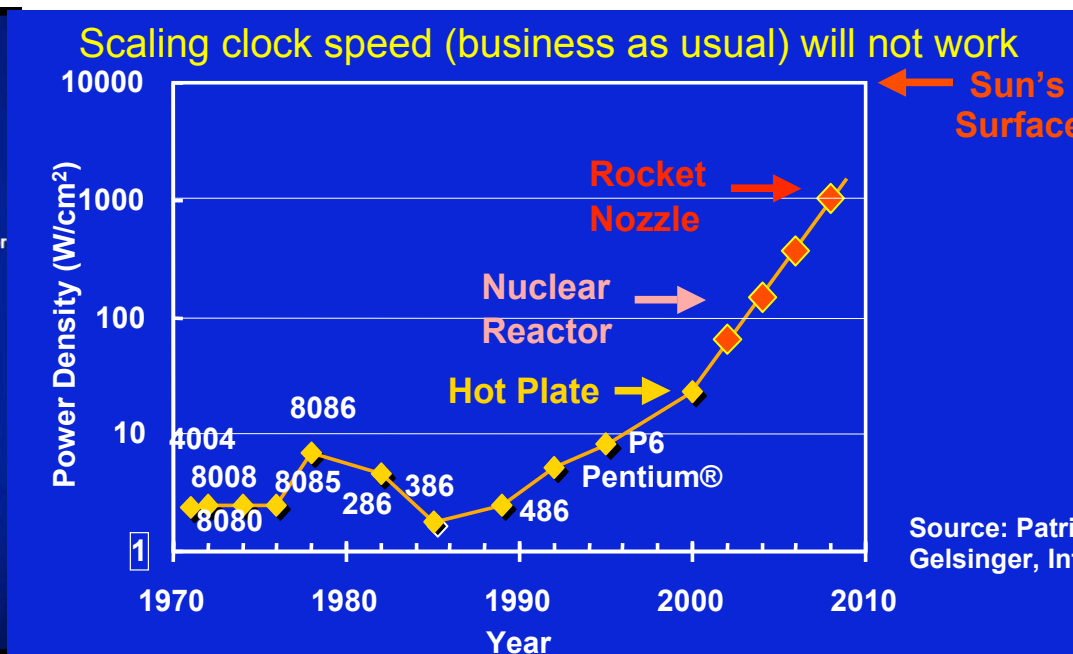
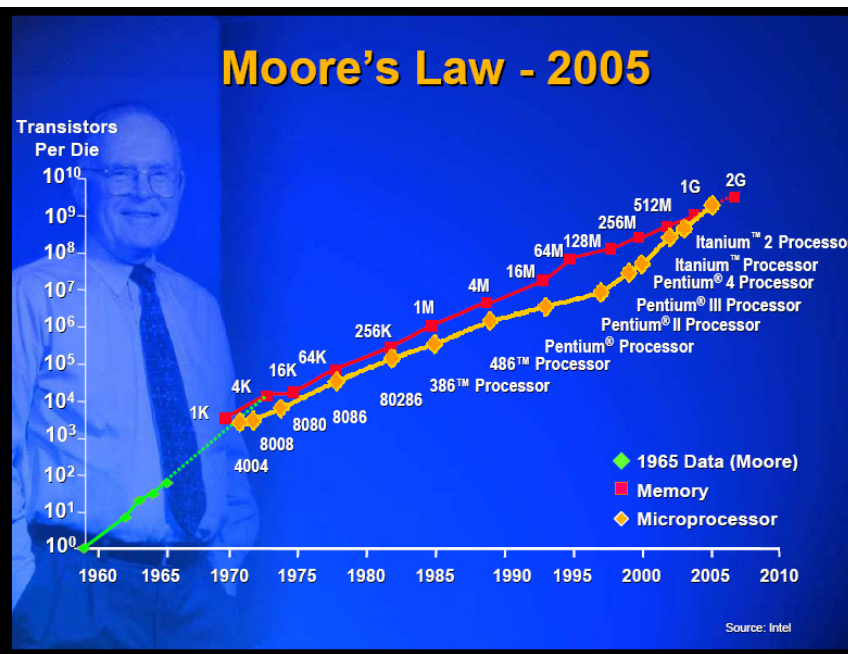
# Making computers more efficient



# Moore's law....a NANO heat transfer problem

$$\text{Power flux} = \text{Power/area}$$

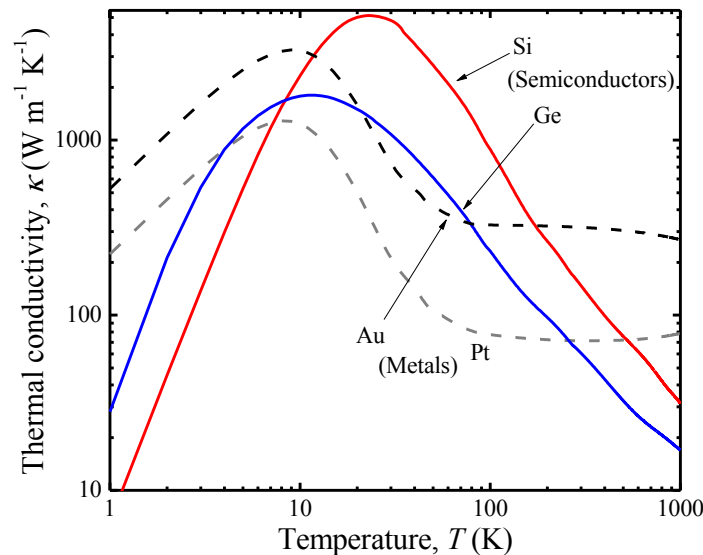
Length scale goes down, power flux goes up as  $L^2$



Moore, "Cramming more components onto integrated circuits," Electronics, **38**, 113 (1965)

# Nanoscale heat transfer

$$q = -\kappa \frac{\partial T}{\partial z}$$

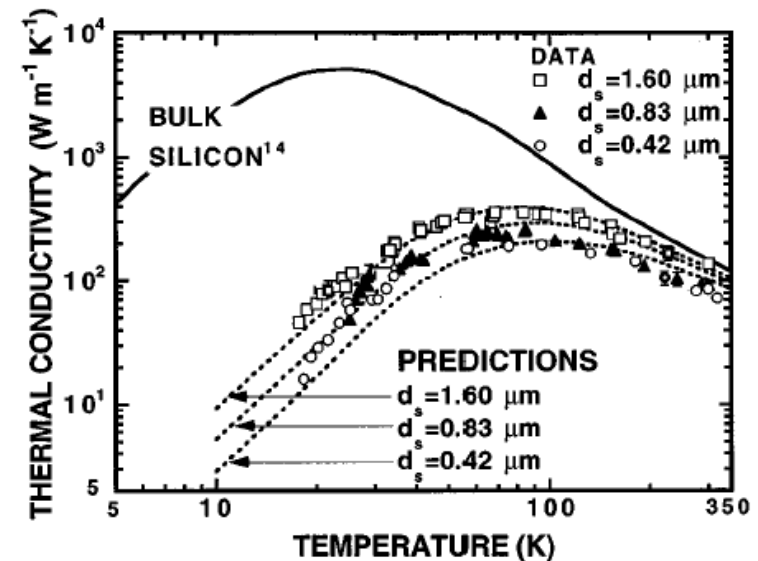


Notice different trends  
between  $\kappa$  in metals and  
 $\kappa$  in semiconductors

Tabulated data from: Ho, Powell, and Liley, "Thermal conductivity of the elements,"  
Journal of Physical and Chemical Reference Data, **1**, 279 (1972).

This doesn't work when  
lengths become too  
short....why??? We'll  
find out soon!

## Silicon thin films



# Definition of nanotechnology

“Nanotechnology is the understanding and control of matter at dimensions of roughly **1 to 100 nanometers**, where unique phenomena enable novel applications. Encompassing nanoscale science, engineering and technology, nanotechnology involves imaging, measuring, modeling, and manipulating matter at this length scale.”

-National Nanotechnology Initiative



# The Scale of Things – Nanometers and More

## Things Natural

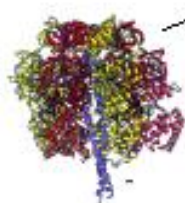
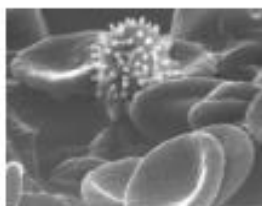


Dust mite  
200  $\mu\text{m}$

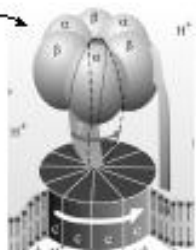


Human hair  
~ 60-120  $\mu\text{m}$  wide

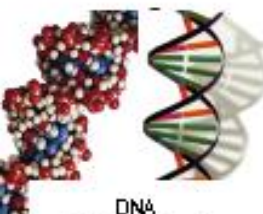
Red blood cells  
with white cell  
~ 2-5  $\mu\text{m}$



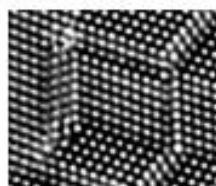
~ 10 nm diameter



ATP synthase



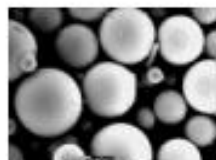
DNA  
~ 2-12 nm diameter



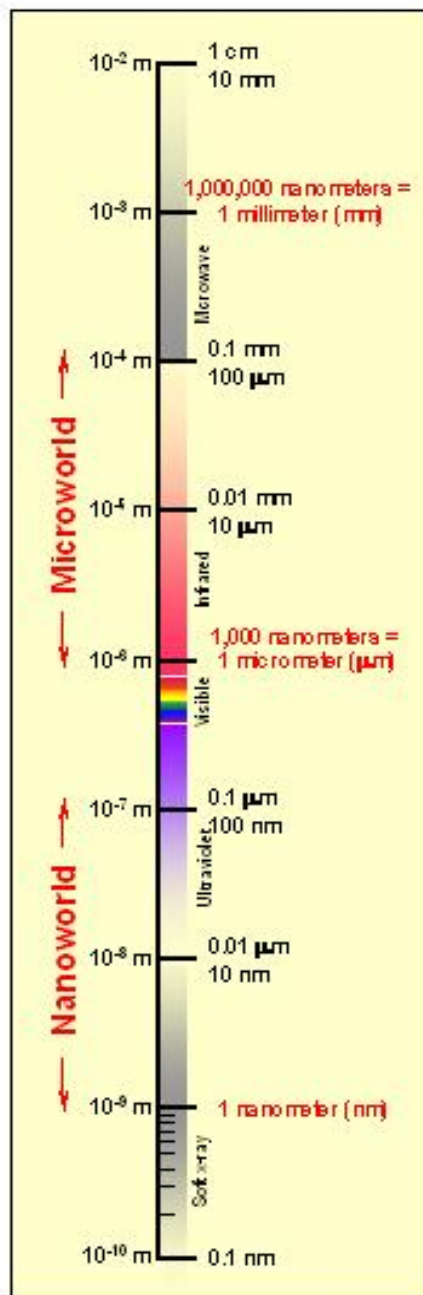
Atoms of silicon  
spacing ~ tenths of nm



Ant  
~ 5 mm



Fly ash  
~ 10-20  $\mu\text{m}$



## Things Manmade



Head of a pin  
1-2 mm

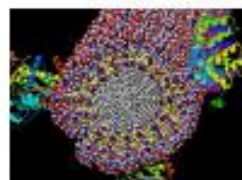
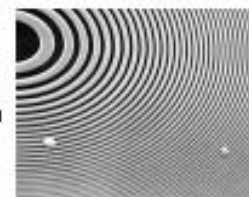


Micro Electro Mechanical (MEMS) devices  
10 - 100  $\mu\text{m}$  wide

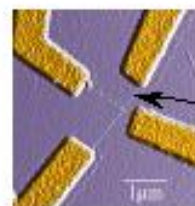


Pollen grain  
Red blood cells

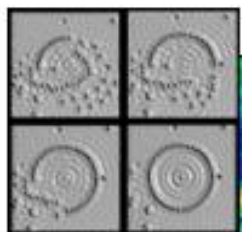
Zone plate x-ray "lens"  
Outer ring spacing ~ 35 nm



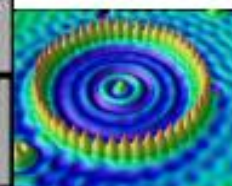
Self-assembled,  
Nature-inspired structure  
Many 10s of nm



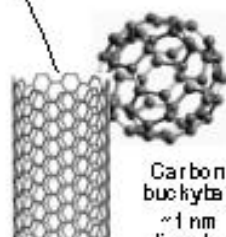
Nanotube electrode



Quantum corral of 48 iron atoms on copper surface  
positioned one at a time with an STM tip  
Corral diameter 14 nm

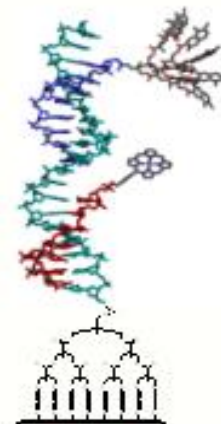


Carbon nanotube  
~ 1.3 nm diameter



Carbon buckyball  
~ 1 nm diameter

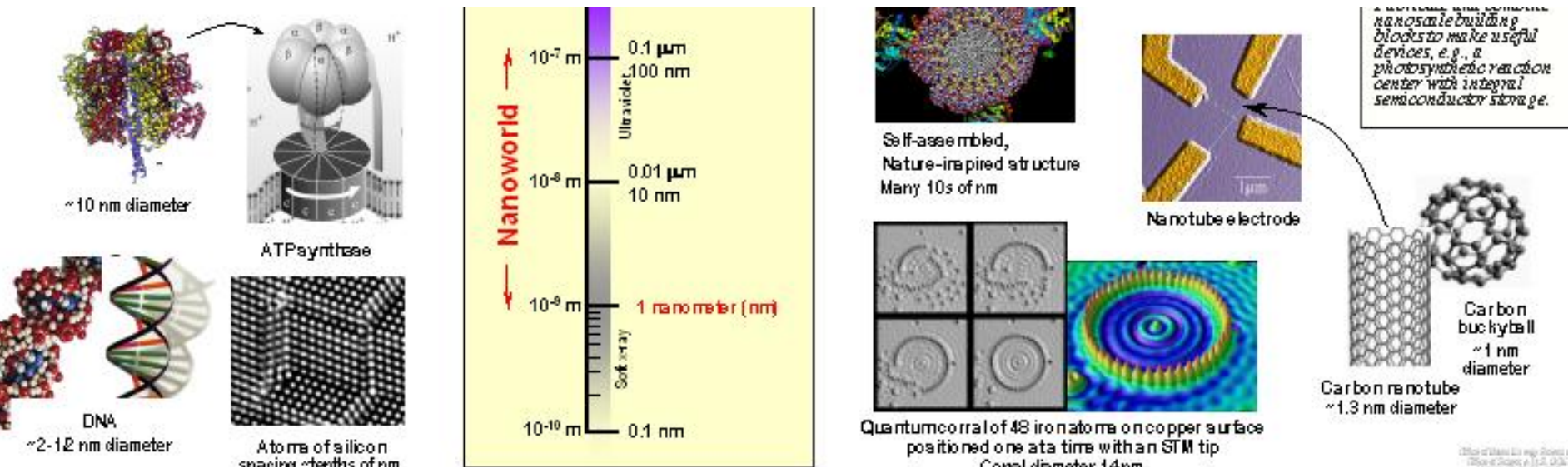
### The Challenge



*Fabricate and combine nanoscale building blocks to make useful devices, e.g., a photosynthetic reaction center with integral semiconductor storage.*

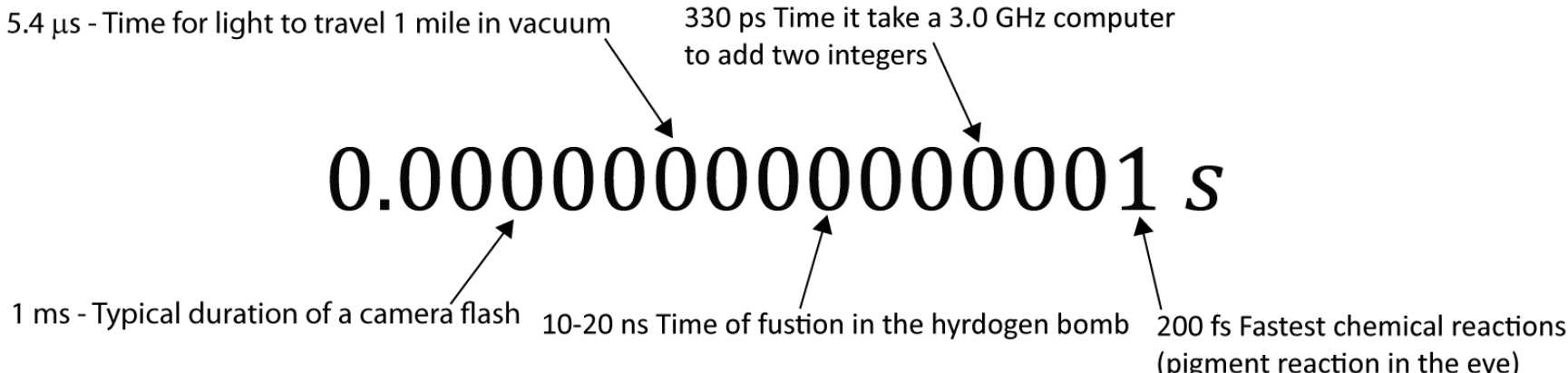


# What does this mean for heat?

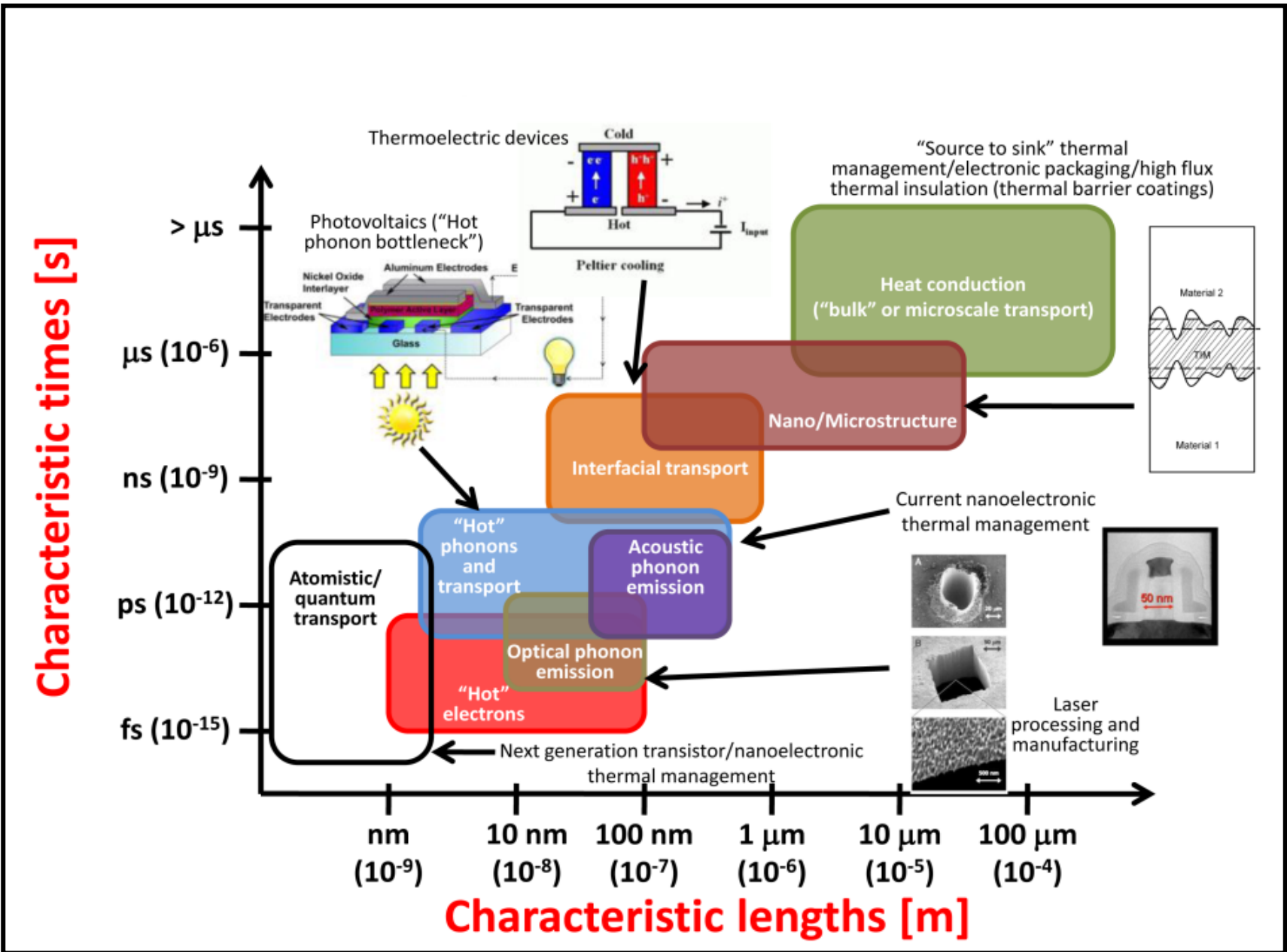


**NEED TO UNDERSTAND HEAT TRANSFER ON THE ATOMIC LEVEL WHERE ALL THE ACTION HAPPENS ON THE ORDER OF FEMTOSECONDS TO NANOSECONDS**

How fast is a femtosecond (10<sup>-15</sup> s)?

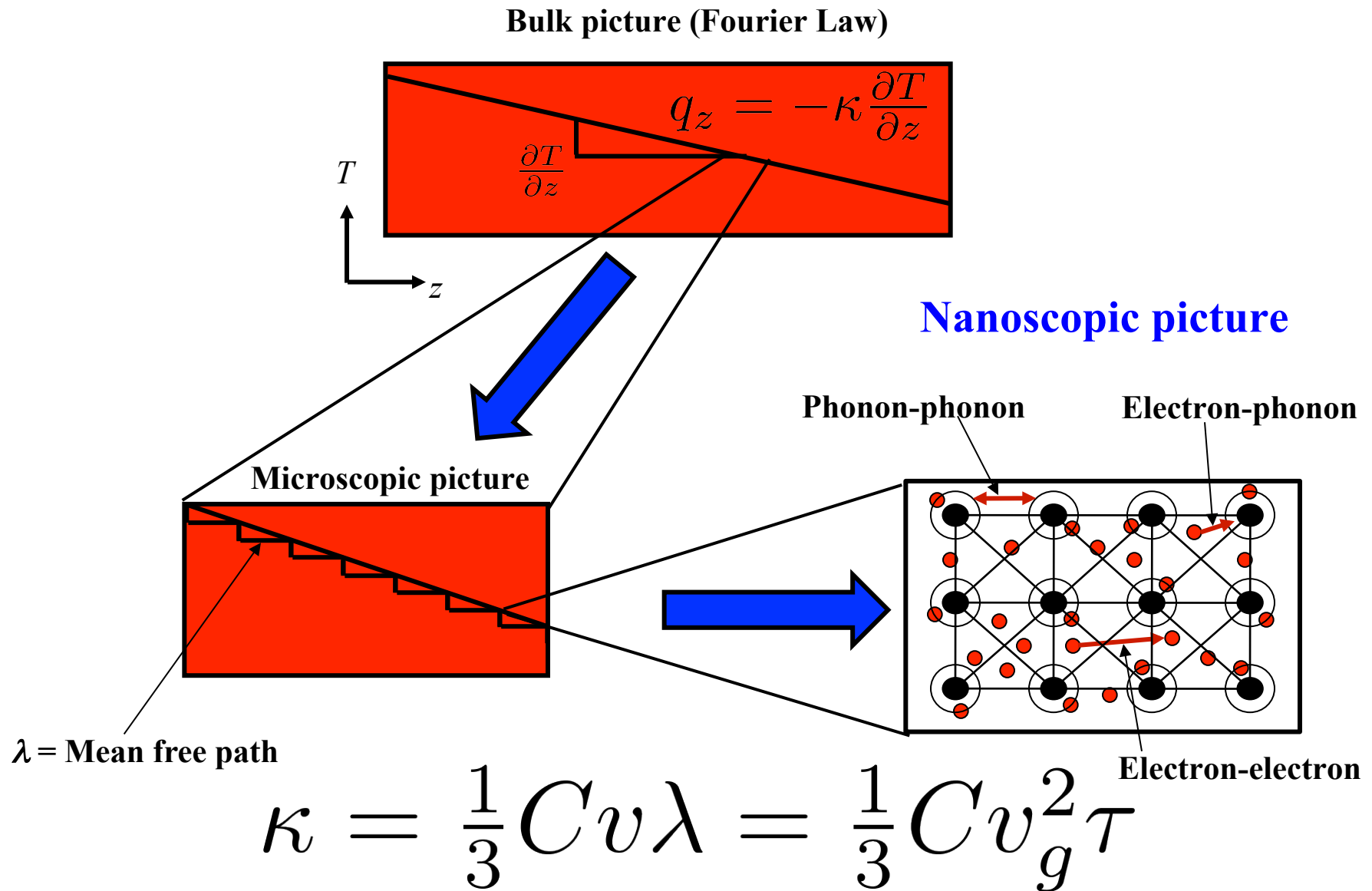


# Energy/heat time and length scales



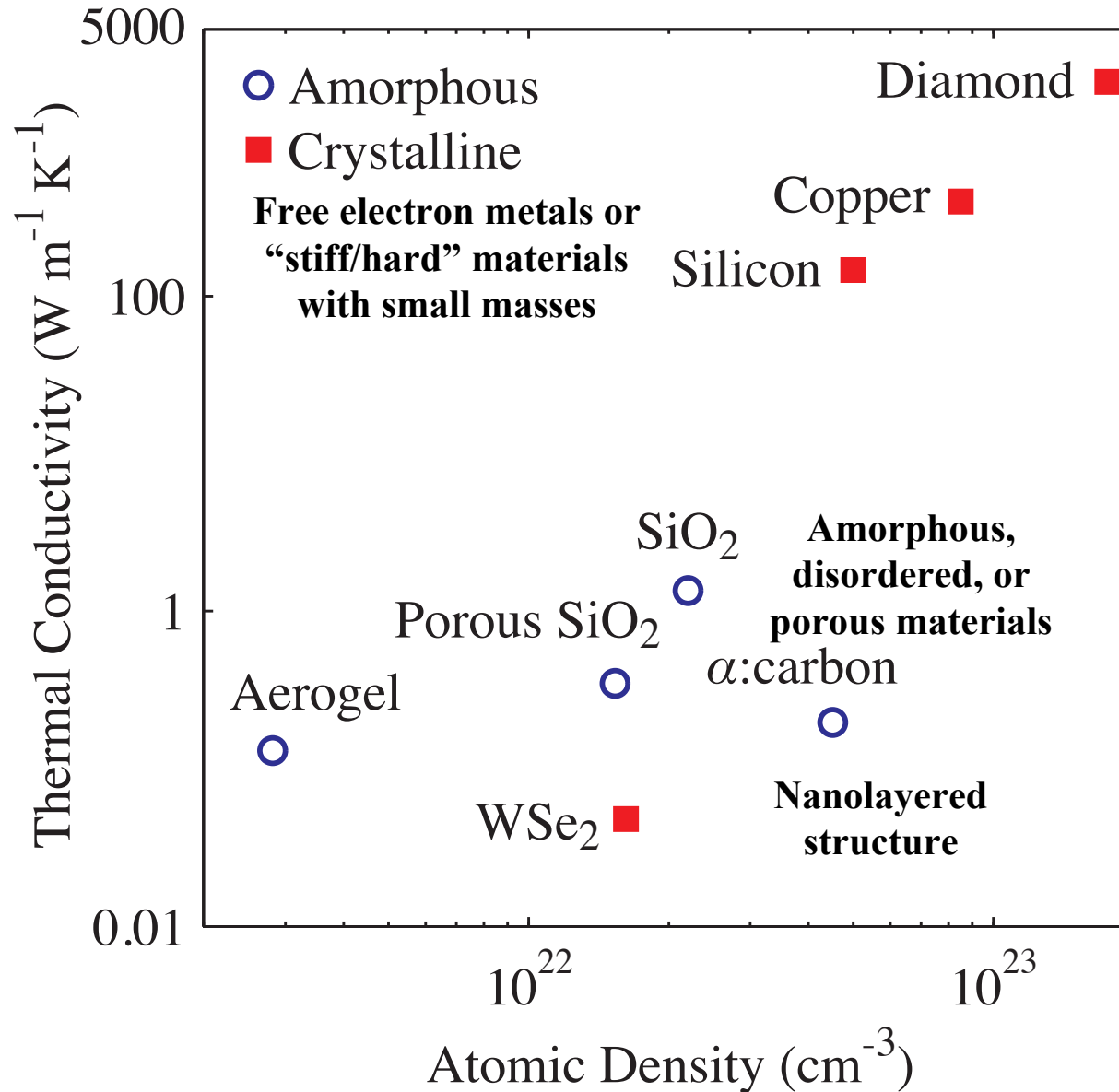
- **Thermophysics background**
- **Measurement of electron and phonon thermal properties on the nanoscale with time domain thermoreflectance – time scales and phenomena**
- **Example 1: Amorphous metals: electron AND phonon transport**
- **Example 2: Interfaces: disorder and adhesion**
- **Example 3: Exceptionally low thermal conductivity of organic semiconducting polymers: making Einstein proud**

# Thermophysics on the nanoscale



# Thermal conductivity of solids

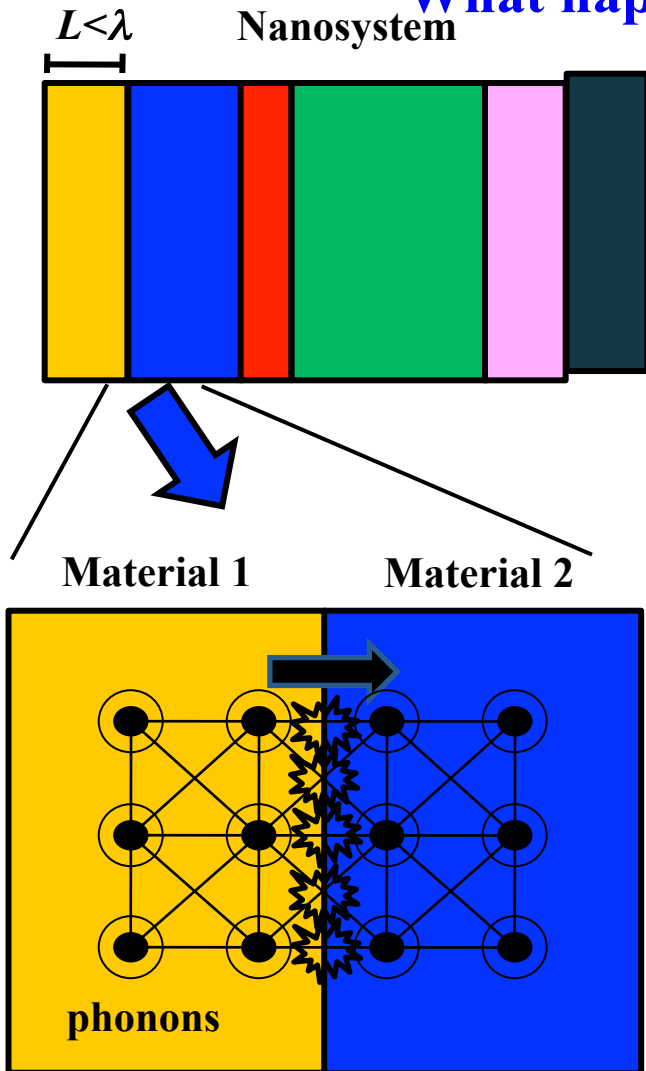
**What's the nanoscopic story here???**



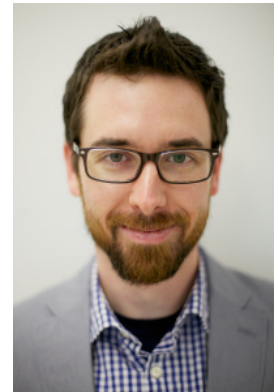
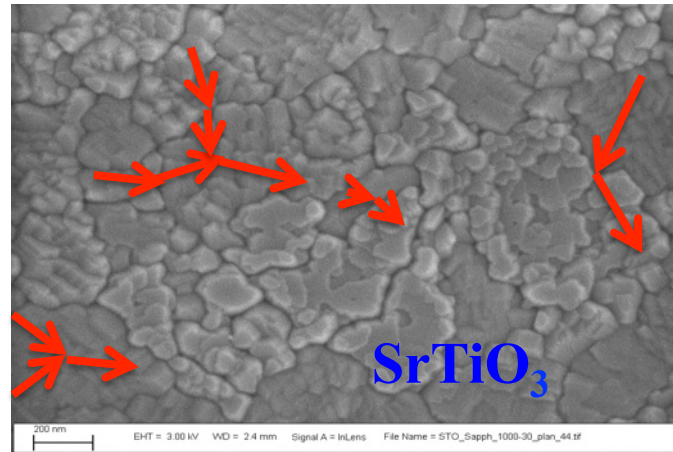
# Thermophysics on the nanoscale

$$\kappa = \frac{1}{3} C v \lambda = \frac{1}{3} C v_g^2 \tau$$

What happens if  $\lambda$  is on the order of  $L$ ?



e.g. Nanoscale composites and thin films



APPLIED PHYSICS LETTERS **101**, 231908 (2012)

## Thermal conductivity of nano-grained $\text{SrTiO}_3$ thin films

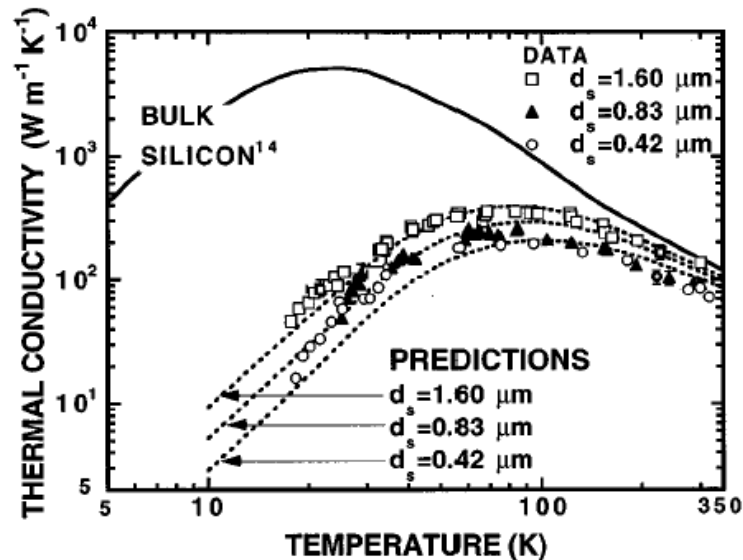
Brian M. Foley,<sup>1</sup> Harlan J. Brown-Shaklee,<sup>2</sup> John C. Duda,<sup>1,2</sup> Ramez Cheaito,<sup>1</sup> Brady J. Gibbons,<sup>3</sup> Doug Medlin,<sup>4</sup> Jon F. Ihlefeld,<sup>2</sup> and Patrick E. Hopkins<sup>1,a)</sup>

<sup>1</sup>Department of Mechanical and Aerospace Engineering, University of Virginia, Charlottesville, Virginia 22904, USA  
<sup>2</sup>Sandia National Laboratories, Albuquerque, New Mexico 87185, USA  
<sup>3</sup>Materials Science, School of Mechanical, Industrial, and Manufacturing Engineering, Oregon State University, Corvallis, Oregon 97331, USA  
<sup>4</sup>Sandia National Laboratories, Livermore, California 94550, USA



# Effects of “nano” on thermal conductivity

## Thermal conductivity of various silicon-based structures v. temperature



How far does energy move before it loses momentum?

$$\kappa = \frac{1}{3} C v \lambda = \frac{1}{3} C v_g^2 \tau$$

How much energy?

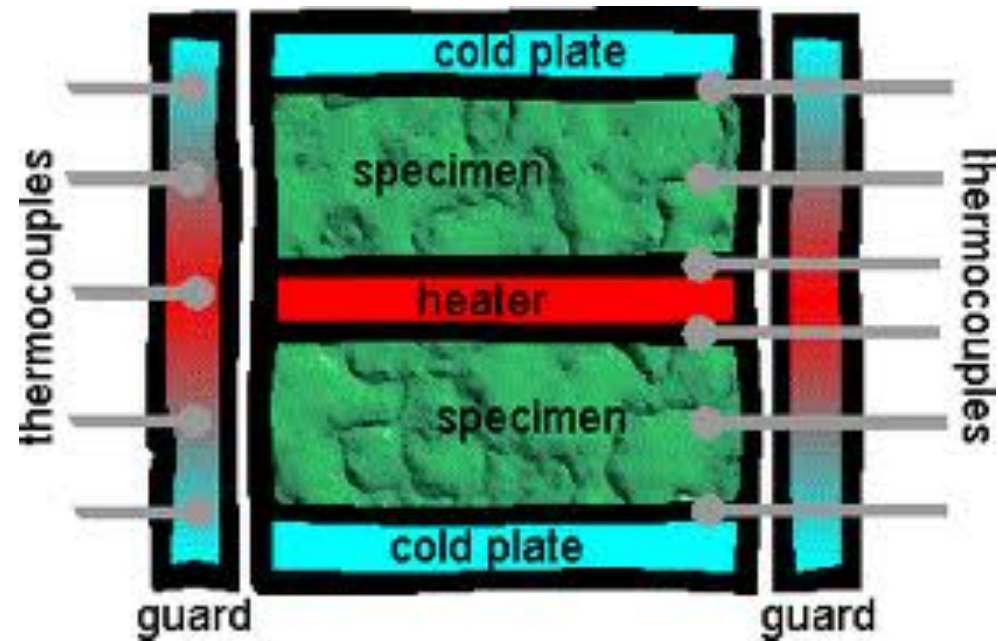
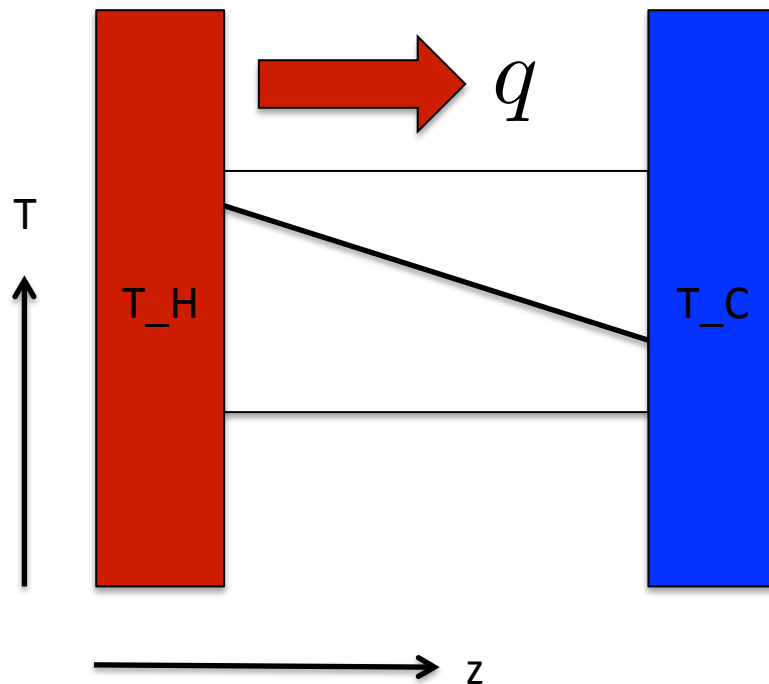
How fast does the energy move?

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# Steady state measurements

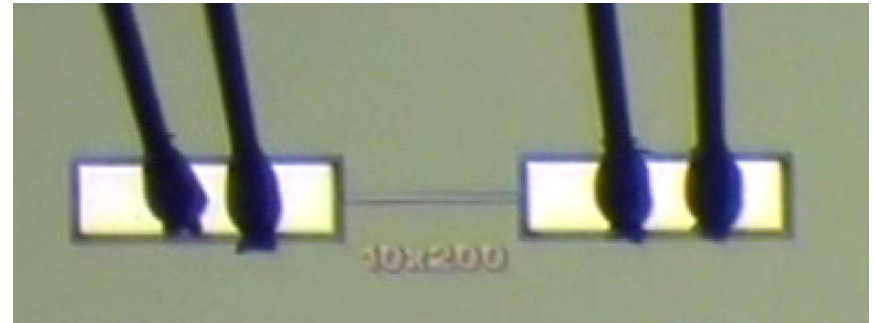
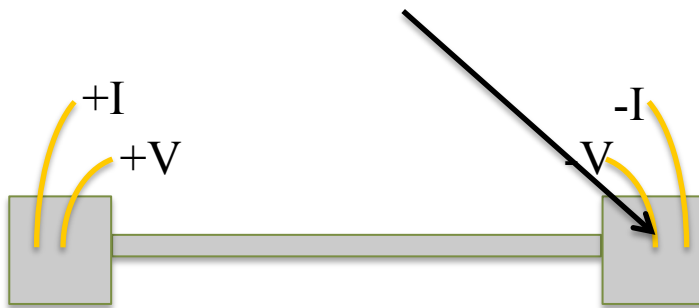
**“Guarded hot plate”**

$$q = -\kappa \frac{\partial T}{\partial z}$$



# Steady state measurements - nano

**Electrical/thermal contact resistances are inherently present in measurements**



**How do you make these contacts in a nanosystem??**

**When would these contact resistances matter in terms of sample geometry???**

P. E. Hopkins and L. M. Phinney. Thermal conductivity measurements on polycrystalline silicon micro-bridges using the 3w technique. Journal of Heat Transfer, 131:043201, 2009.

Transient/frequency domain measurements – more robust

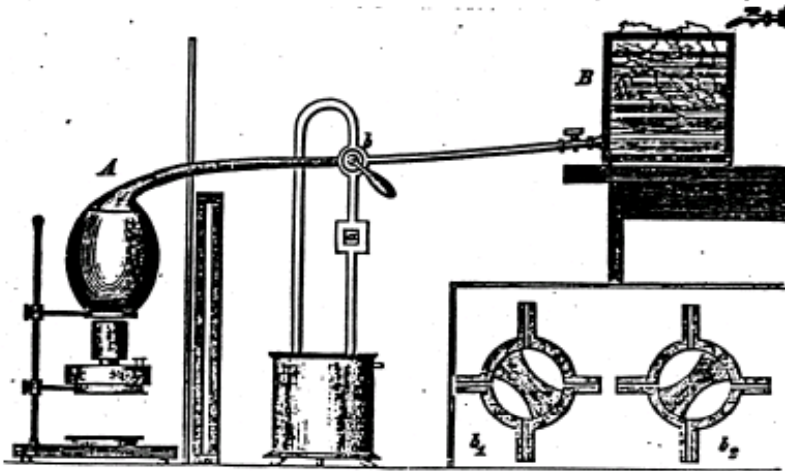
# Angström method

Used fixed temperature  
boundary conditions

$$T(x = 0) = 0^{\circ}\text{C} \quad 0 < t < \Gamma/2$$

$$T(x = 0) = 100^{\circ}\text{C} \quad \Gamma/2 < t < \Gamma$$

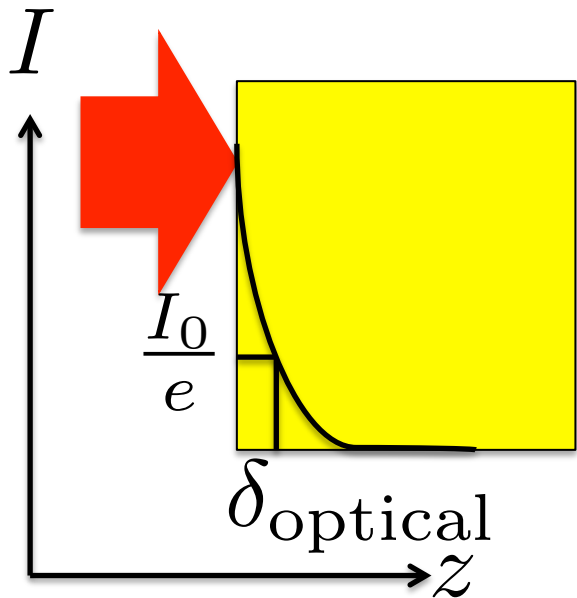
where  $\Gamma$  is the period of temperature oscillations  
produced by alternating flow of ice water and steam



Frequency dependent  
temperature rise leads to  
temperature fluctuation at end  
of sample with some phase lag  
based on RC

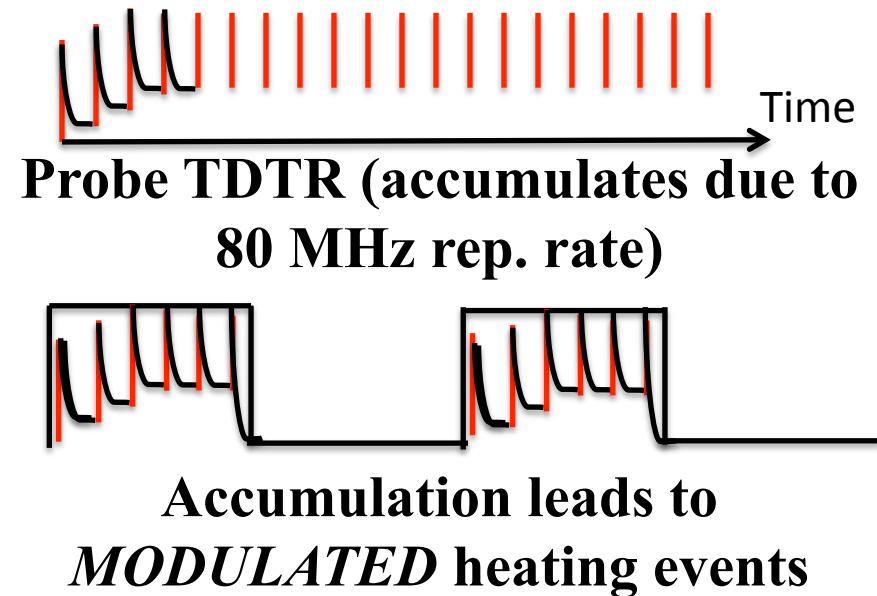
# Can we do this optically???

Coat surfaces with metals to achieve near-surface absorption high *opto-spatial* resolution (i.e., surface localized heat source)



$$\delta_{\text{optical}} = \frac{\lambda}{4\pi k} \approx 10 \text{ nm}$$

Modulated heat transfer regime achieves variable *thermo-spatial* resolution (i.e., variable temperature gradient via distance)



**Pulses on the order of femtoseconds and pulse separation on the order of 12 ns**

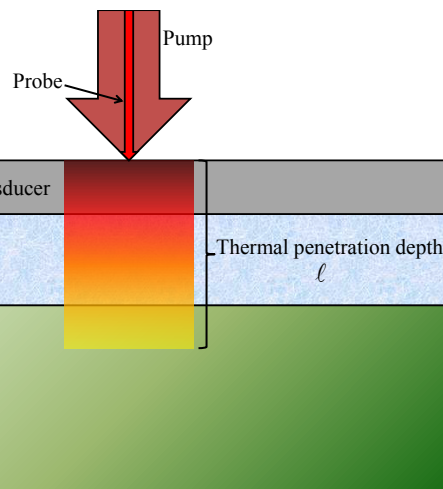
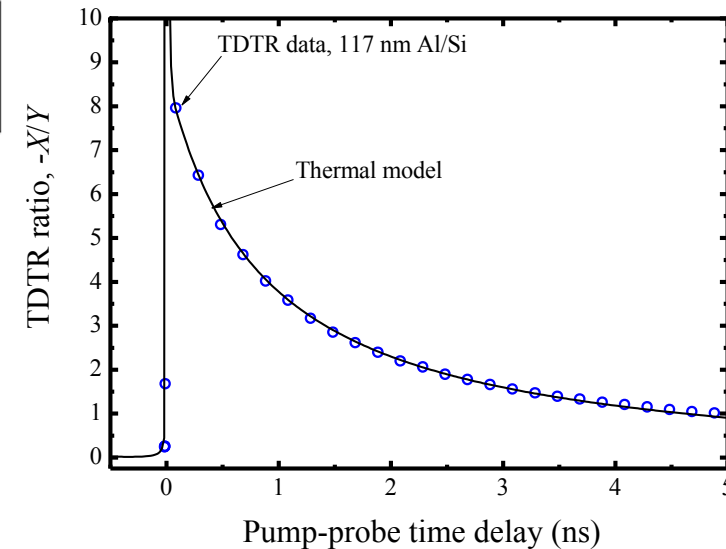
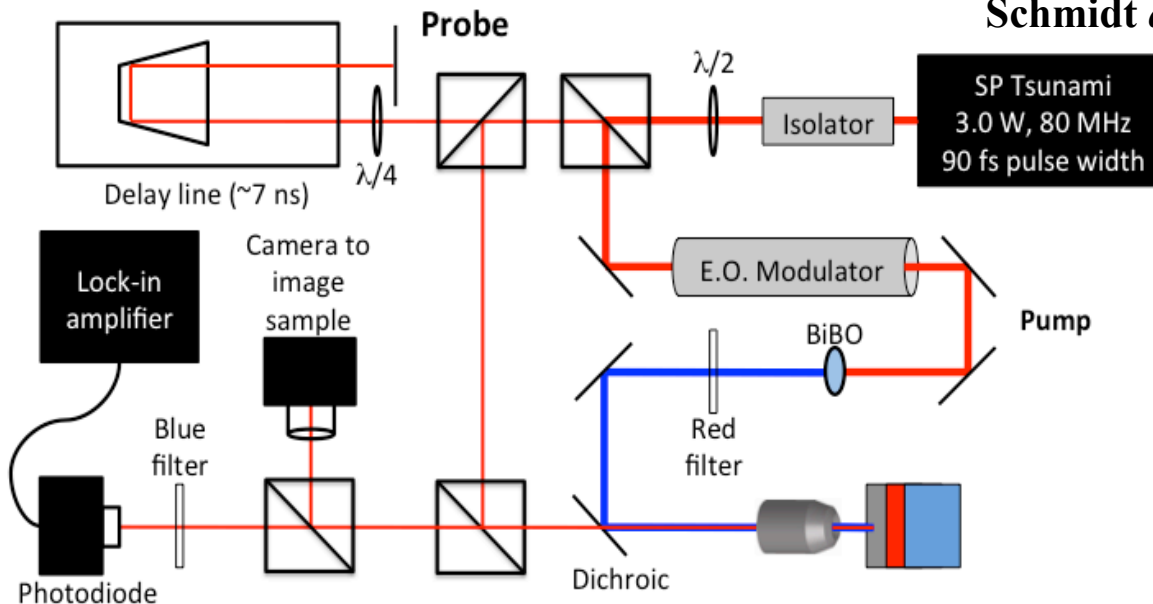


# Time Domain ThermoReflectance (TDTR)

Hopkins *et al.*, *J. Heat Trans.* 132, 081302 (2010)

Cahill, *Rev. Sci. Instr.* 75, 5119 (2004)

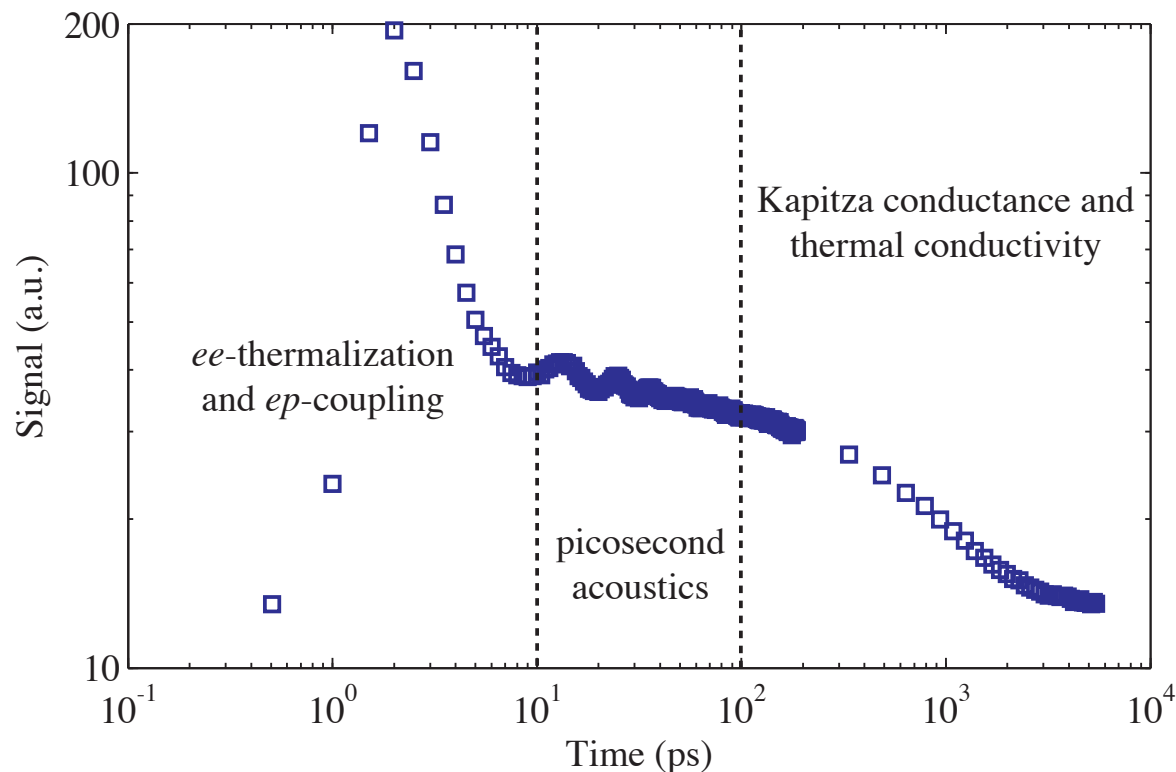
Schmidt *et al.*, *Rev. Sci. Instr.* 74, 114902 (2008)



- Can measure thermal conductivity of thin films and substrates ( $\kappa$ ) separately from thermal boundary conductance ( $h_K$ )
- Nanometer spatial resolution (~10's of nm)
- Femtosecond to nanosecond temporal resolution
- Noncontact

# Temporal regimes in TDTR data

## FANTASTIC temporal resolution (limited by pulse width)



Pulse absorption ( $\sim 100$  fs)



Fermi relaxation and  
ballistic transport (few  
hundred fs)



Electron-phonon coupling  
(a few ps)



Strain propagation in film  
(10's of ps)



Thermal diffusion  
(hundreds of ps to ns)

Now let's look at a few specific examples....

# Electron thermalization and scattering (100's of fs to a few ps)

## Journal of Heat Transfer

APRIL 2011, Vol. 133 / 044505-1

### Re-examining Electron-Fermi Relaxation in Gold Films With a Nonlinear Thermoreflectance Model

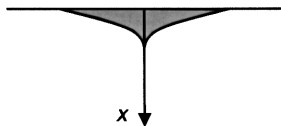
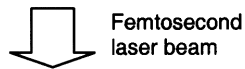
Patrick E. Hopkins

e-mail: pehopki@sandia.gov

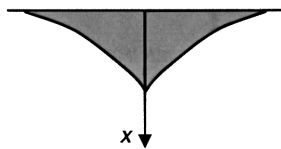
Leslie M. Phinney

Justin R. Serrano

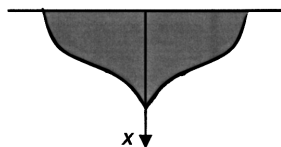
Sandia National Laboratories,  
Albuquerque, NM 87185



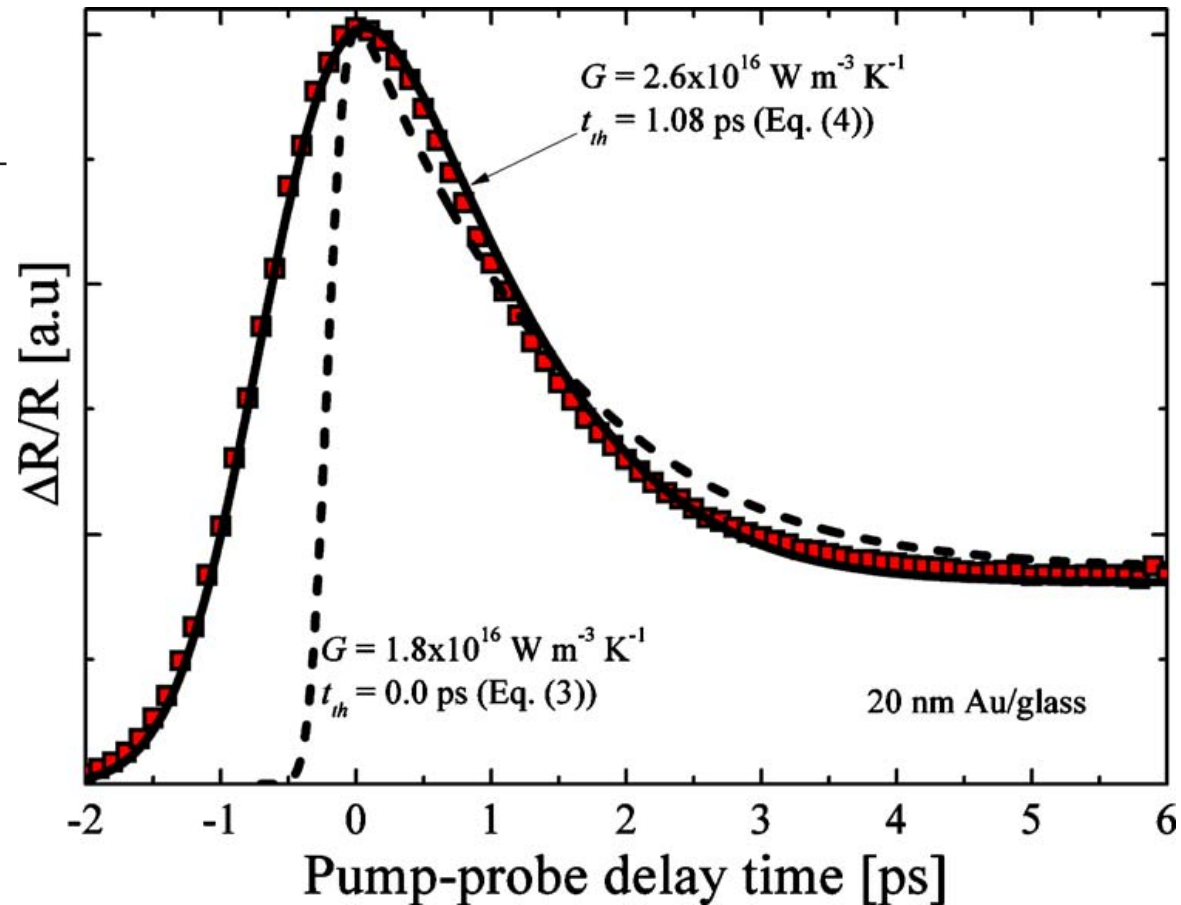
Heat transfer by  
ballistic motion of non-  
equilibrium electrons



Heat transfer by diffusion  
of hot electrons  $T_e > T_l$

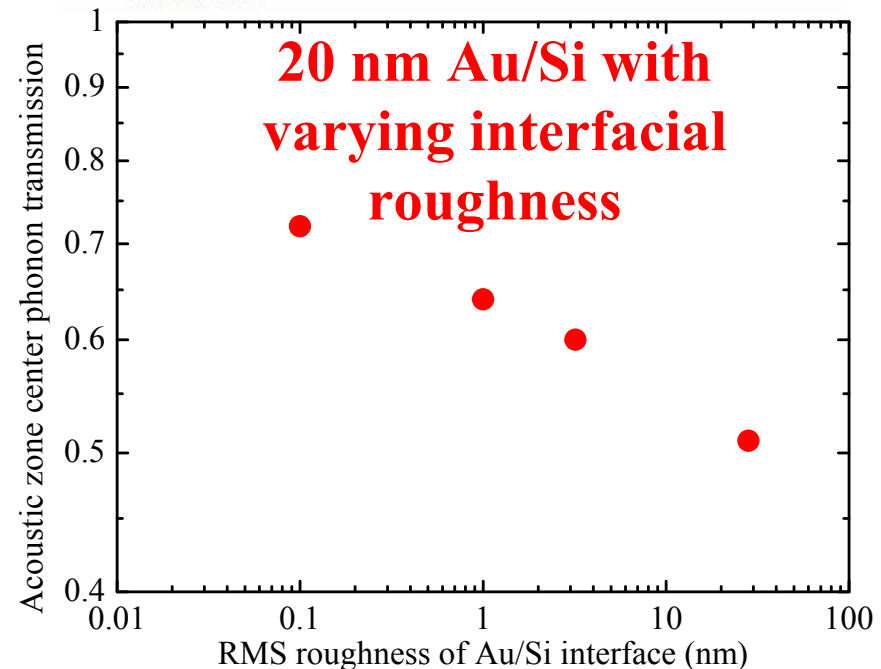
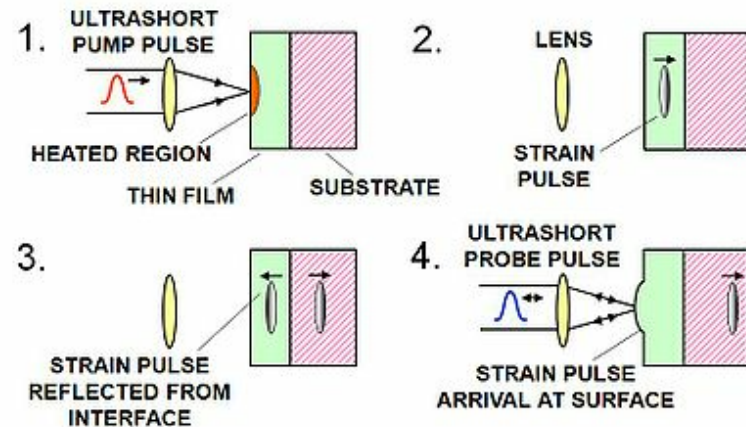
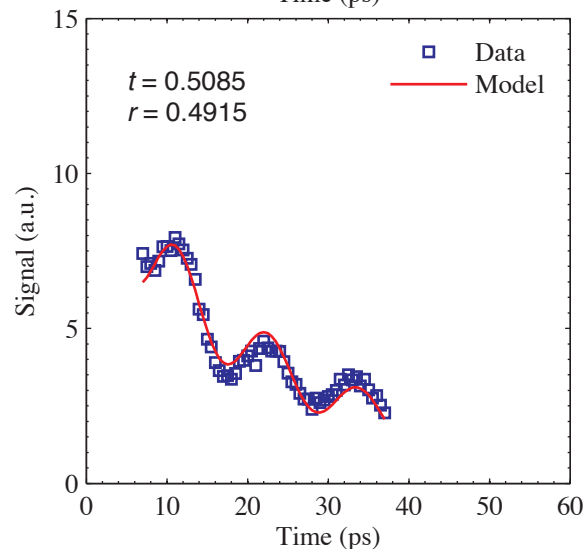
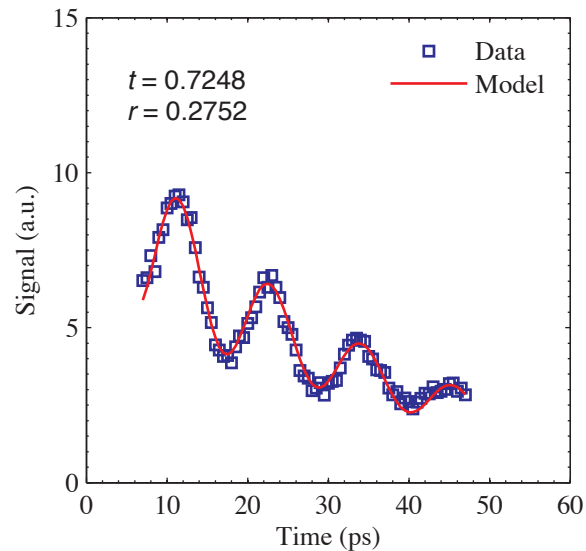


Heat transfer by  
normal thermal  
diffusion  $T_e = T_l$



# Phonon transmission (10's of ps)

**“Echoes” related to strain wave partially reflecting at film/substrate interface. Can determine interfacial transmission of zone center modes via *picosecond ultrasonics***



# Thermal conductivity of thin films (100's of ps – ns)



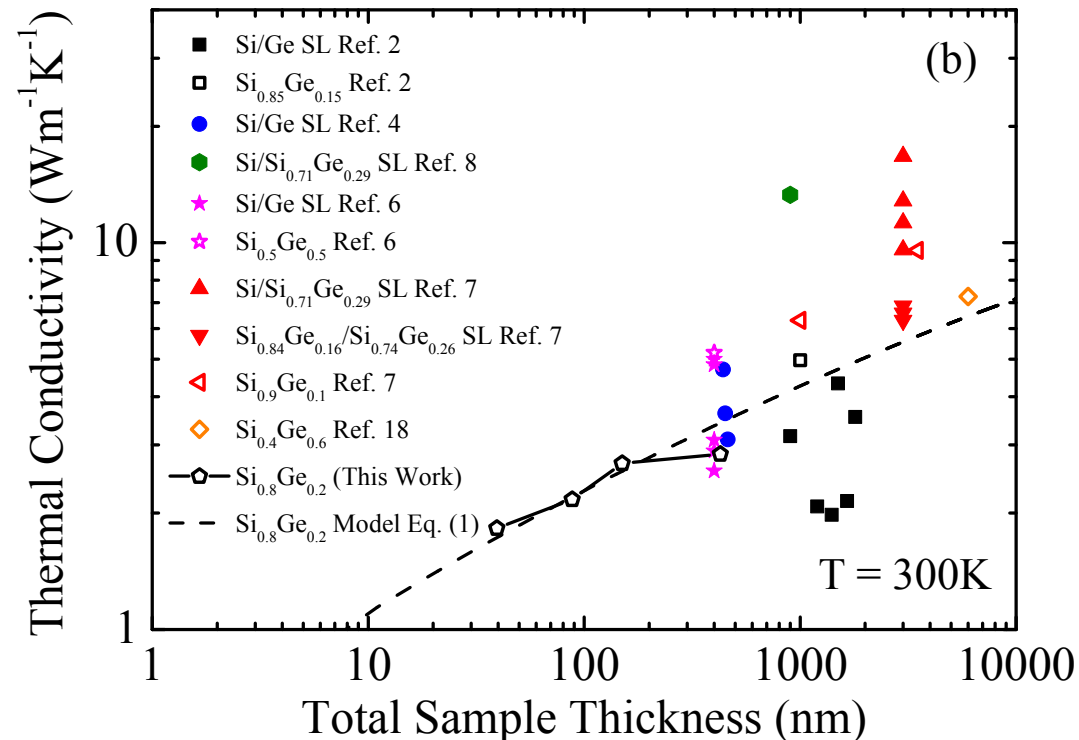
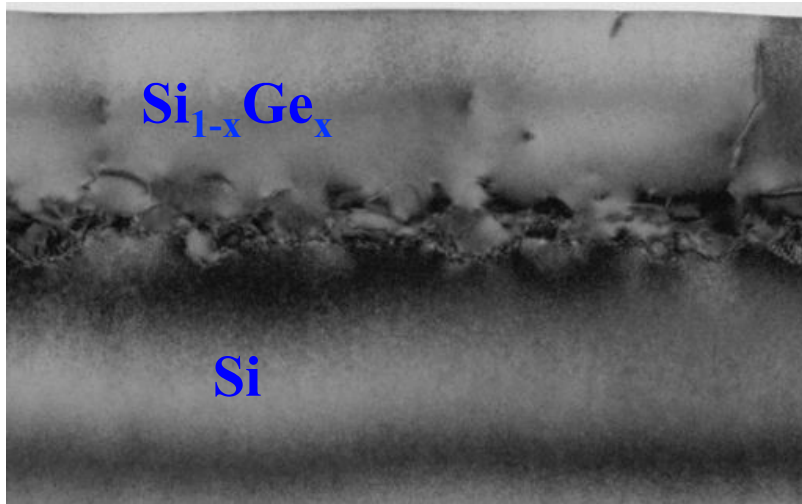
PRL **109**, 195901 (2012)

PHYSICAL REVIEW LETTERS

week ending  
9 NOVEMBER 2012

## Experimental Investigation of Size Effects on the Thermal Conductivity of Silicon-Germanium Alloy Thin Films

Ramez Cheaito,<sup>1</sup> John C. Duda,<sup>1,2</sup> Thomas E. Beechem,<sup>2</sup> Khalid Hattar,<sup>2</sup> Jon F. Ihlefeld,<sup>2</sup> Douglas L. Medlin,<sup>3</sup> Mark A. Rodriguez,<sup>2</sup> Michael J. Campion,<sup>2,4</sup> Edward S. Piekos,<sup>2</sup> and Patrick E. Hopkins<sup>1,\*</sup>



# Highly porous/nonconformal films (e.g., aerogels)

JOURNAL OF APPLIED PHYSICS **111**, 113532 (2012)

## Minimum thermal conductivity considerations in aerogel thin films

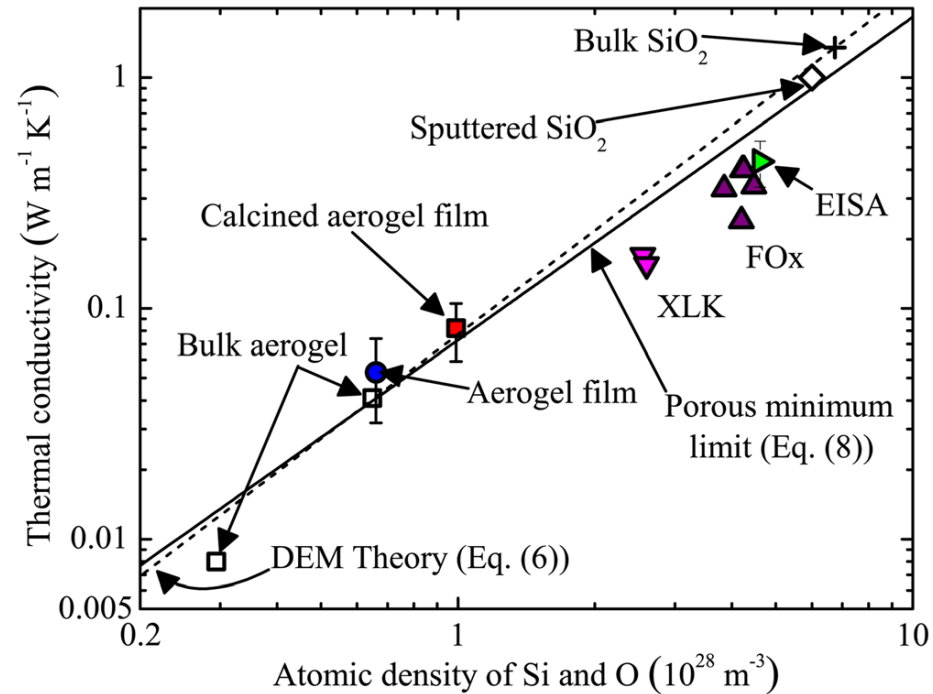
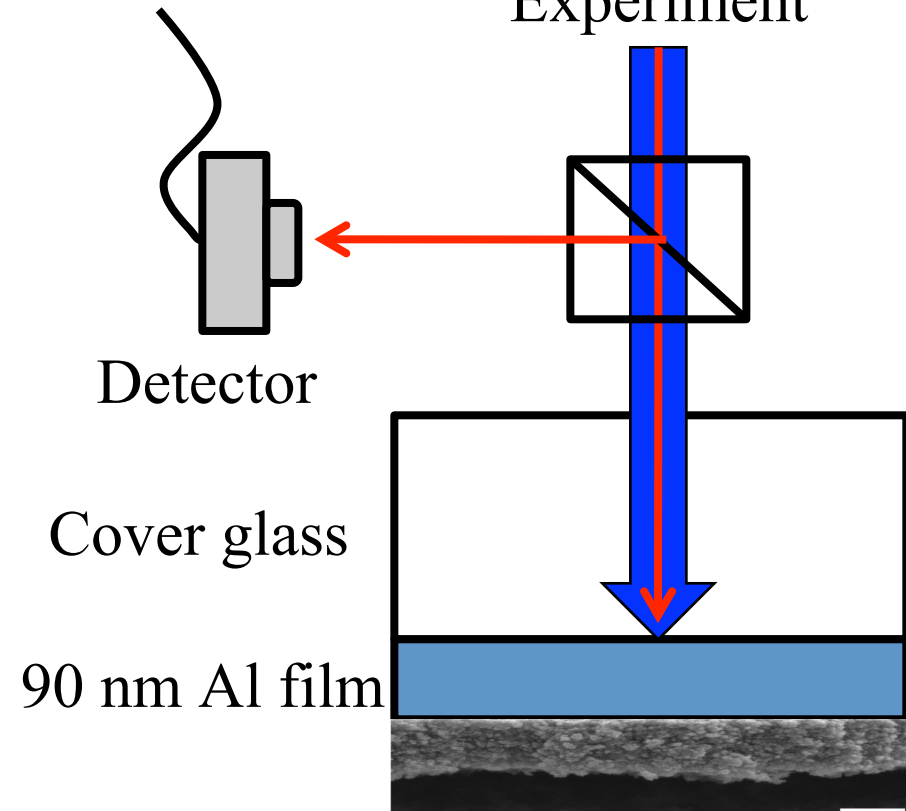
Patrick E. Hopkins,<sup>1,a)</sup> Bryan Kaehr,<sup>2,3</sup> Edward S. Piekos,<sup>2</sup> Darren Dunphy,<sup>3</sup> and C. Jeffrey Brinker<sup>2,3</sup>

<sup>1</sup>Department of Mechanical and Aerospace Engineering, University of Virginia, Charlottesville, Virginia 22904, USA

<sup>2</sup>Sandia National Laboratories, Albuquerque, New Mexico 87123, USA

<sup>3</sup>Department of Chemical and Nuclear Engineering, University of New Mexico, Albuquerque, New Mexico 87106, USA

### Experiment

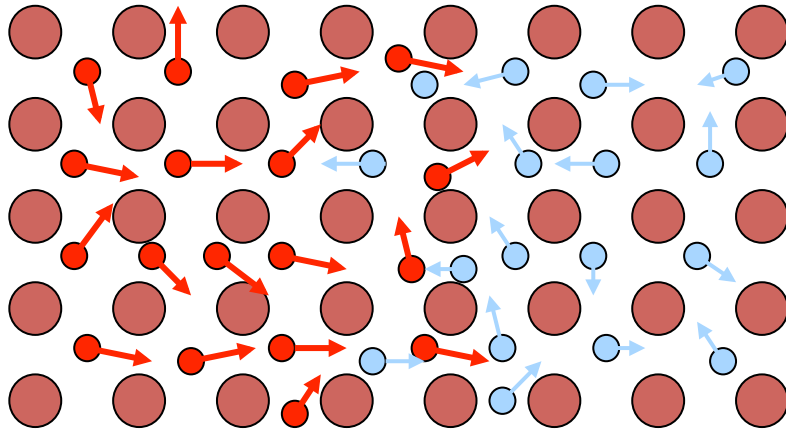




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# Heat transfer in metal vs non-metals

Diffusion of “hot” electrons



$$\kappa = \frac{1}{3} C v \lambda = \frac{1}{3} C v_g^2 \tau$$

Metals:

Free electrons are the dominant energy carriers in metals, velocity  $\sim 10^6$  m/s



atom



“hot” free electron



“cold” free electron

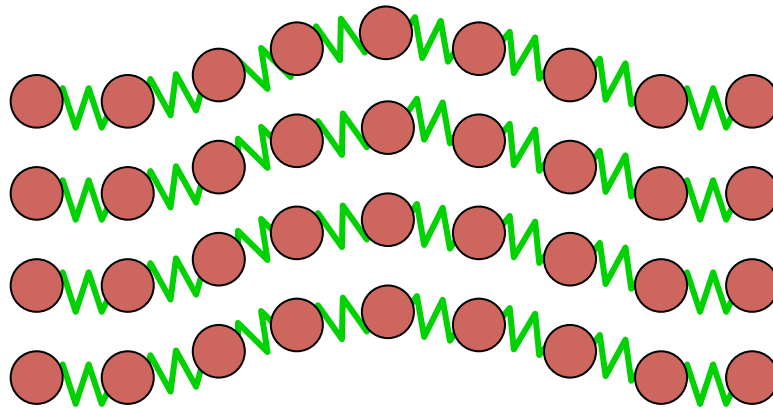
Electron carrier density:

in metals  $\sim 10^{23}$  cm $^{-3}$

in semiconductors  $\sim 10^{18}$  cm $^{-3}$

Semiconductors:

Phonons (lattice vibrations) are the dominant energy carriers in semiconductors, velocity  $\sim 10^3$  m/s

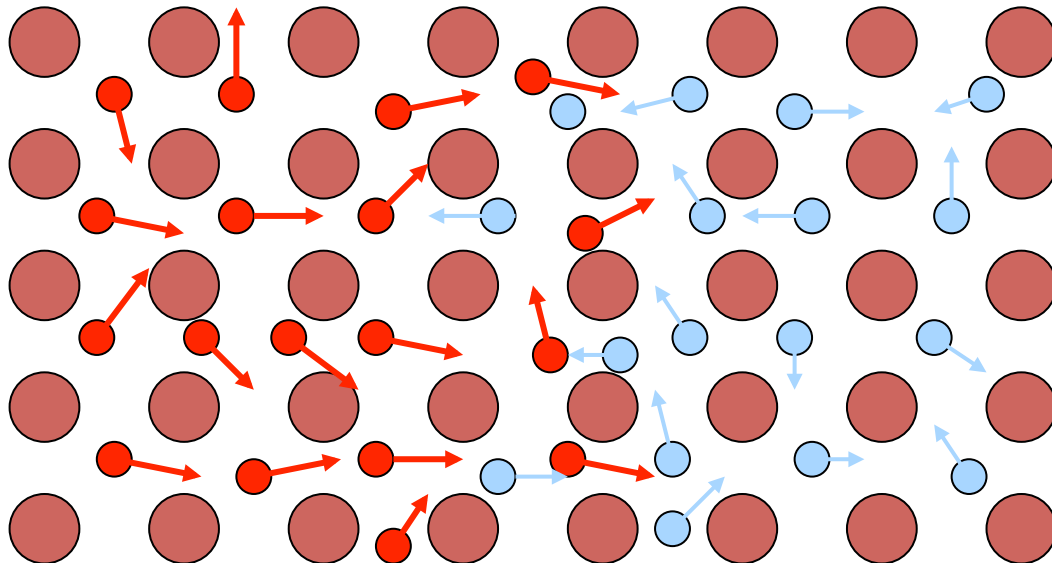
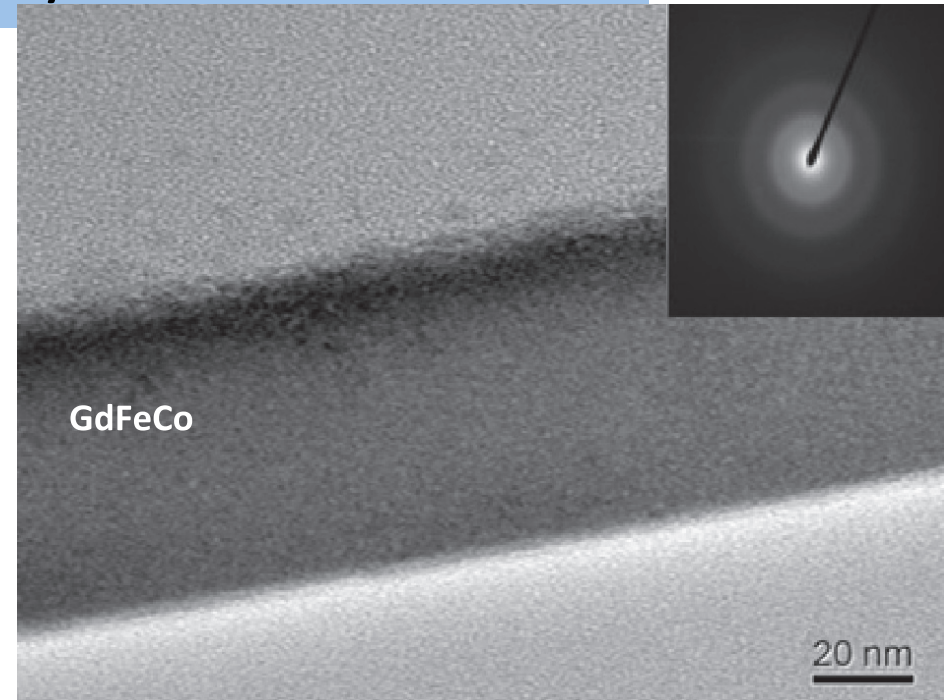


Phonon propagation

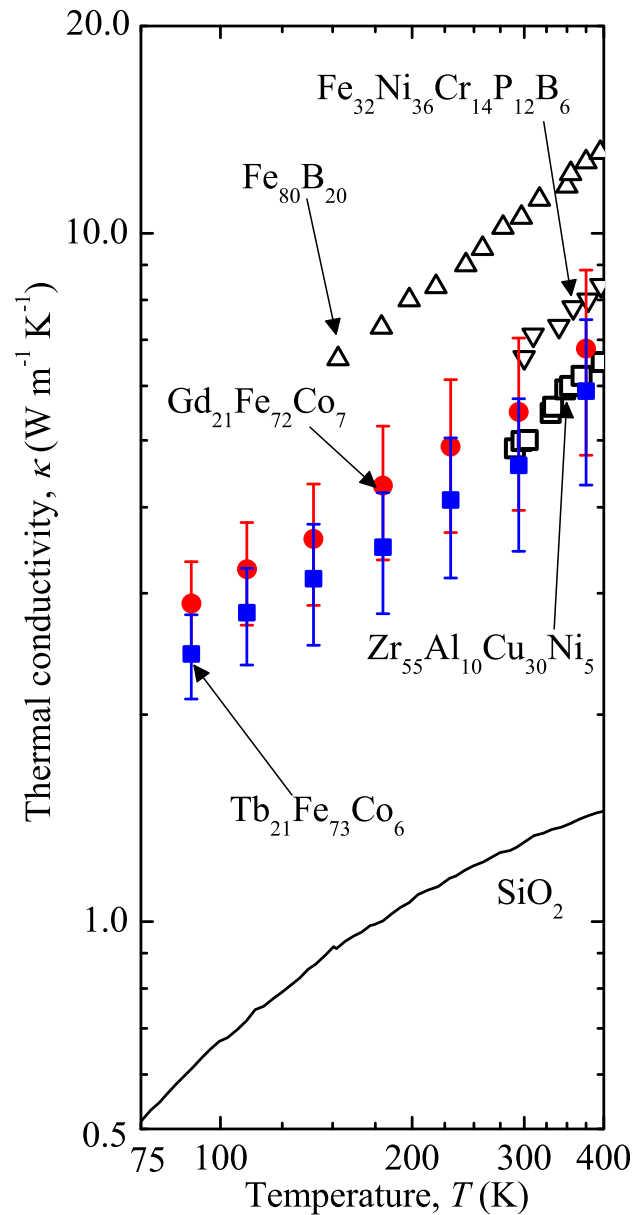


What happens if  $\lambda$  becomes very small in a metal?

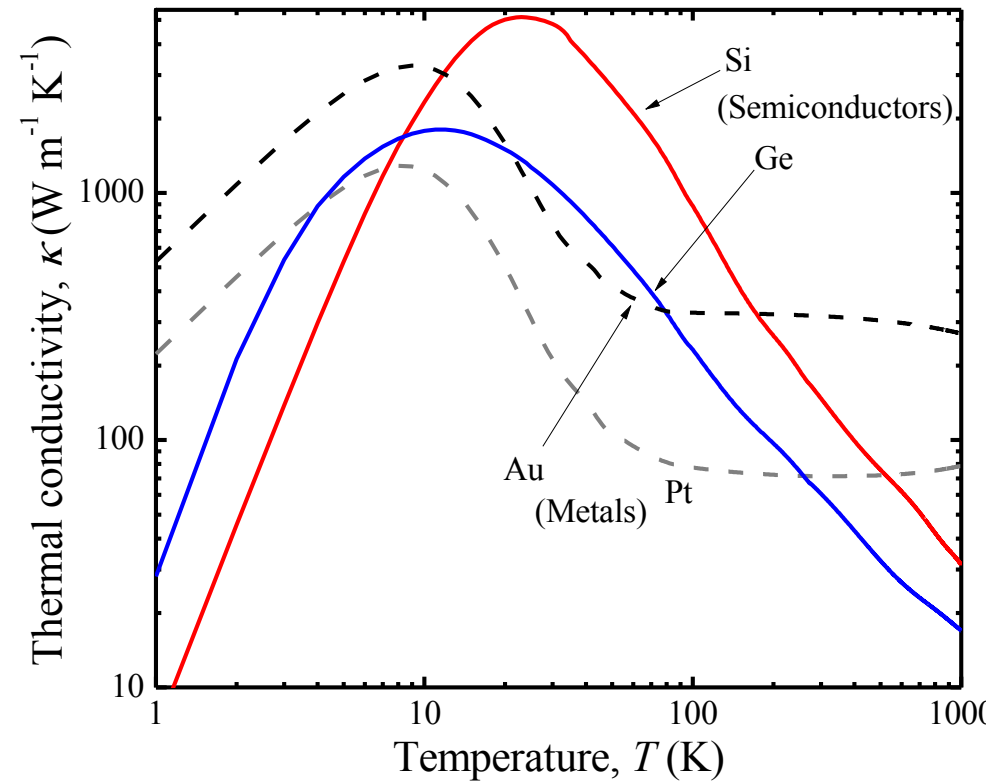
Amorphous means no atomic order. Electrons scatter A LOT!!!!



# Thermal conductivity of amorphous metals

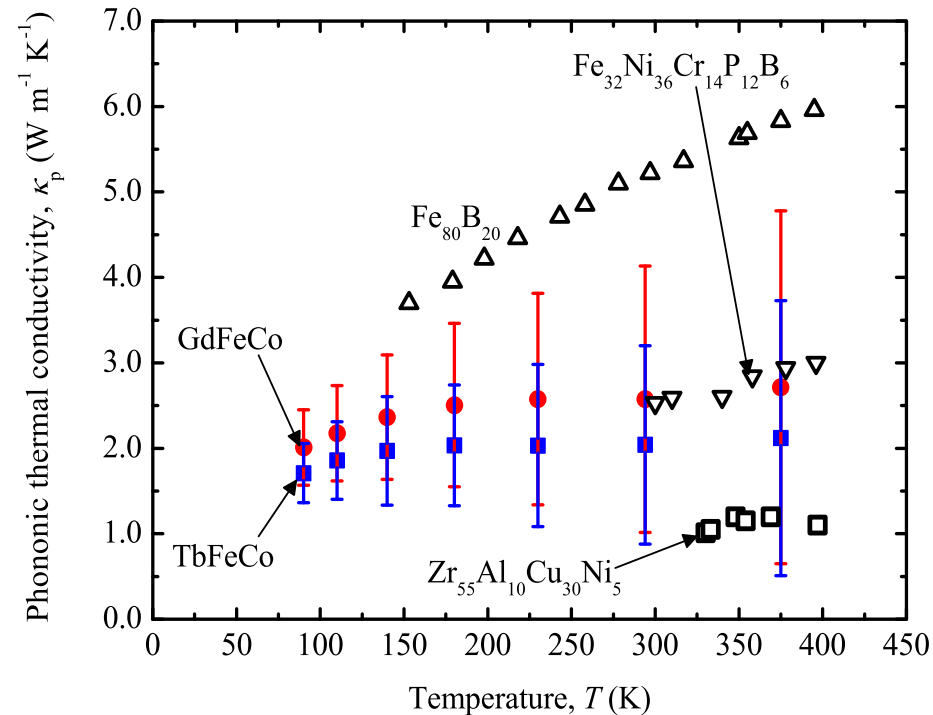
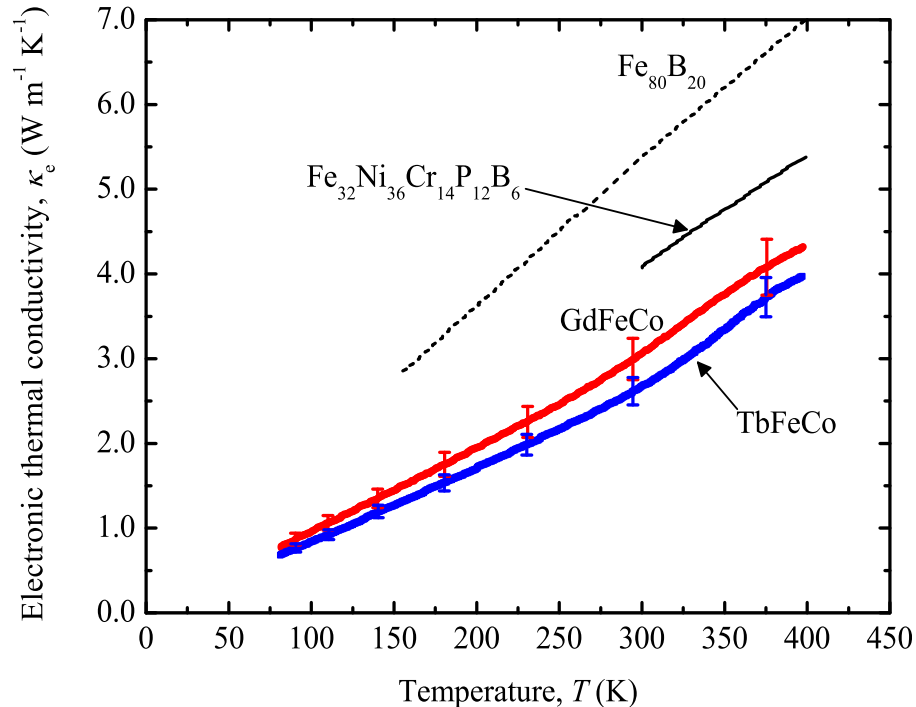


## Compare to crystalline



# BREAKDOWN...

Phonons contribute as much or more than electrons in amorphous metals



JOURNAL OF APPLIED PHYSICS **111**, 103533 (2012)

## Contributions of electron and phonon transport to the thermal conductivity of GdFeCo and TbFeCo amorphous rare-earth transition-metal alloys

Patrick E. Hopkins,<sup>1,a)</sup> Manli Ding,<sup>2</sup> and Joseph Poon<sup>2</sup>

<sup>1</sup>Department of Mechanical and Aerospace Engineering, University of Virginia, Charlottesville, Virginia 22904, USA

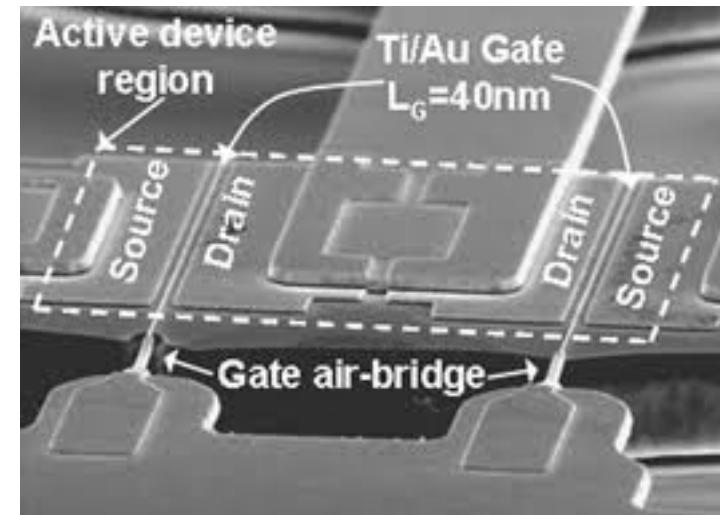
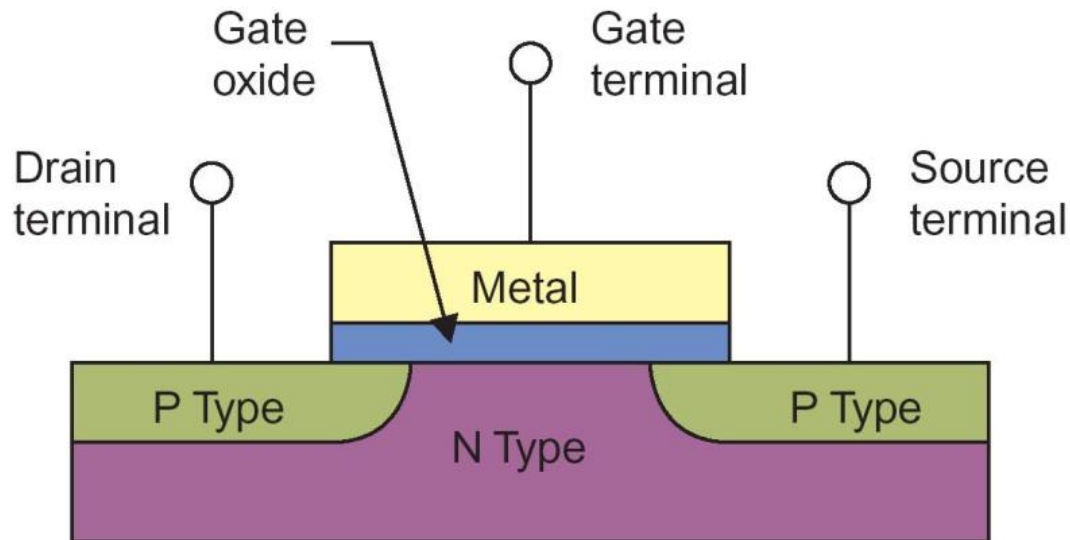
<sup>2</sup>Department of Physics, University of Virginia, Charlottesville, Virginia 22904, USA

- **Thermophysics background**
- **Measurement of electron and phonon thermal properties on the nanoscale with time domain thermoreflectance – time scales and phenomena**
- **Example 1: Amorphous metals: electron AND phonon transport**
- **Example 2: Interfaces: disorder and adhesion**
- **Example 3: Exceptionally low thermal conductivity of organic semiconducting polymers: making Einstein proud**



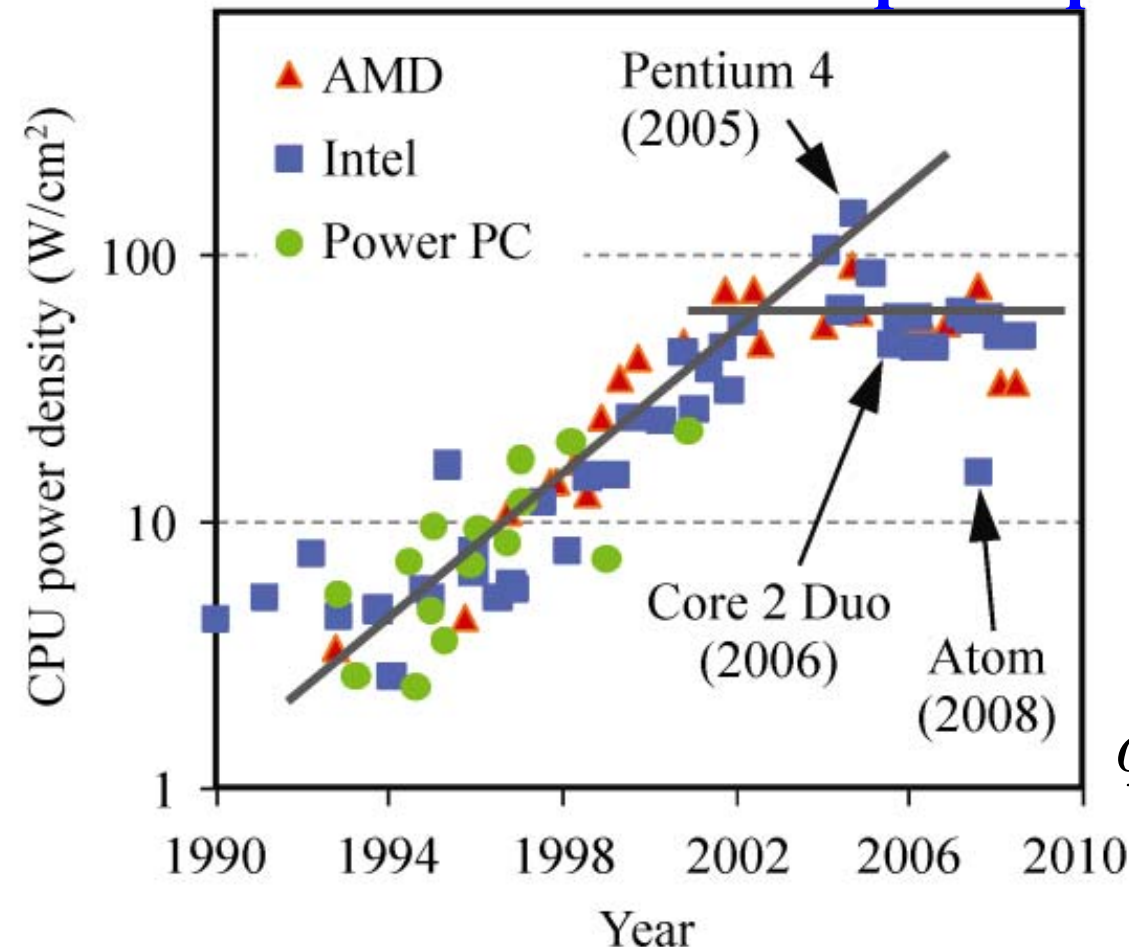
# Nanodevices – interface problems

**Electronic devices have length scales less than the thermal mean free paths. The various interfaces must be understood to mitigate the heat load.**



**Silicon mean free paths at room temperature  
~50 – 500 nm (it's a spectrum like photons)**

## Silicon device interfaces cause overheating Sacrifice computer performance



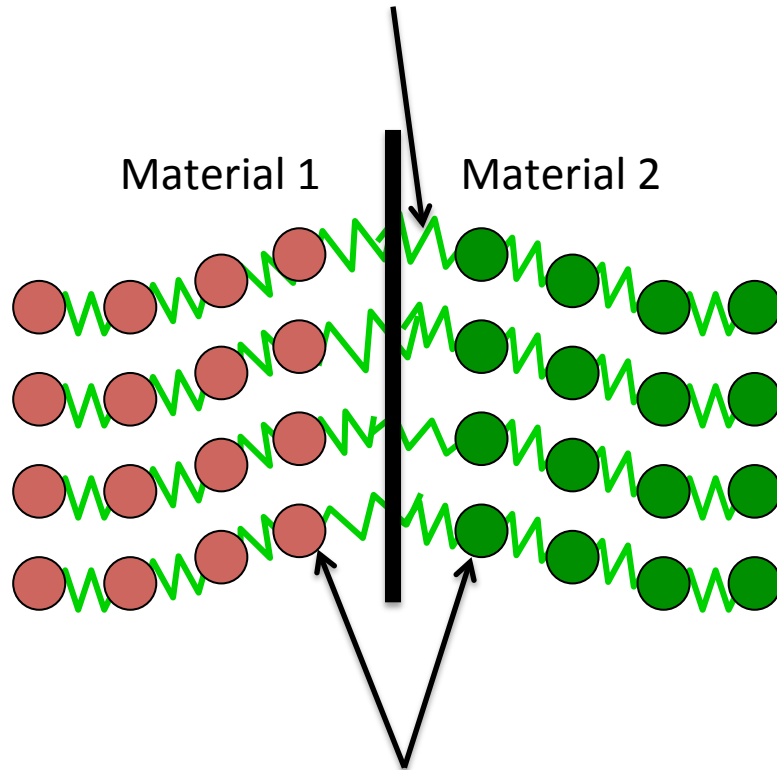
*Nano. Res. 3, 147 (2010)*

A schematic diagram showing a cross-section of a thermal interface. On the left is a yellow rectangular block, and on the right is a blue rectangular block. A curved black line represents the interface between them. A vertical arrow labeled  $T$  points upwards on the left side. A horizontal arrow labeled  $q_{\text{int}}$  points to the right above the interface. A horizontal arrow labeled  $z$  points to the right below the blocks.

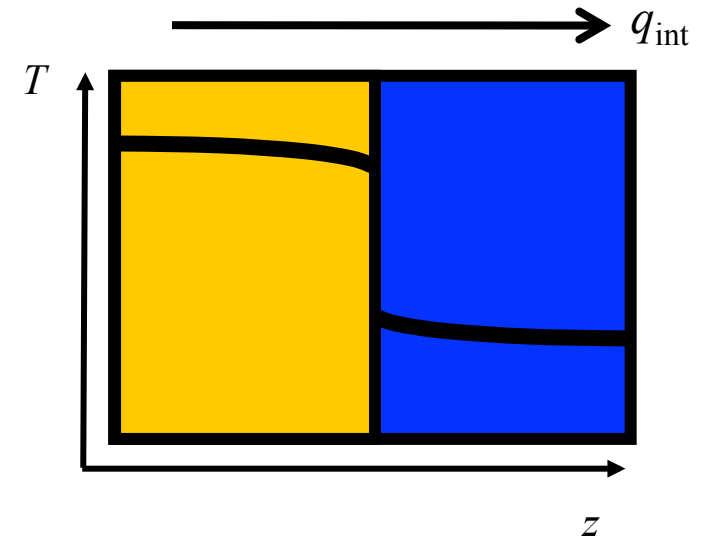
$$q_{\text{int}} = h_K \Delta T = \frac{1}{R_K} \Delta T$$

Let's just consider a mass spring problem!

## Interfacial springs



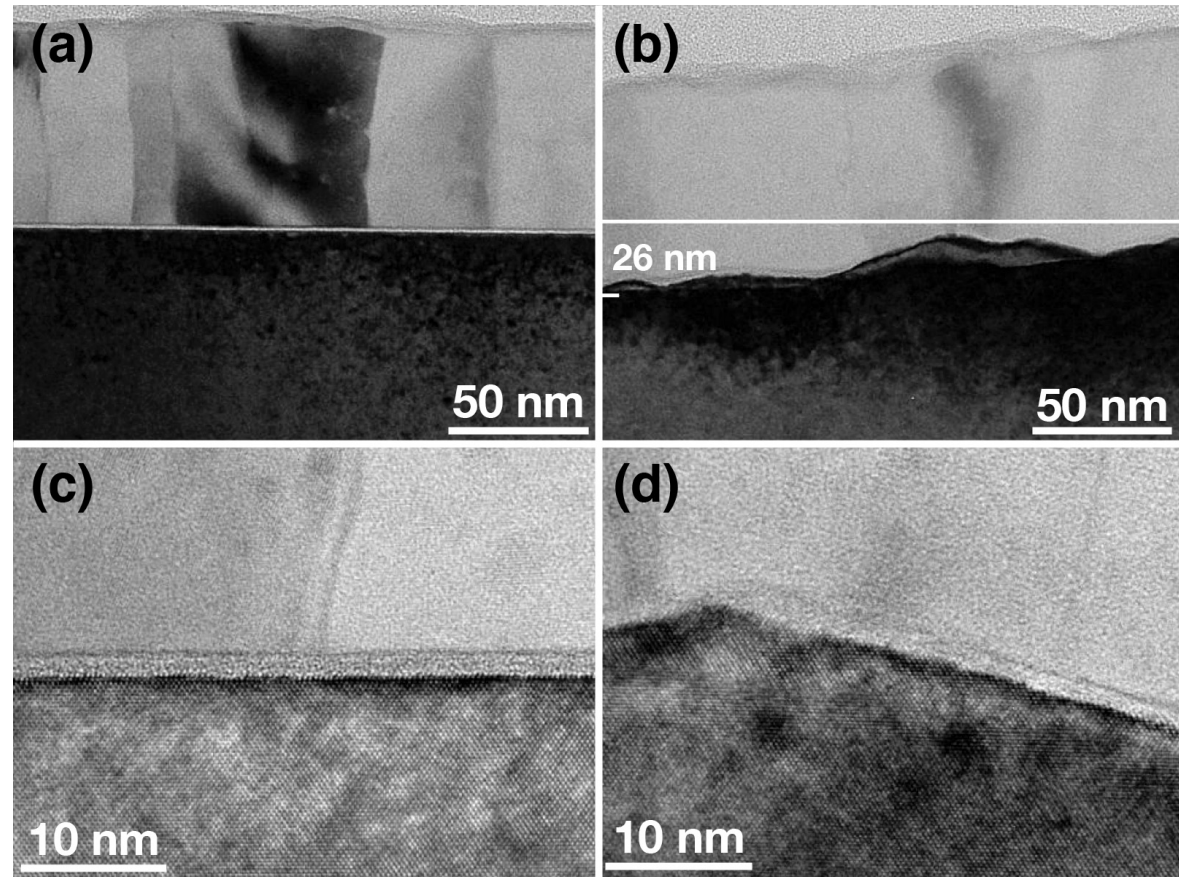
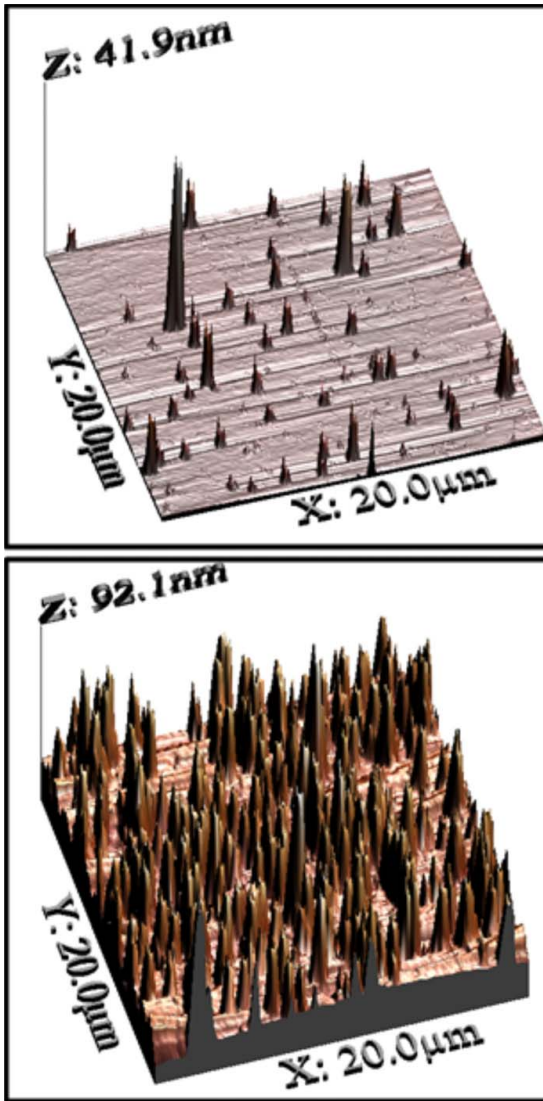
## Interfacial masses



$$q_{\text{int}} = h_K \Delta T = \frac{1}{R_K} \Delta T$$

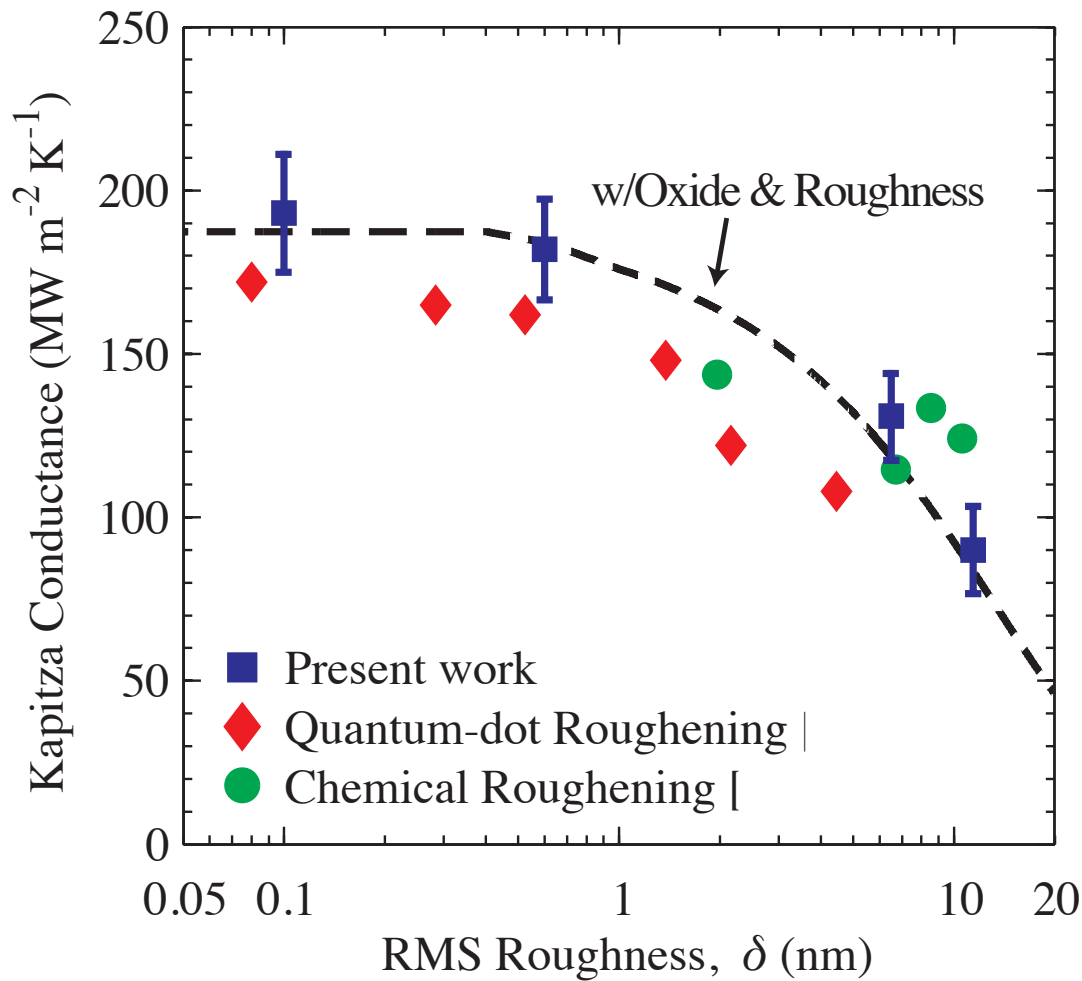
# Let's mess up some simple interfaces – Al/Si

**TMAH processed to change surface roughness**

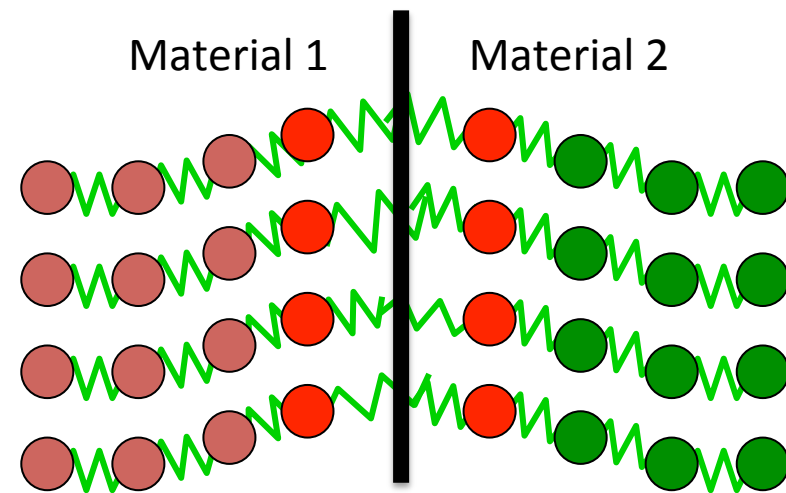


Hopkins *et al.*, *Phys. Rev. B.* 82, 085307 (2010)  
Duda and Hopkins, *Appl. Phys. Lett.* 100, 111602 (2012)

# Roughness as a “knob” for thermal control



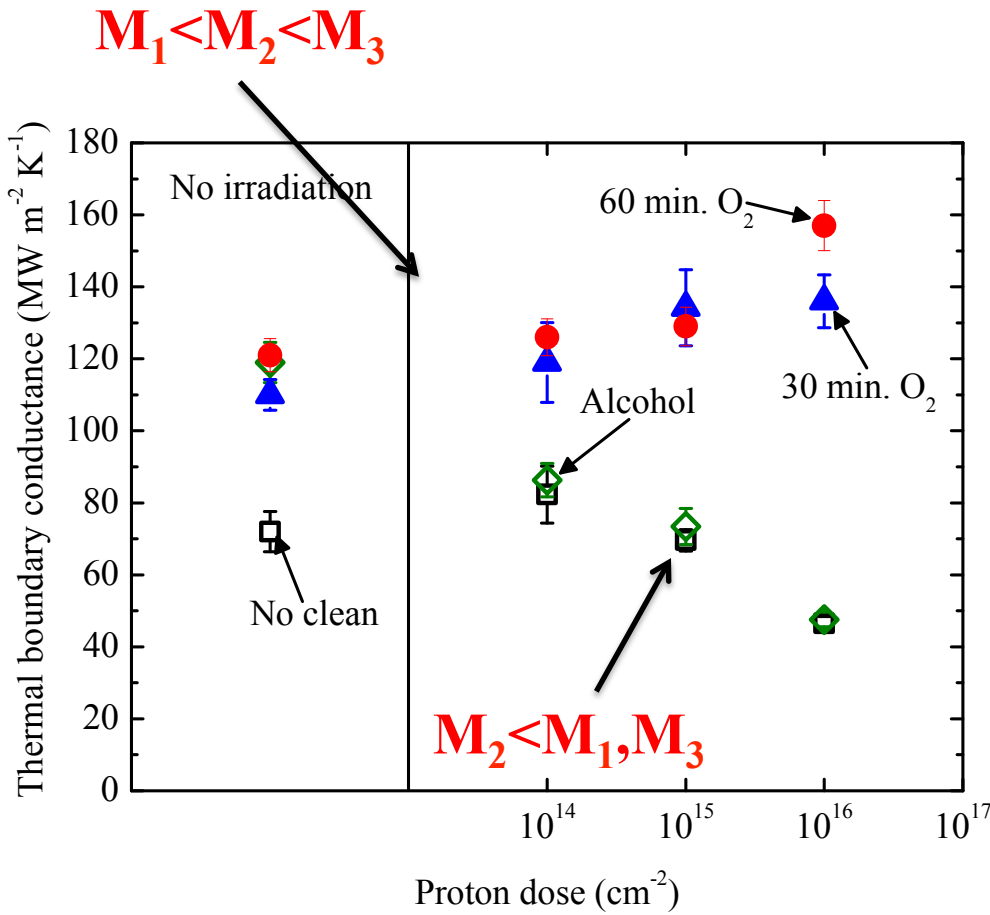
**Change the arrangement  
of masses around the  
interface (disorder)**



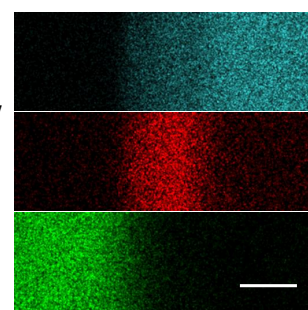
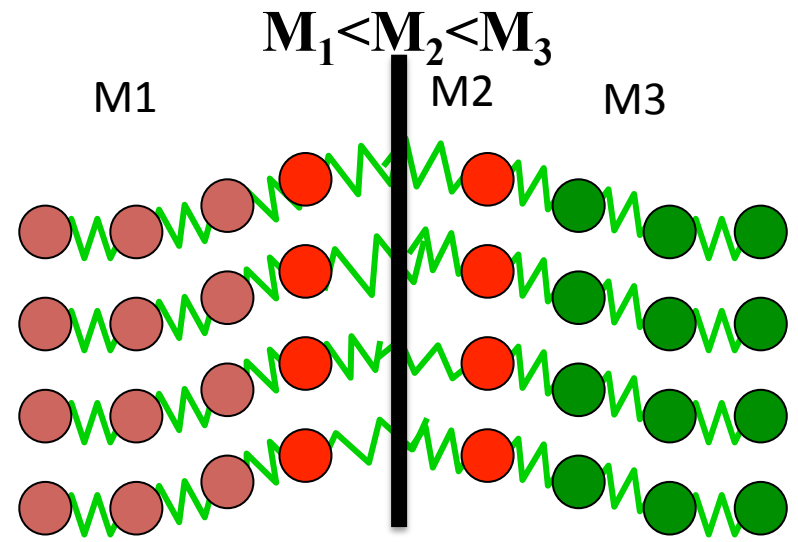
**Duda and Hopkins, *Appl. Phys. Lett.* 100, 111602 (2012)**



# Can mass disorder *increase* TBC?



TBC can increase if



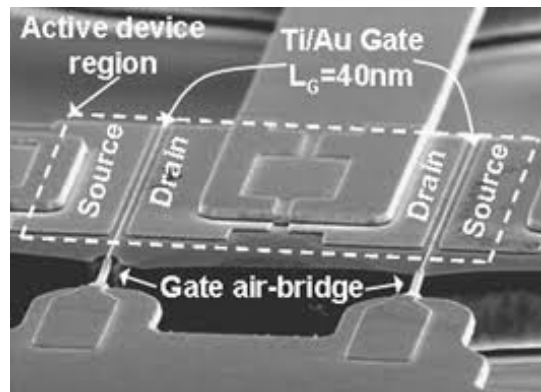
An interfacial mixing region creates an “impedance bridge” (Polanco and Ghosh, ECE)



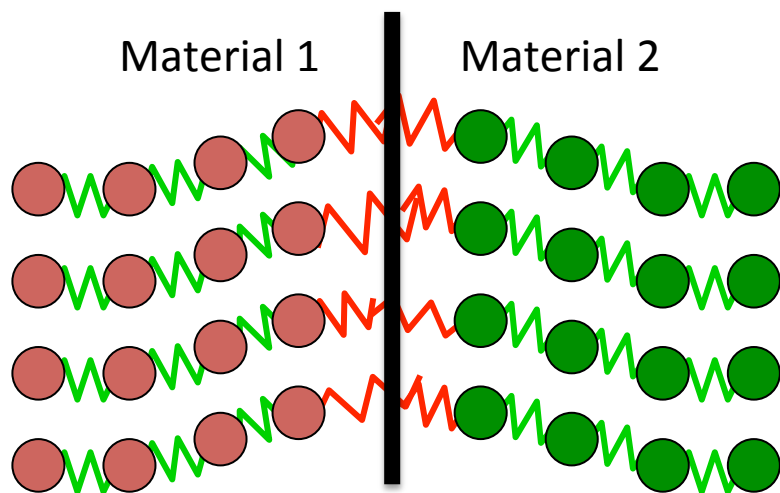
**Caroline Gorham** *et al.*, to be presented next week at MRS



# What about device contacts? Au/Si

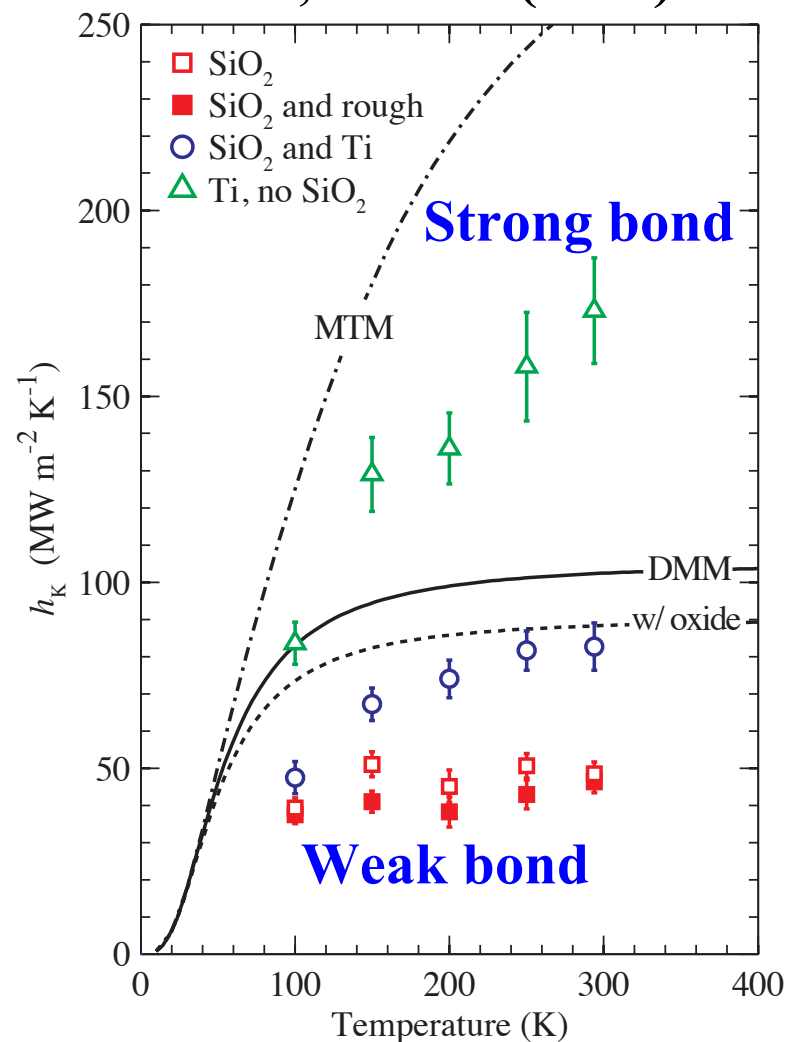


However, bonding plays a **HUGE ROLE** at the Au/Si interface



Change the springs around the interface (disorder)

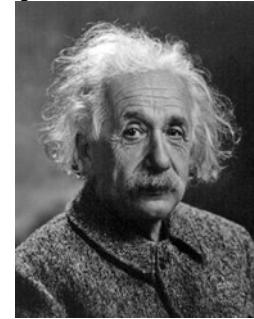
Duda *et al. Appl. Phys. Lett.*  
102, 081902 (2013)



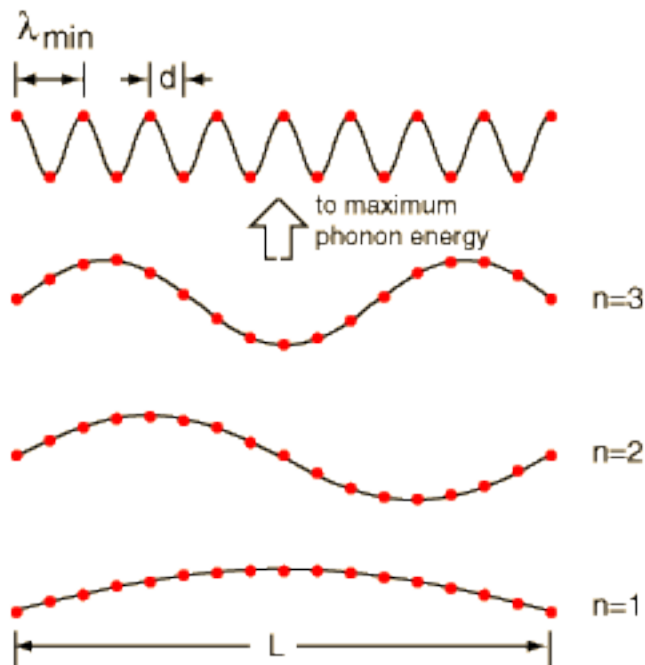
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# “The Einstein oscillator”

Vibrations of atoms are not coupled, they are independent with random phases



The phonon picture (coupled oscillators): several different wavelength in a lattice (many energies)

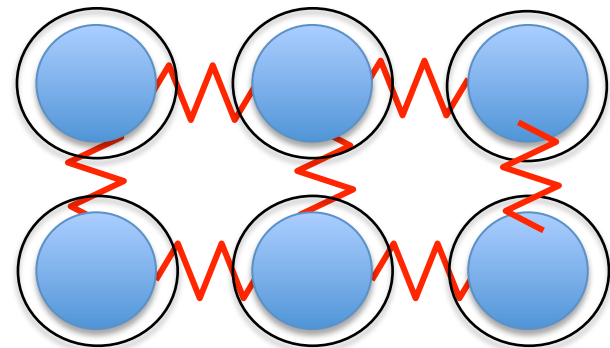


$$\lambda_{\min} = 2d$$

$$\lambda_n = \frac{2L}{n}$$

$$\lambda_{\max} = 2L$$

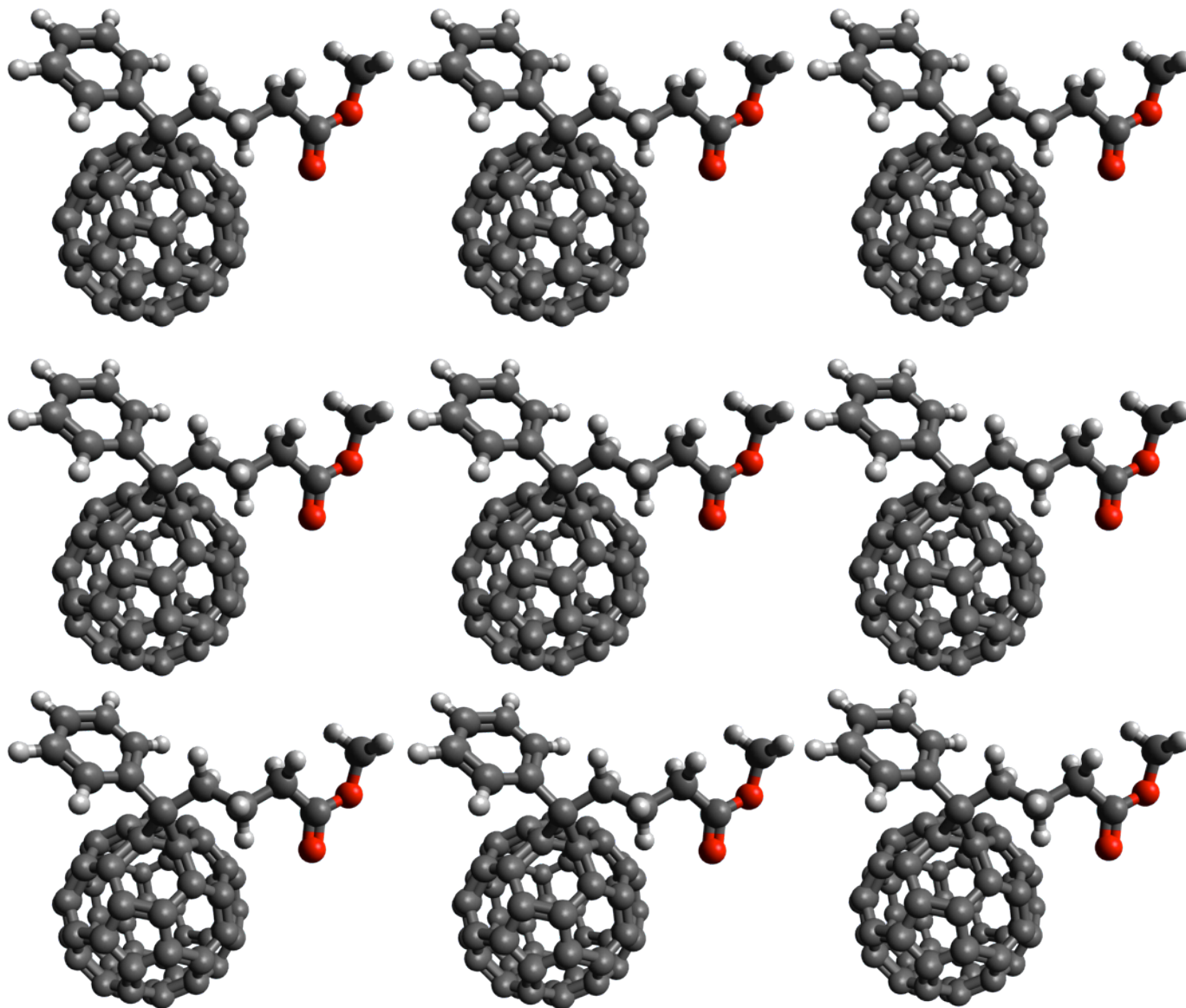
Single frequency of vibration of atom and energy “hops” from one site to another



“Springs” are very very weak

# Weakly interacting buckyballs

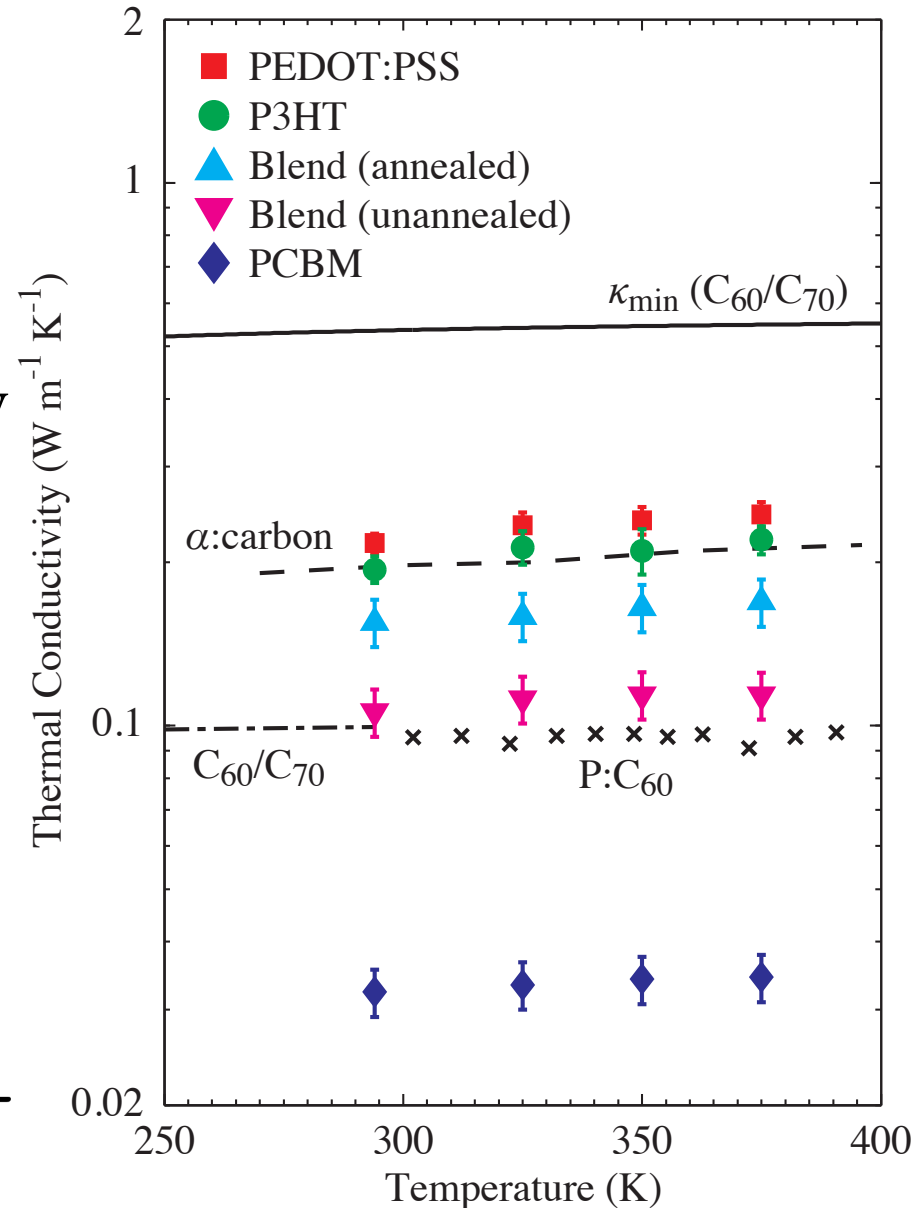
**[6,6]-phenyl C<sub>61</sub>-butyric acid methyl ester (PCBM) – an Einstein oscillator**



# Thermal conductivity of thin film polymers

- Annealing increases blend thermal conductivity by ~40%
- PCBM thermal conductivity  $0.032 \text{ W m}^{-1} \text{ K}^{-1}$
- Nearly 1.5 orders of magnitude less than theoretical minimum limit to thermal conductivity

$$\kappa = \frac{1}{3} C v \lambda = \frac{1}{3} C v_g^2 \tau$$



# Lowest thermal conductivity of ANY dense solid

## Exceptionally Low Thermal Conductivities of Films of the Fullerene Derivative PCBM

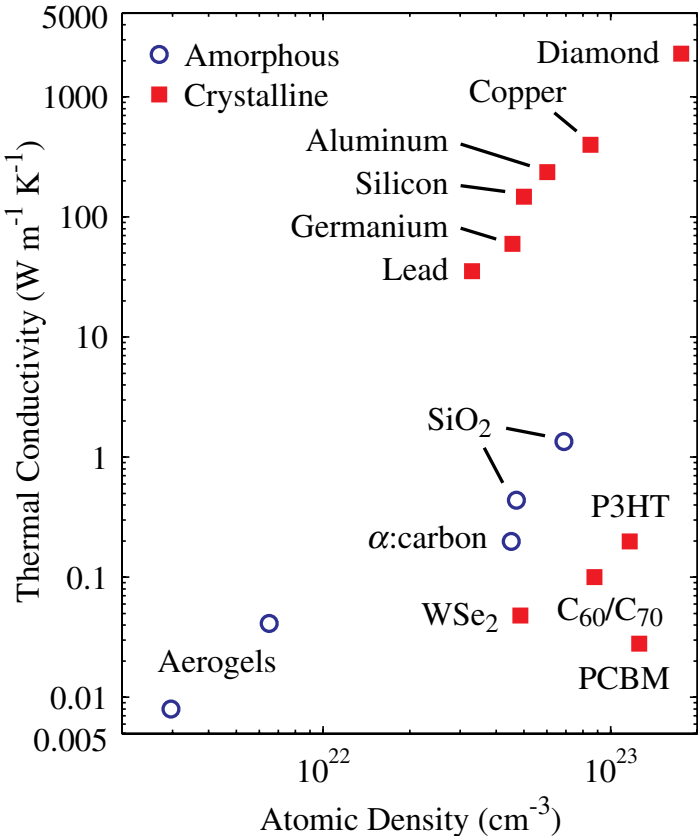
John C. Duda and Patrick E. Hopkins\*

Department of Mechanical and Aerospace Engineering, University of Virginia, Charlottesville, Virginia 22904, USA

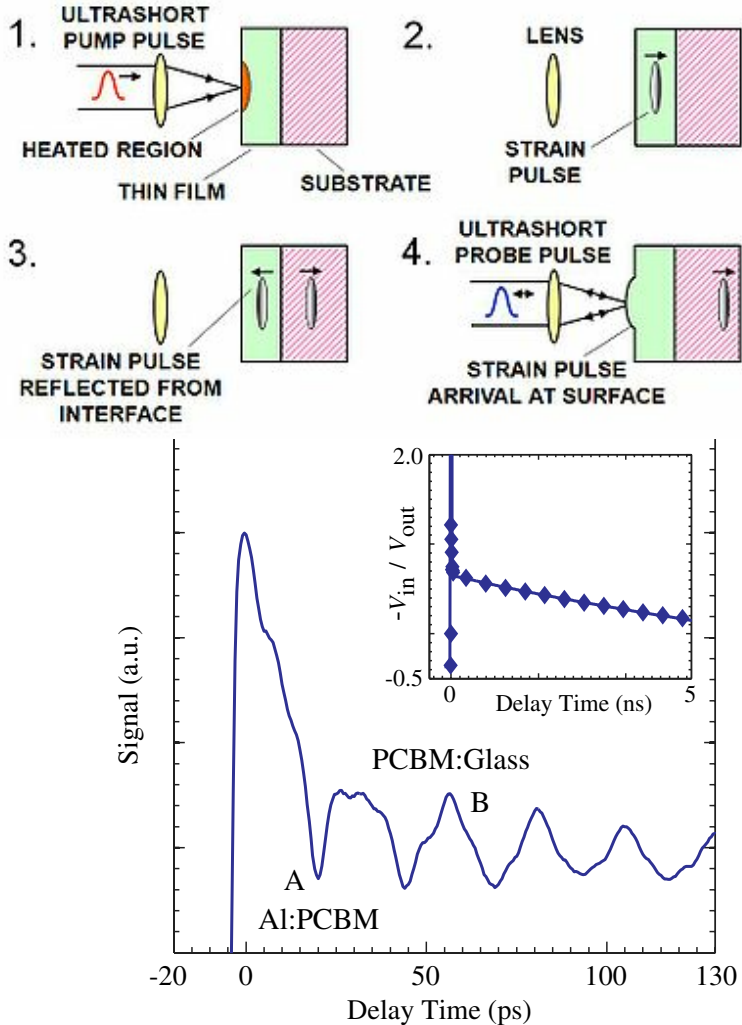
Yang Shen and Mool C. Gupta\*

Department of Electrical and Computer Engineering, University of Virginia, Charlottesville, Virginia 22904, USA

(Received 25 May 2012; revised manuscript received 30 October 2012; published 2 January 2013)



$$\kappa = \frac{1}{3} C v \lambda = \frac{1}{3} C v_g^2 \tau$$



## Nanostructuring can lead to remarkable thermal transport properties and some control of heat transfer

