



SCHOOL of ENGINEERING & APPLIED SCIENCE  
UNIVERSITY of VIRGINIA



# Effects of temperature and anharmonicity at single interfaces: evidence from experiments

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Assistant Professor

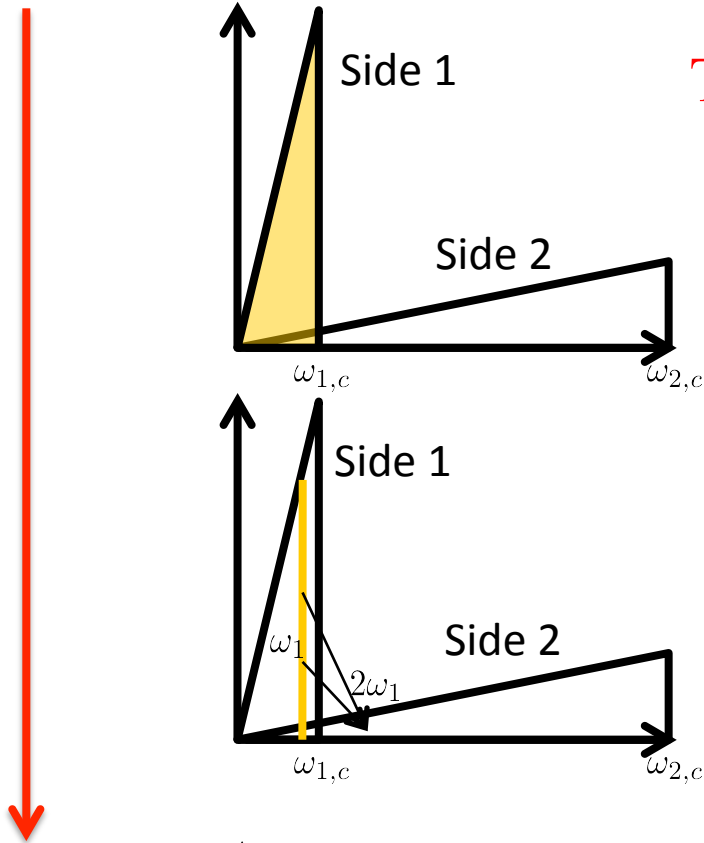
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[www.patrickehopkins.com](http://www.patrickehopkins.com)

# The density of states picture



The traditional “elastic” picture (DMM)

Swartz and Pohl, *Rev. Mod. Phys.* 61, 605 (1989)

Selected inelastic scattering

Hopkins, *J. Appl. Phys.* 106, 013528 (2009)

Hopkins, Duda, Norris, *J. Heat Trans.* 133, 062401 (2011)

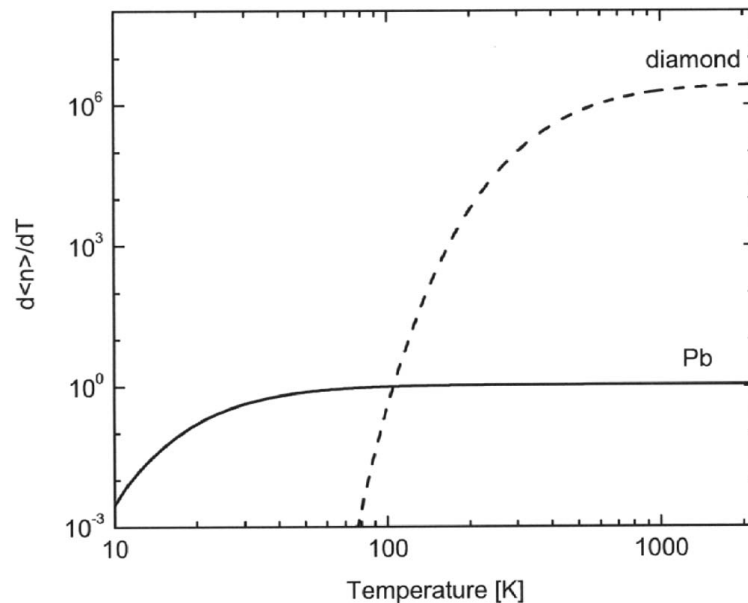
Maximum transmission (MTM)

Dames and Chen, *J. Appl. Phys.* 95, 682 (2004)

More  
anharmonicity/  
inelastic  
scattering

# Temperature dependence - anharmonicity

Hopkins and Norris, *Nano. Micro. Thermophys. Eng.* **11**, 247 (2007)

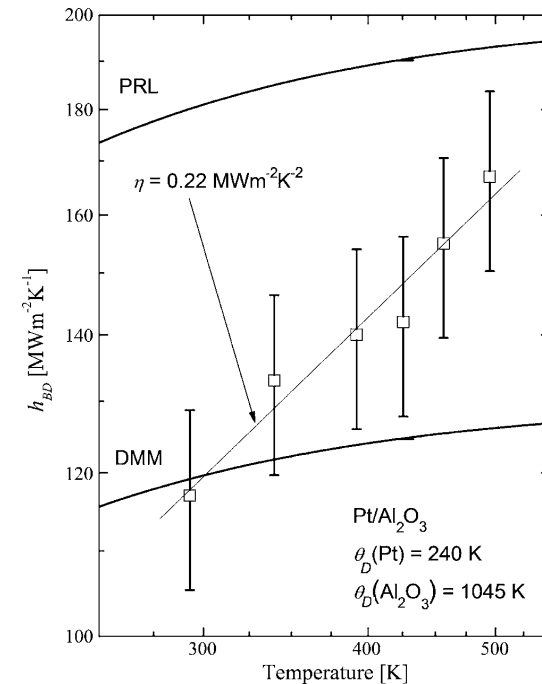
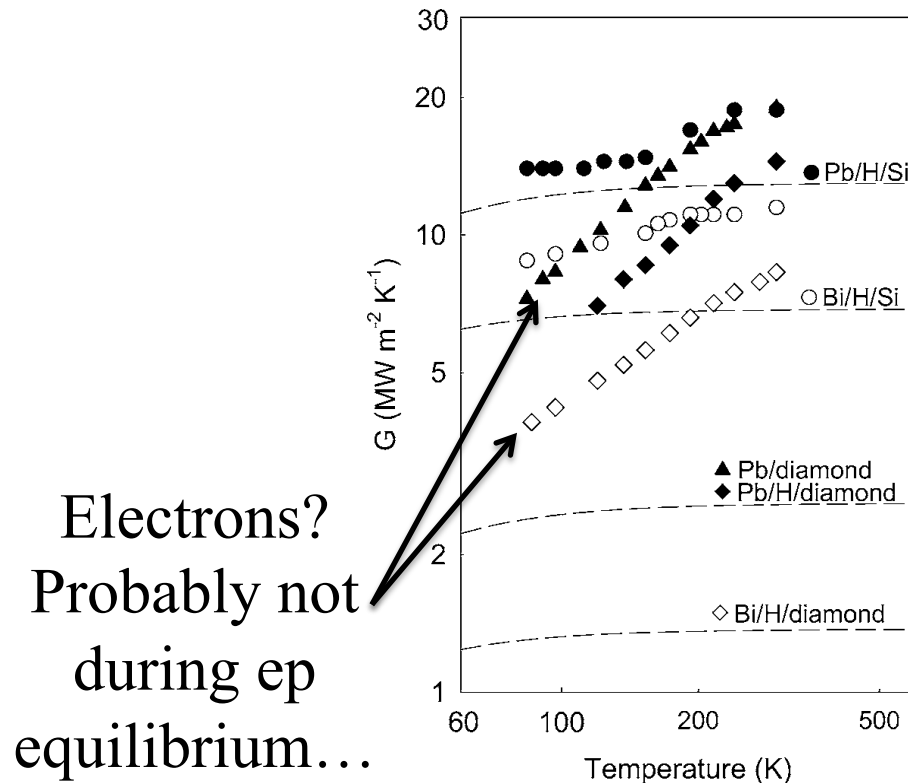


Pb temperature trends = elastic

Diamond temperature trends = inelastic

**How do temperature trends change  
relative to Debye temperatures?**

# Evidence of inelastic scattering – look at temperature trends



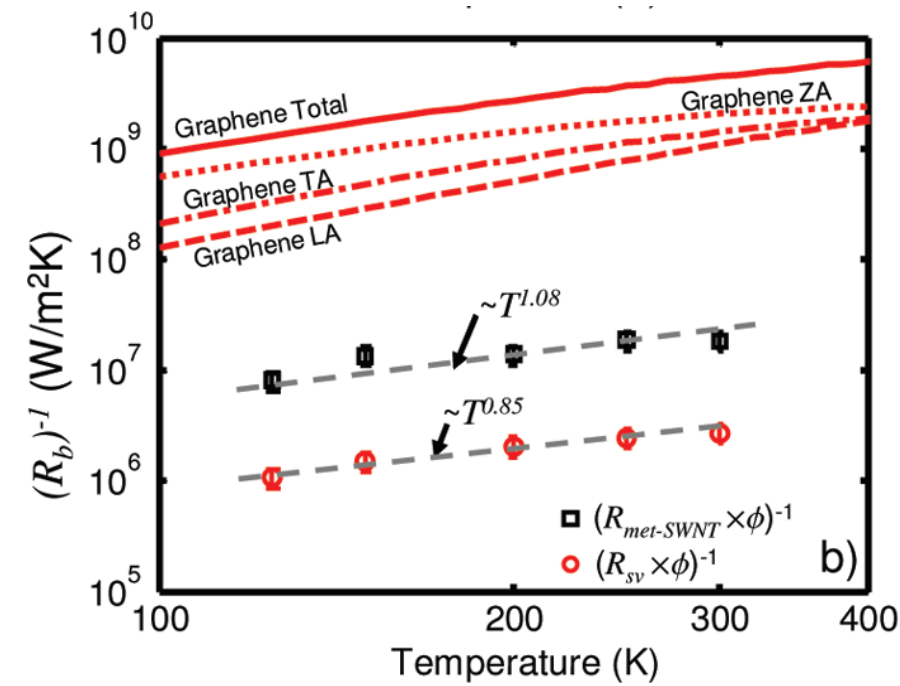
Lyao and Cahill, *Phys. Rev. B*  
**73**, 144301 (2006)

Hopkins, Norris and Stevens, *J. Heat Trans.* **130**, 022401 (2008)

**What has been observed beyond the simple metal/bulk non-metal substrate picture?**

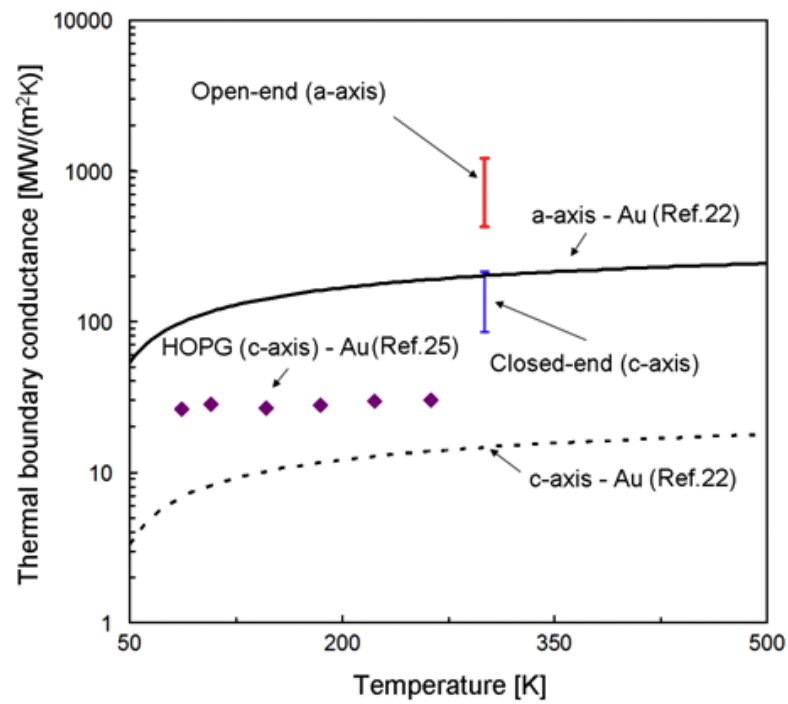
# Metal/carbon nanotubes

## Metal/SWCNT film



Panzer *et al.*, *Nano Lett.* **10**,  
2395 (2010)

## Metal/individual SWCNT



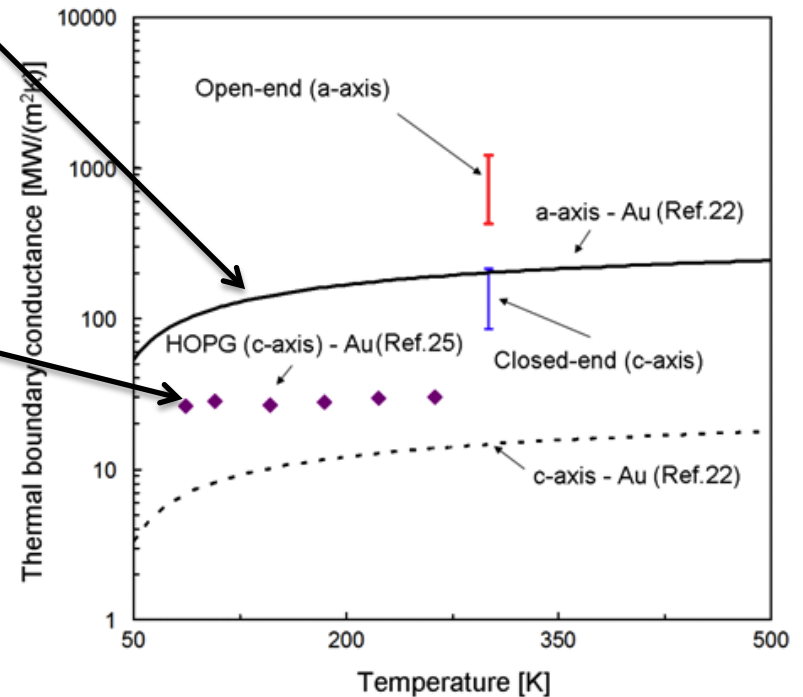
Hirotsu *et al.*, *Nanotech.* **22**, 315702 (2011)

# Metal/carbon nanotubes

Duda *et al.*, *Appl. Phys. Lett.* 95,  
031912 (2009)  
(note: Theory)

Schmidt *et al.*, *J. Appl. Phys.*  
107, 104907 (2010)

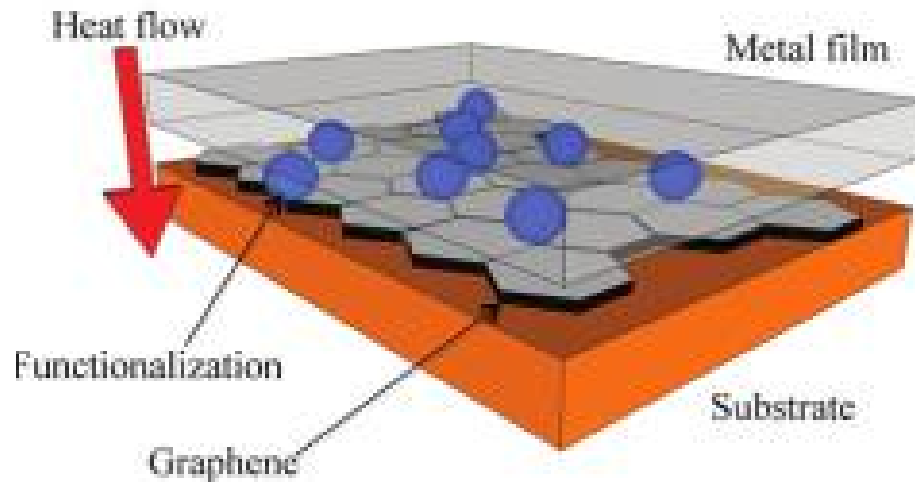
## Metal/individual SWCNT



**Can the interfacial bond enhance inelastic scattering, or does it just add elastic modes?**

Hirotsu *et al.*, *Nanotech.*  
22, 315702 (2011)

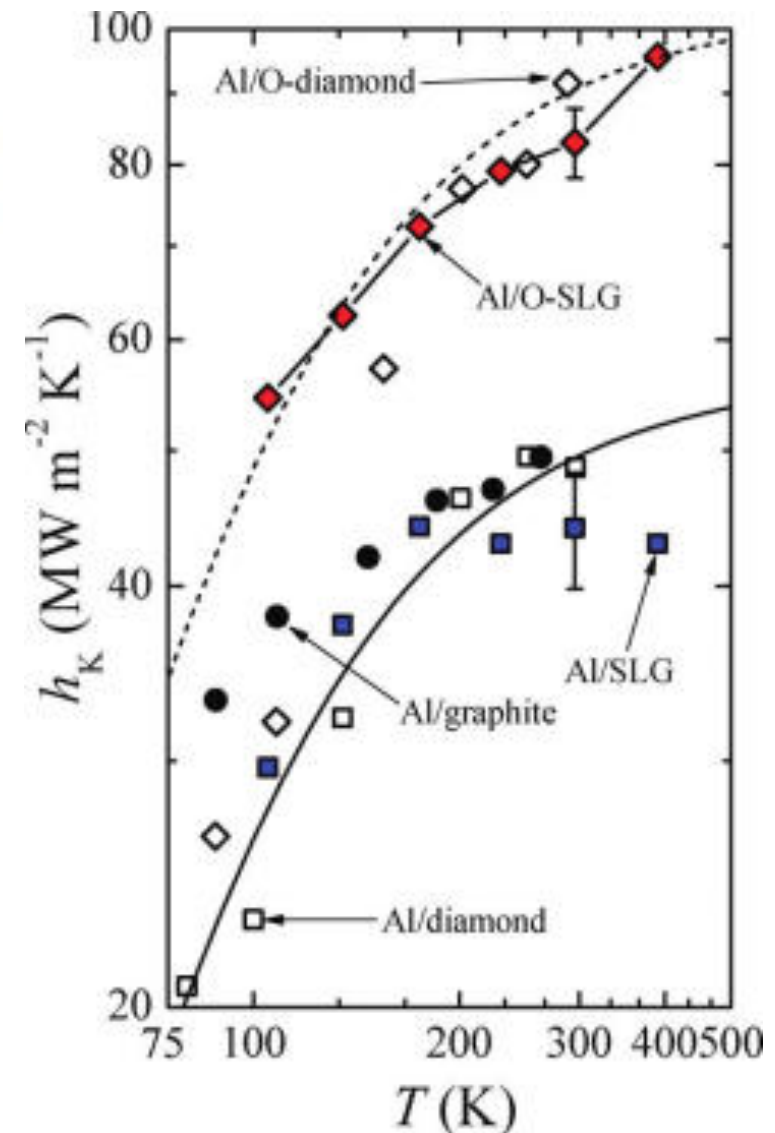
# Bonding vs. anharmonicity: graphene, graphite and diamond



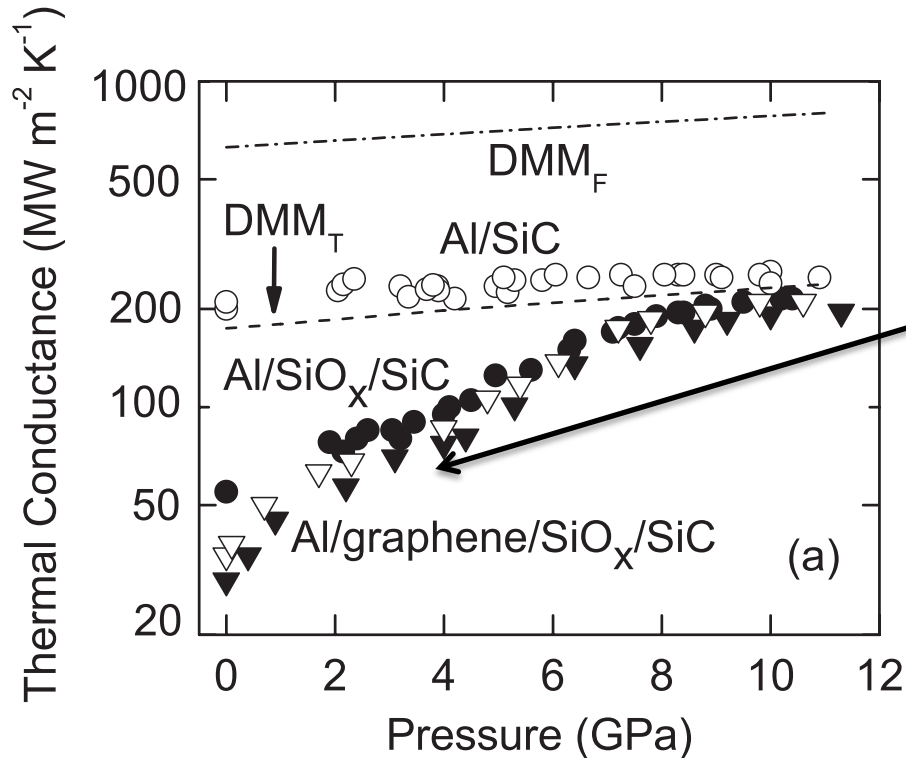
**Graphene:** Hopkins *et al.*,  
*Nano Lett.* **12**, 590 (2012)

**Graphite:** Schmidt *et al.* *J.*  
*Appl. Phys.* **107**, 104907 (2010)

**Diamond:** Collins *et al.*  
*Appl. Phys. Lett.* **97**, 083102 (2010)



# Bonding vs. anharmonicity: can pressure lend insight?



All the “action” is for the weak bond, no further change with the strong bonds. TBC scales linearly.

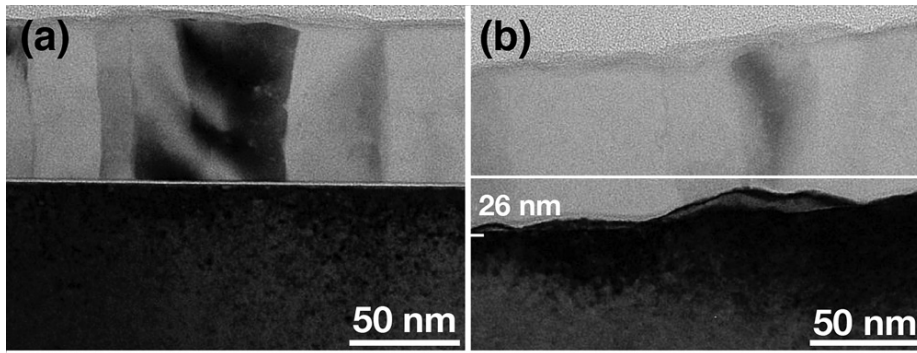
**Jury is still out. Need more work on this topic, both experimental and computational**

Hsieh *et al.*, *Phys. Rev. B*, **84**, 184107 (2011)

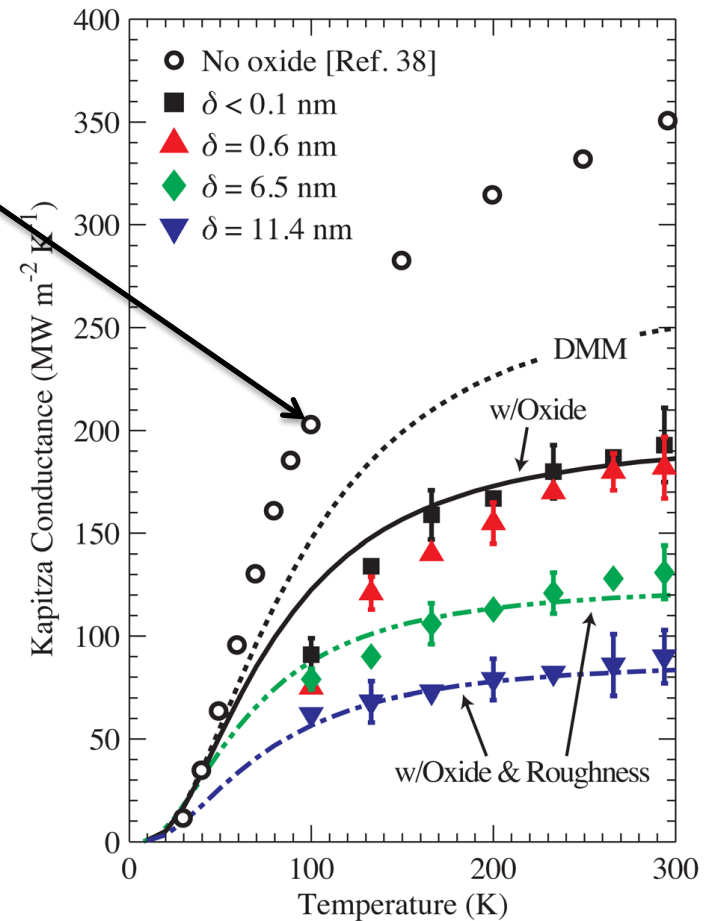


# Anharmonicity vs. disorder?

Data from: Minnich *et al. Phys. Rev. Lett.* **107**, 095901 (2011)



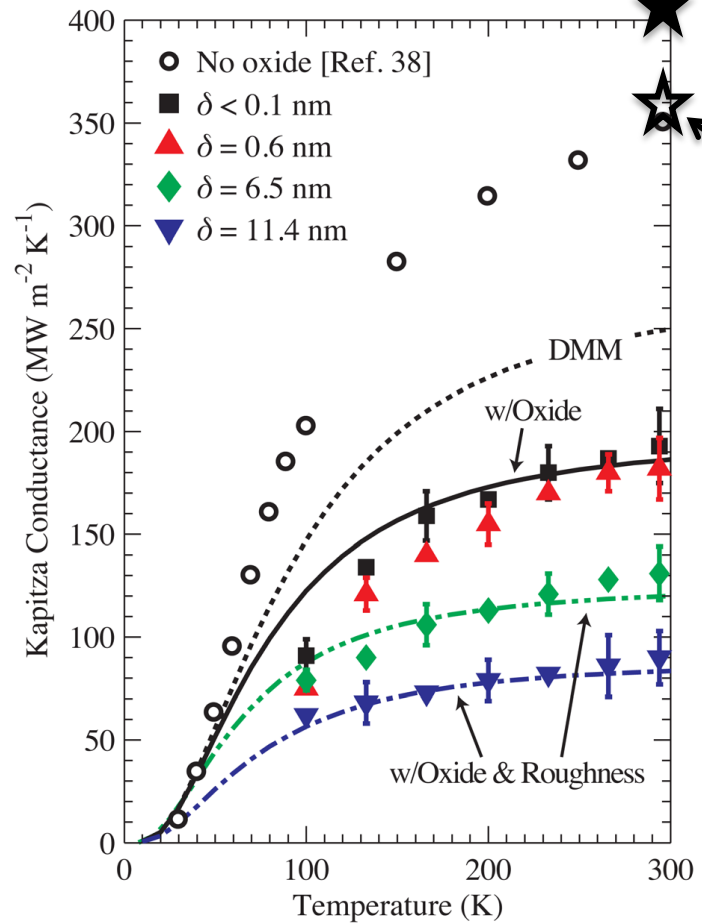
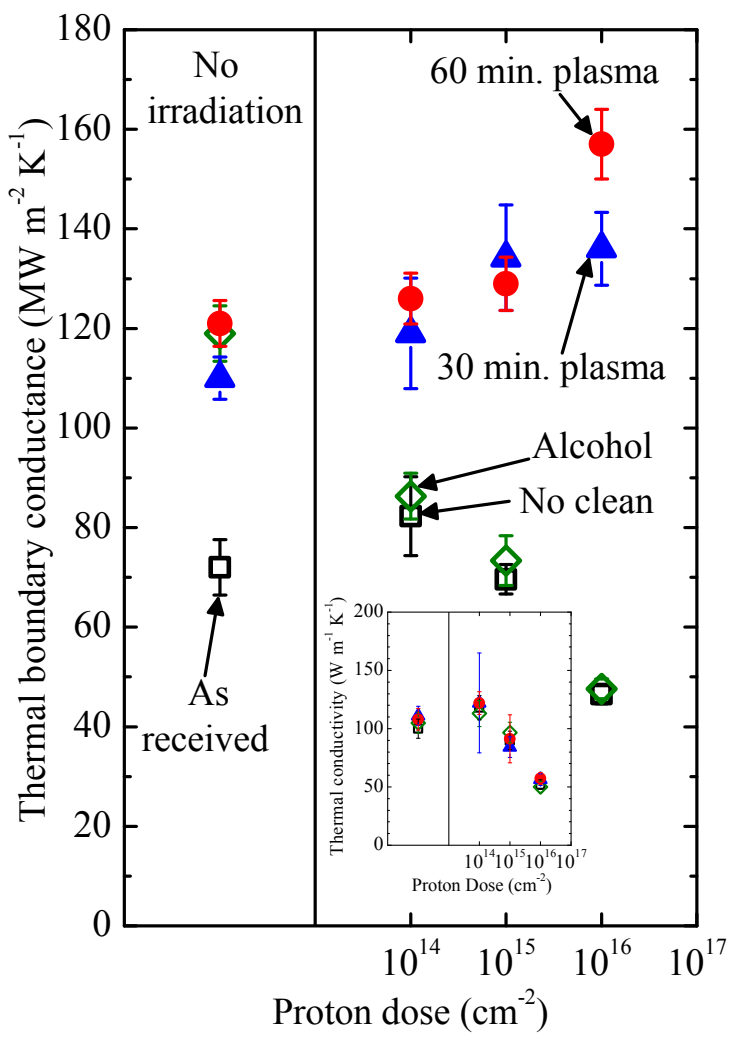
- Rough interfaces “flatten out” with temperature trends
- Removal of oxide increases change with temperature



Duda and Hopkins, *Appl. Phys. Lett.* **100**, 111602 (2012)

# Can disorder increase TBC/anharmonicity?

Gorham *et al.* under review  
**Ion mixing increases TBC**



Ion mixing,  
no oxide  
(Gorham)

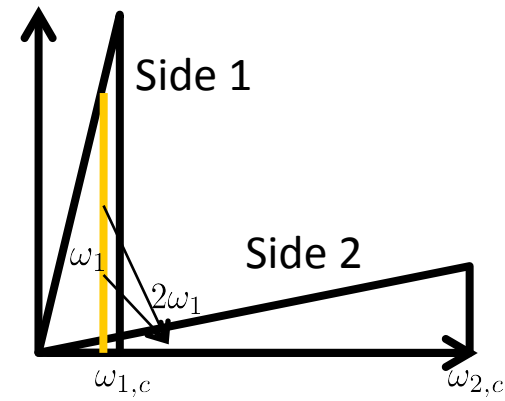
No ion  
mixing, no  
oxide  
(Gorham)

Duda and Hopkins, *Appl. Phys. Lett.* **100**, 111602 (2012)

# Theoretical developments

Let's switch gears and talk about pen and  
paper theoretical developments

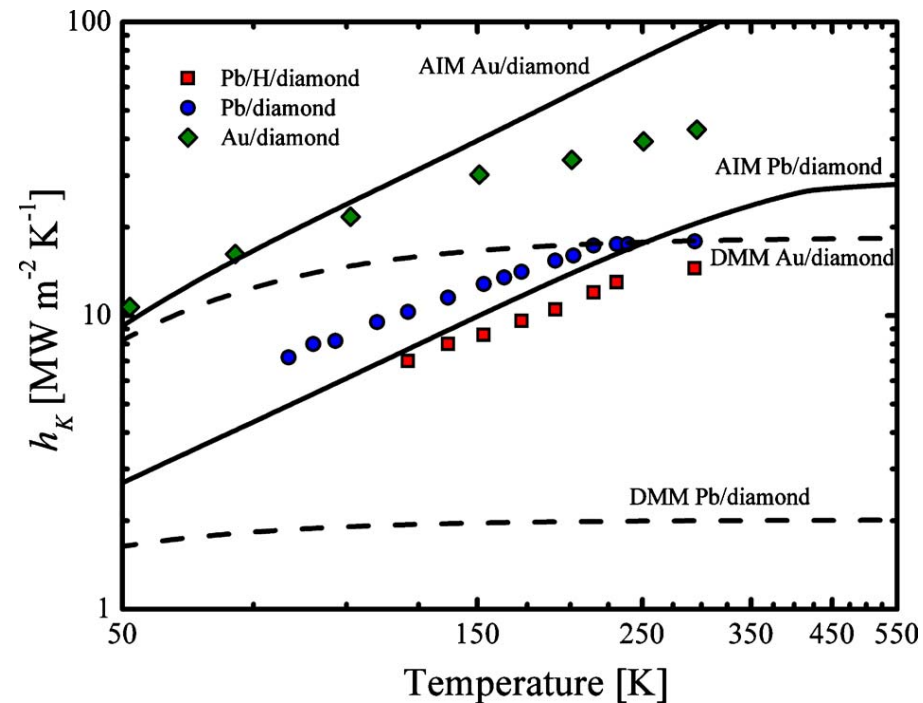
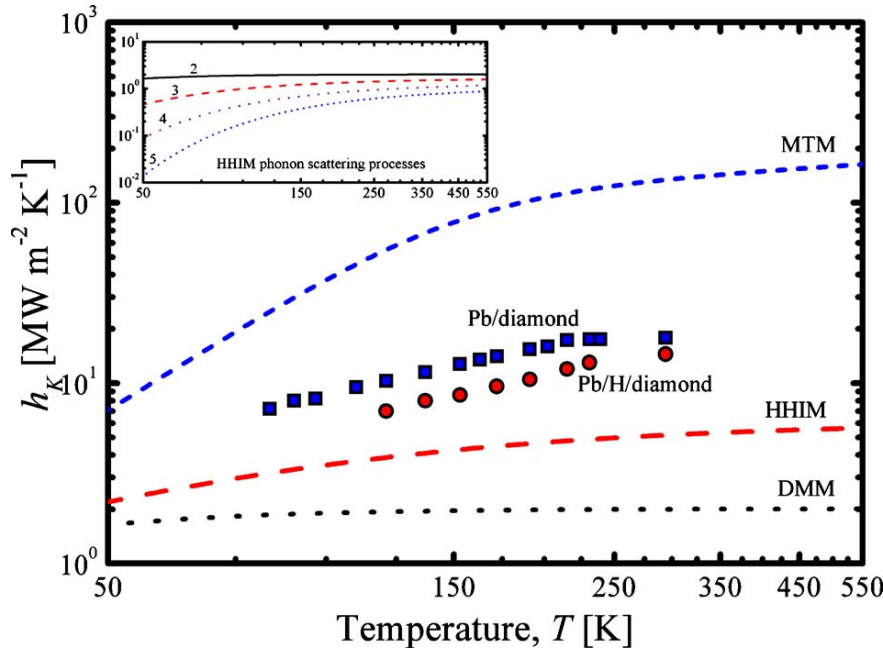
Can we model this (back to the beginning)



Selected inelastic scattering (higher harmonic)

Hopkins, *J. Appl. Phys.* 106, 013528 (2009)

Hopkins, Duda, Norris, *J. Heat Trans.* 133, 062401 (2011)



**Question: what is the most probable interaction? What are the interaction probability/phonon transition probabilities at interfaces?**

# What about in the classical limit? Can we model MD?

## On the Linear Temperature Dependence of Phonon Thermal Boundary Conductance in the Classical Limit

**John C. Duda**

Department of Mechanical and Aerospace Engineering,  
University of Virginia,  
Charlottesville, VA 22904;  
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**Pamela M. Norris**

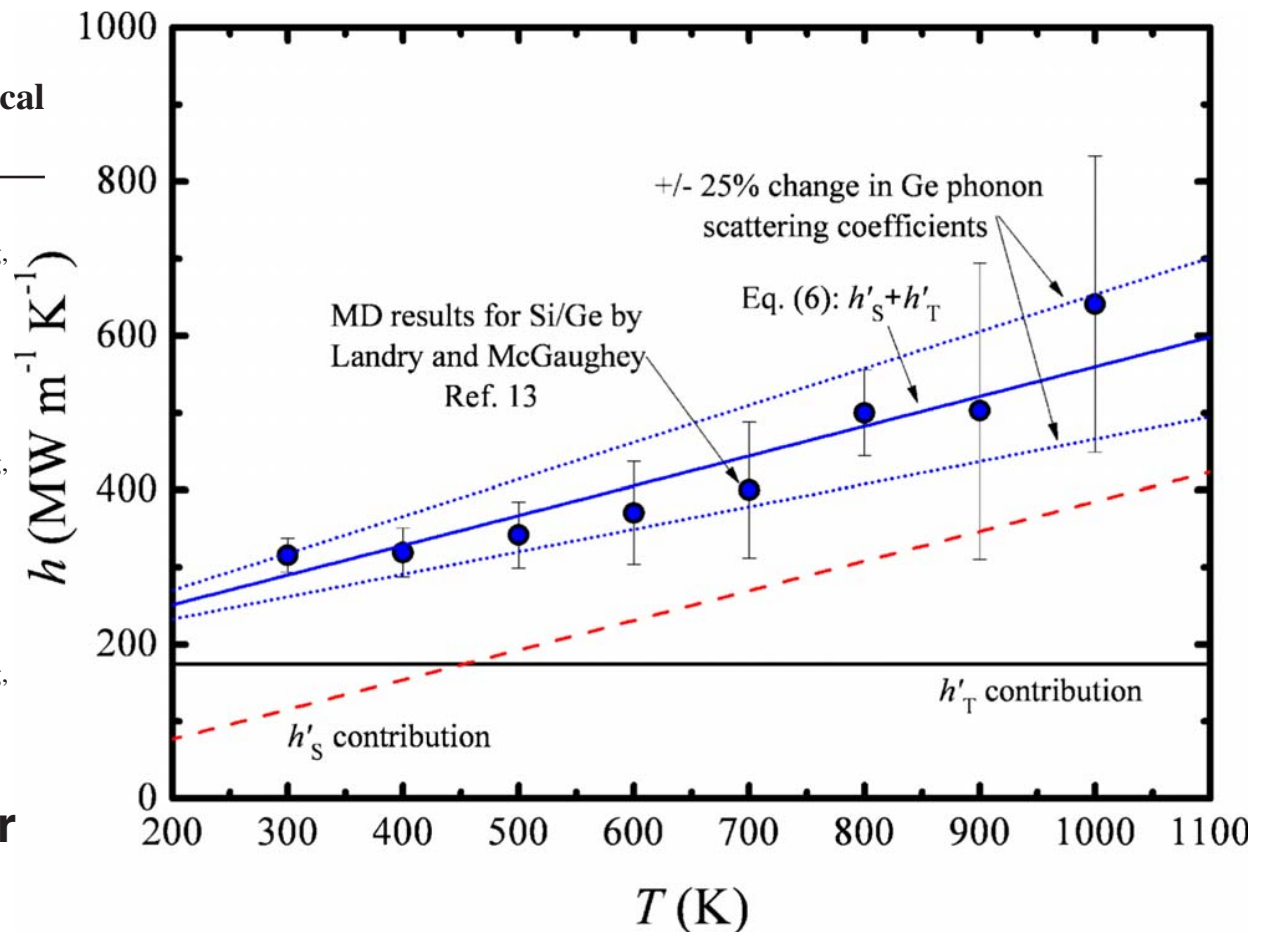
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**Journal of Heat Transfer**

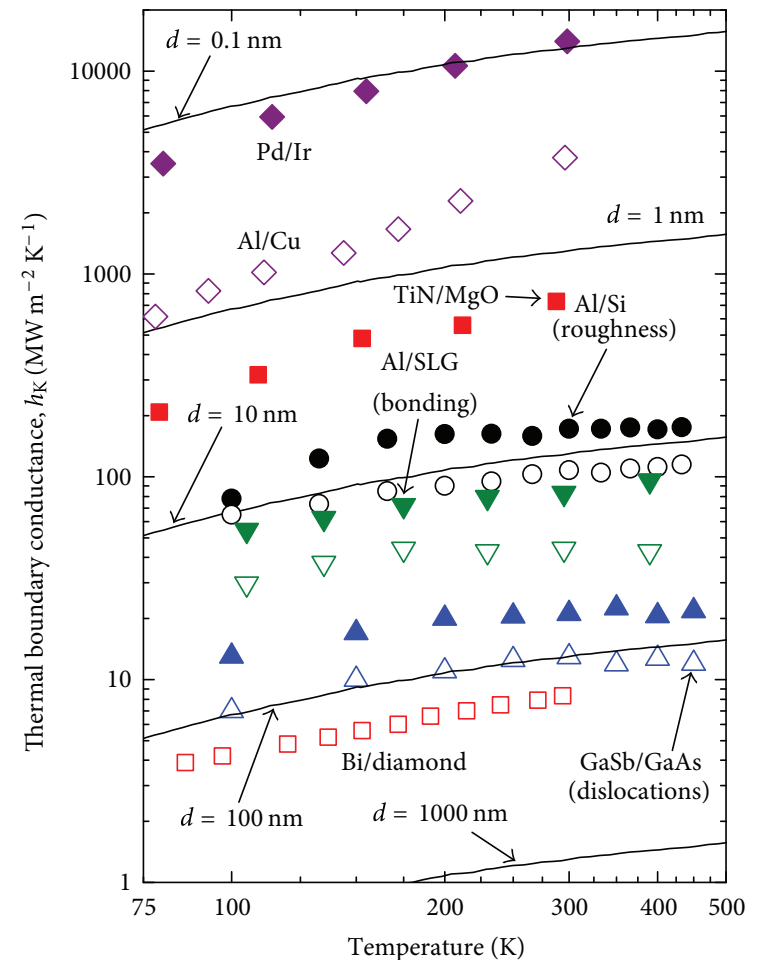
JULY 2011, Vol. 133 / 074501-1



**Phonons emitted across interface are scattered based on other material: linear T dependence comes from UMKLAPP SCATTERING TIME – this needs to be explored in more detail....**

# Challenges – can we push the extremes with anharmonicity?

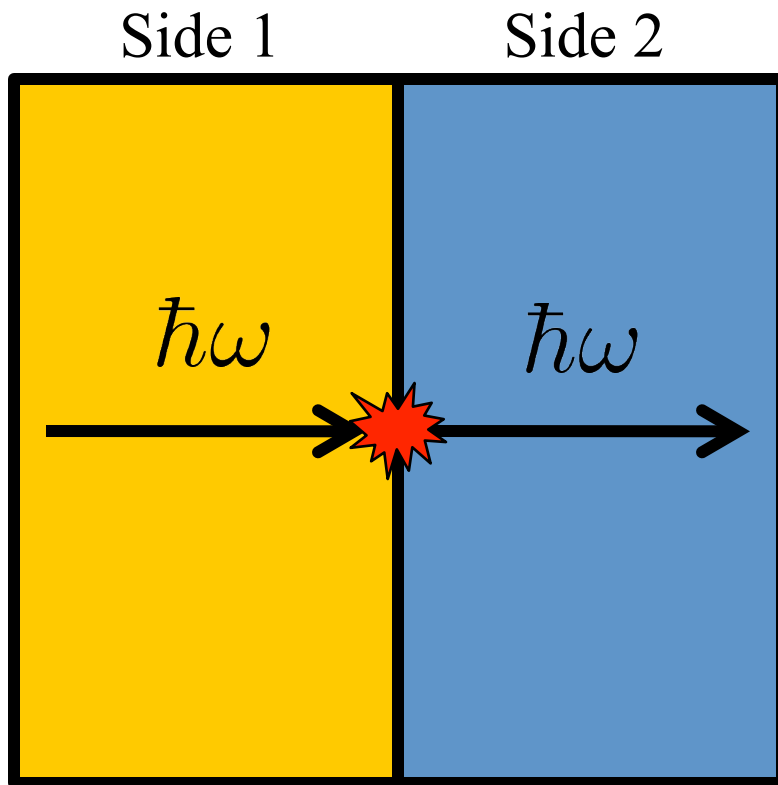
- Interplay between bonding and anharmonicity: what are the roles of 2 and “n-phonon” processes?
- Inelastic scattering vs. disorder: how do interfacial “imperfections” affect the anharmonic processes
- Can we understand anharmonicity from a “bonding” perspective with simulations? How big is “n” in a realistic picture (could  $n > 3$  actually exist?)
- BOTH materials are in classical limit: Can we bridge experiments with MD?



Hopkins, *ISRN Mechanical Engineering* **2013**, 682586 (2013)

# Interfacial phonon processes

**Two phonon scattering (elastic)**



**“n” phonon scattering (inelastic)**

